

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{r}}{dt^2}$$

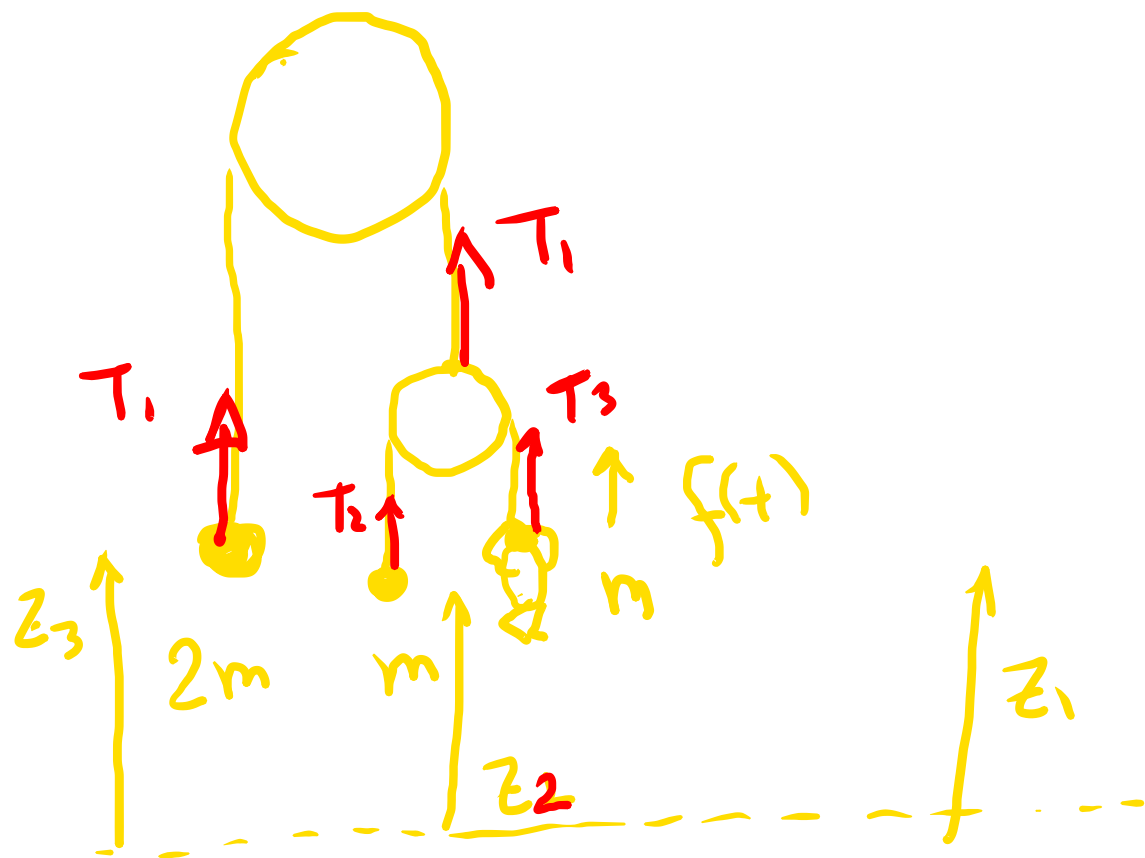
$$a_t = \frac{dv}{dt}$$

$$\left. \begin{array}{l} \vec{a} = a_t \hat{e}_t + \\ a_n \hat{e}_n \end{array} \right\}$$

\parallel
 v^2/R

$$a_n \hat{e}_n = \vec{a} - \frac{dv}{dt} \hat{e}_t$$

$$a_n = \left| \quad \right| \quad \parallel \quad \left| \right.$$



$$T_1 = T_2 + T_3$$

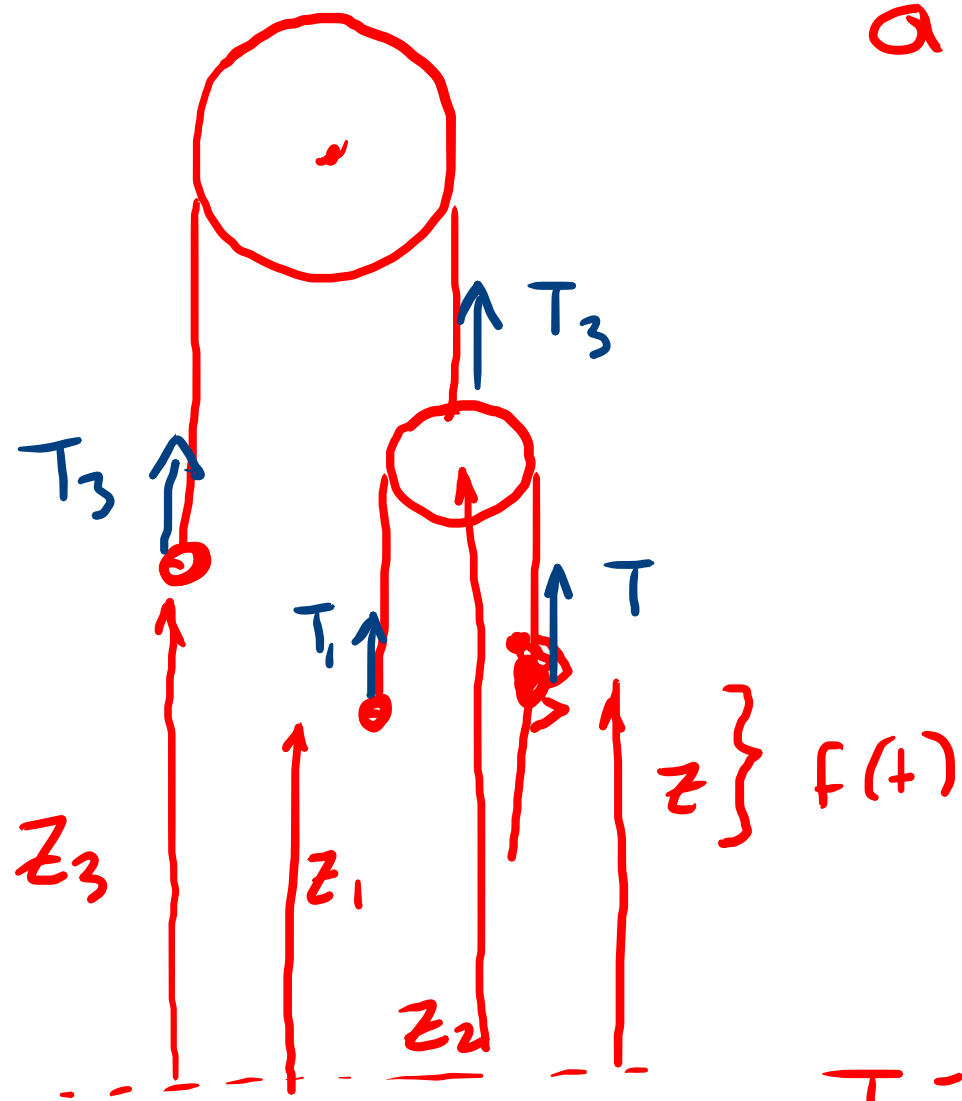
$$T_1 = 2m a_3$$

$$T_2 = m a_2$$

$$T_3 = m a_1$$

$$z_2 - z_1 = f(t) + C$$

$$z_3 - \left(\frac{z_2 + z_1}{2} \right) = C \quad ?$$



$$\underline{T_3 = T_1 + T}$$

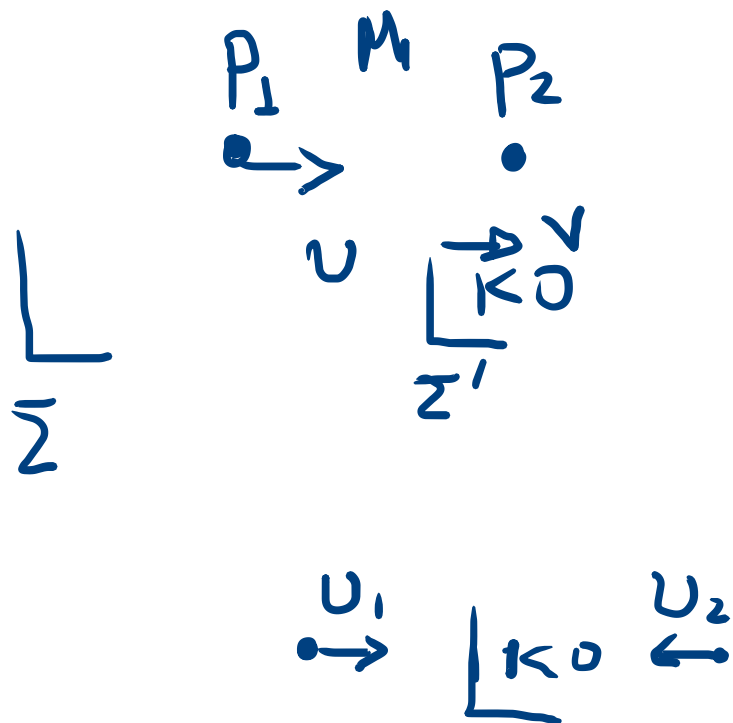
$$a = \frac{d^2 z}{dt^2} \quad a_3 = \frac{d^2 z_3}{dt^2}, \dots$$

$$\underline{z_3 + z_2 = C_1}$$

$$\underline{\frac{z_1 + (z - f)}{2} = z_2 + C_2}$$

$$\underline{T_3 = 2ma_3} \quad \underline{T_1 = ma_1} \quad \underline{T = ma}$$

агау $T_1, T, T_3, z_1, z_2, z_3, z$



$$\vec{P}_1' + \vec{P}_2' = 0$$

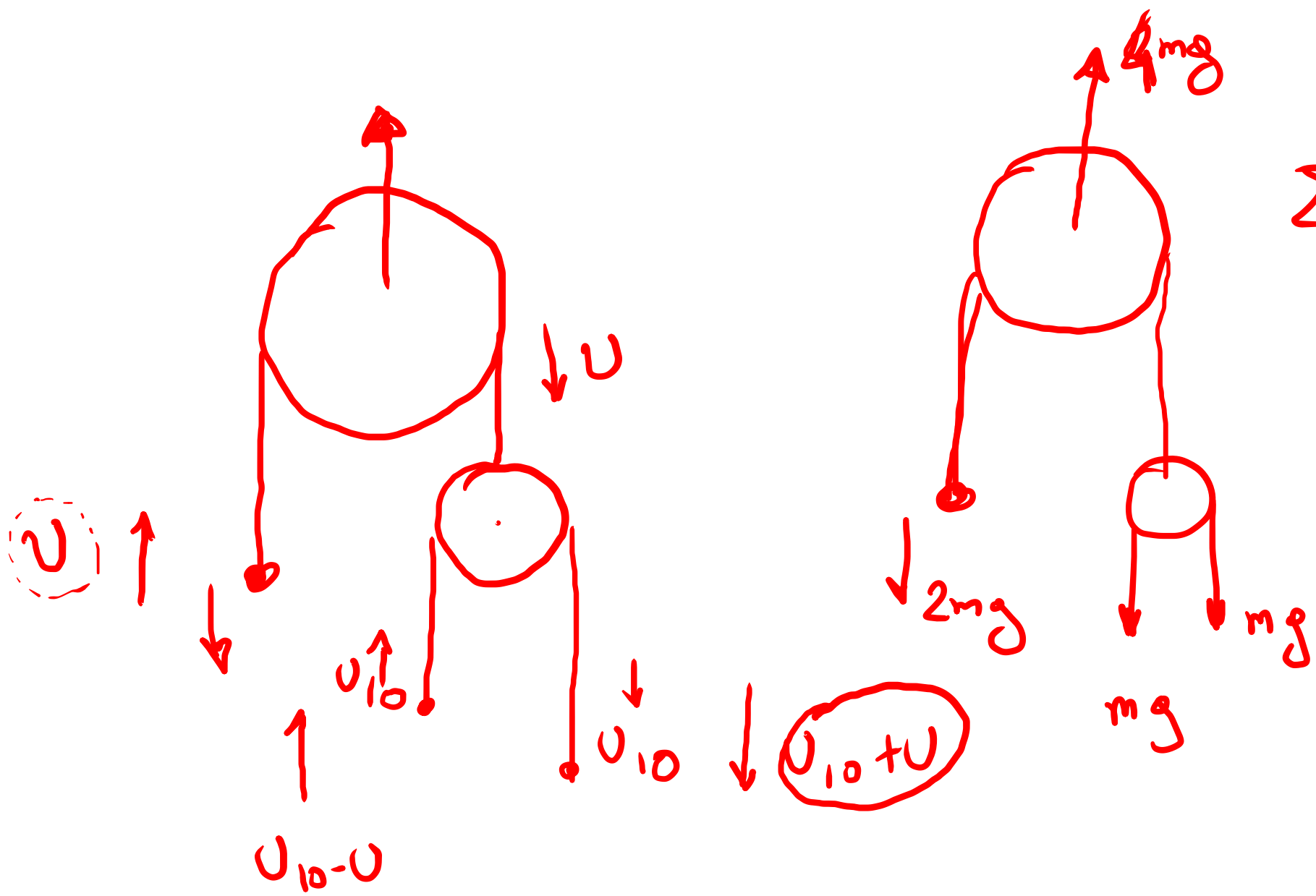
$$\vec{U}_1 = -\vec{U}_2$$

$$\vec{U}_2 = -\vec{V}_{K_0}$$

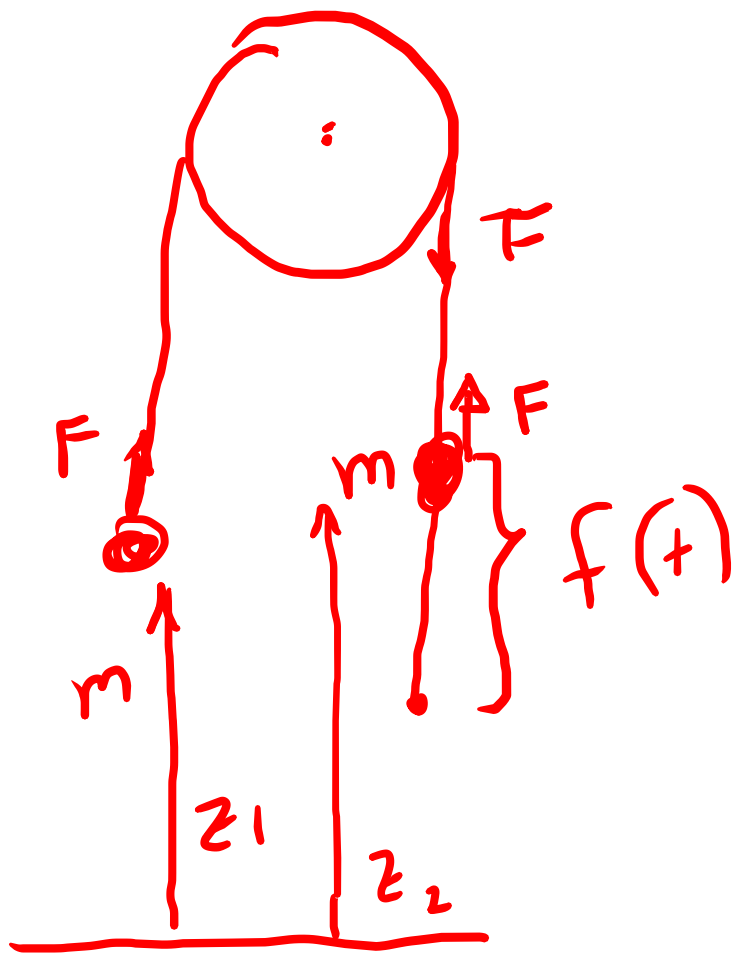
$$U_1 = \frac{U - V_{K_0}}{1 - UV_{K_0}/c^2} = V_{K_0} \Rightarrow \dots$$

$$\Gamma \left(\vec{P}_1 + \vec{P}_2 - V (E_1 + E_2) \right) = 0 \Rightarrow V$$

$$\gamma_1 m U_1 / \gamma_1 m + \gamma_2 m c^2 \vec{v} / \gamma_2 m c^2$$



$$\sum F_{\text{eff}} = 0$$



$$\underline{z_1 - (z_2 - f) = C}$$

$$F - mg = m \frac{d^2 z_2}{dt^2}$$

$$F - mg = m \frac{d^2 z_1}{dt^2}$$

$$\frac{d^2}{dt^2} (z_2 - z_1) = 0$$

• $m = 100 \text{ MeV}/c^2$

$\tau = 10^{-6} \text{ s}$ $H = 30 \text{ km}$

$p_{min} \text{ (MeV}/c) ? \quad \gamma u/c ?$

$\tau_{\text{lab}} = 10^{-3} \text{ s}$

$t = \gamma \tau$

$H/t = u$

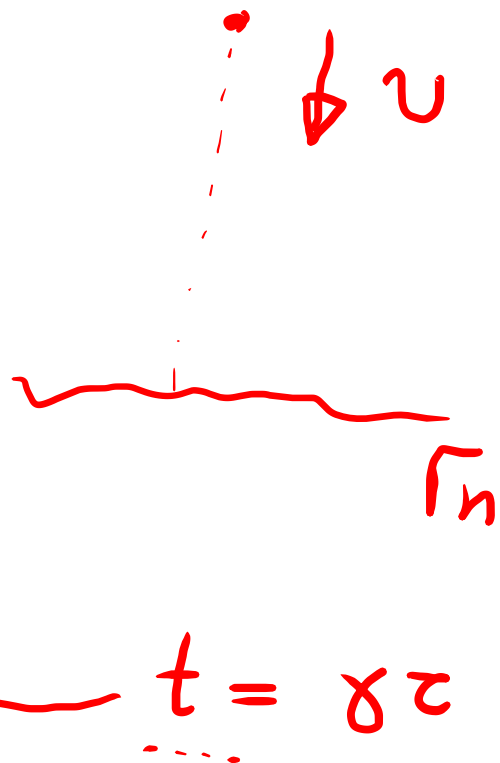
$\frac{H}{t} = \gamma u$

$p = m \gamma u$

$p_{min} = m \frac{H}{\tau} = 100 \frac{\text{MeV}}{c^2} \frac{30 \text{ km}}{10^{-6} \text{ s}} = 100 \cdot 100 \frac{\text{MeV}}{c}$

$\gamma = 10^3 \rightarrow \frac{u}{c} = \dots 1 - 10^{-6}$

$\frac{3 \times 10^7 \text{ km/s}}{3 \times 10^7 \text{ km/s}} = 3 \times 10^{10} \text{ m/s}$



$$A \rightarrow V = c/5$$

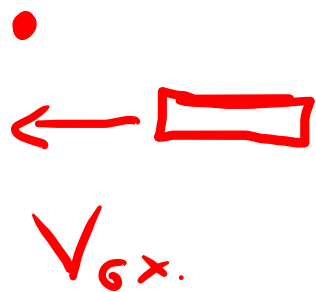


$$u = 3c/5$$

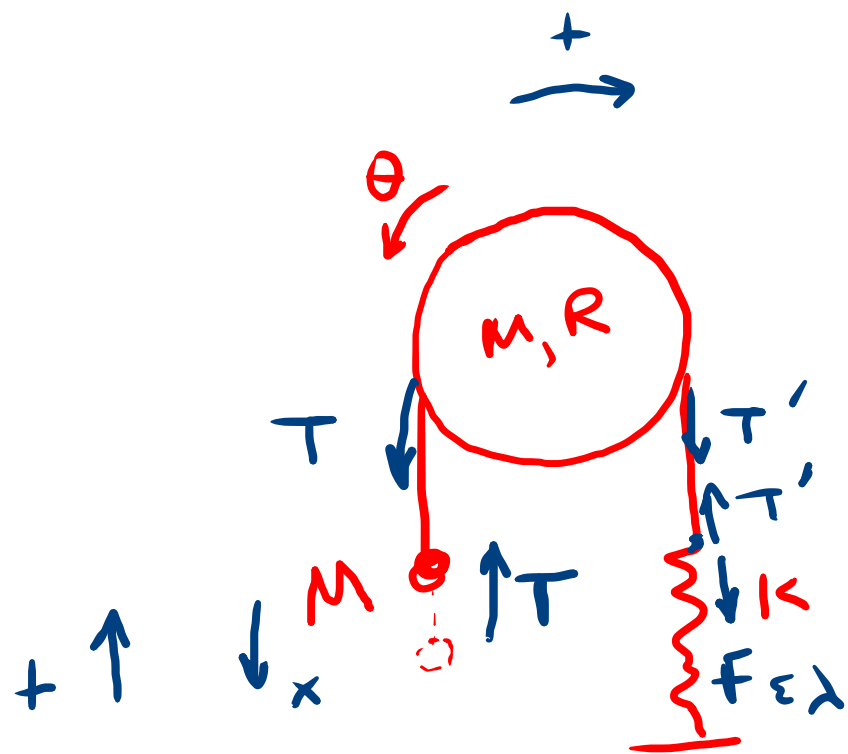


$$V_{\text{observed}} = V_{\text{proper}} = V - u = \frac{c}{5}$$

$$\left(\frac{V - u}{1 - Vu/c^2} \right) = V_{\text{obs}}$$



$$t = \frac{L}{V_{6x}} = \frac{L_0 / \gamma_{6x}}{V_{6x}}$$



$$I = \frac{1}{2} m R^2$$

$$T - Mg = Ma$$

$$\alpha = \frac{a}{R}$$

$$R(T' - T) = \frac{1}{2} m R^2 \alpha$$

$$T - Mg = m \frac{d^2 x}{dt^2}$$

$$T' - T = \frac{M}{2} a$$

$$\left. \begin{array}{l} T' - Mg = \frac{3m}{2} \frac{d^2 x}{dt^2} \\ = \\ -kx \end{array} \right\}$$

$$T' - T = \frac{M}{2} \frac{d^2 x}{dt^2}$$

$$T' = -kx$$

$$\boxed{T' = -kx}$$

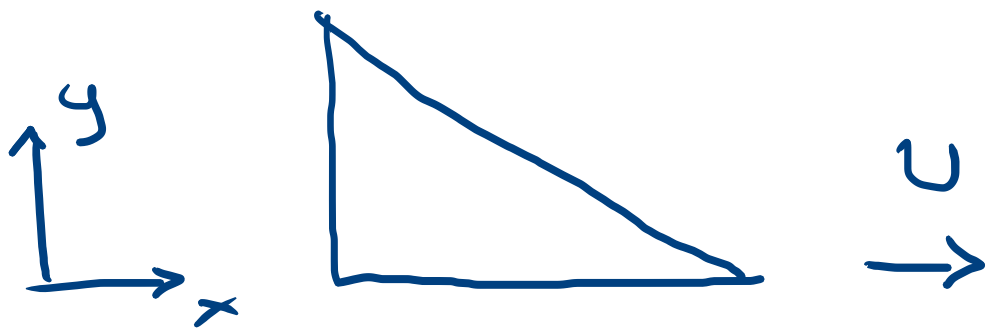
$$\frac{3M}{2} \frac{d^2 x}{dt^2} + kx = -Mg$$



$$\zeta = x + \frac{Mg}{k}$$

$$\frac{3M}{2} \frac{d^2 \zeta}{dt^2} + k\zeta = 0$$

$$\Rightarrow T = 2\pi \sqrt{\frac{\frac{3}{2}M}{k}}$$



$$\delta = 2$$

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$$\sigma = \frac{dm_{np}}{dx dy} = \frac{dm}{\frac{dx}{\delta} dy'} = \delta \sigma'$$



$$P_A = \rho g 2h$$

$$-PS = F = ma$$

$$-\rho g 2h S = \rho S \delta z a$$

$$La = \delta z a = -g 2h$$

$$L_0 - 2h$$

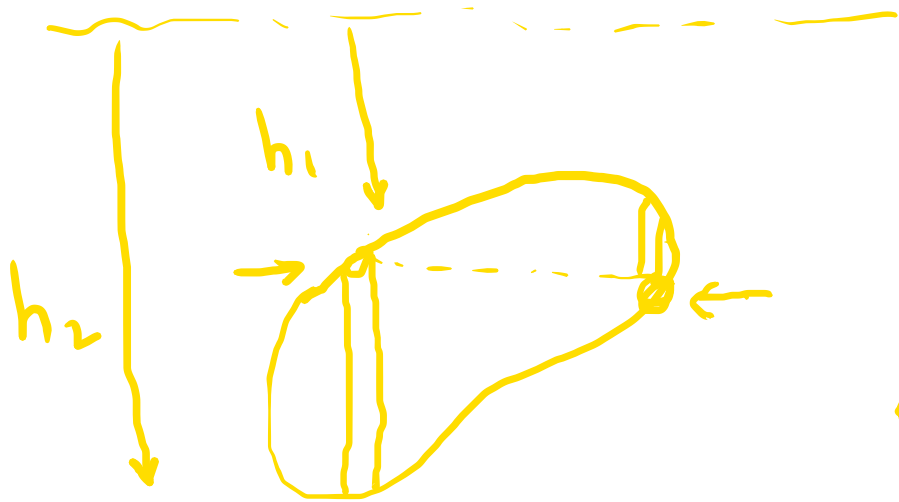


$$F_{\text{net}} = -\rho g S 2x$$

$$M \frac{d^2 x}{dt^2} = -\rho g S 2x$$

$$\omega^2 = \frac{2gS}{L_0} = \frac{2g}{L_0}$$

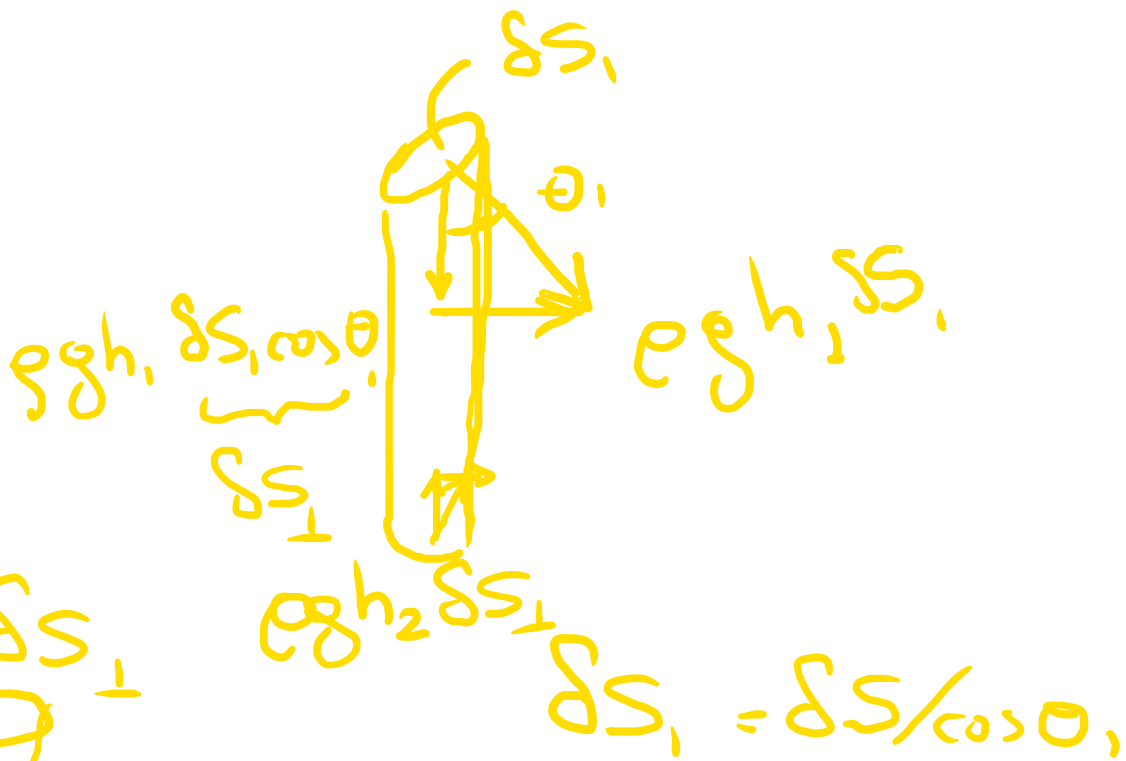
$$\frac{d^2 x}{dt^2} + \frac{2\rho g S}{\rho V} x = 0$$



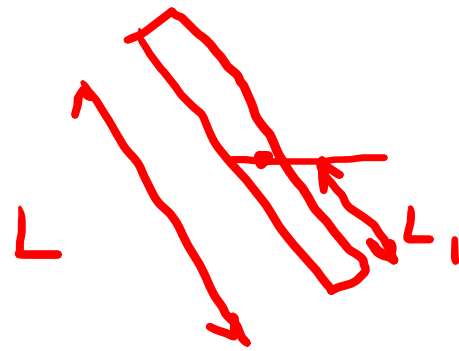
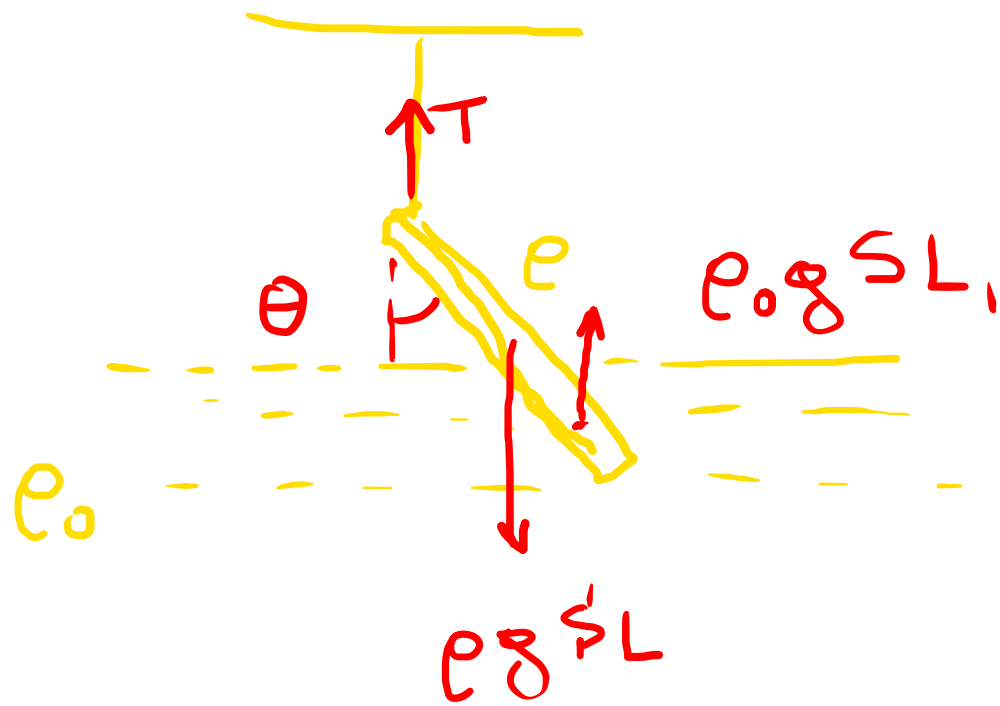
$$\frac{\rho g (h_2 - h_1) \delta S_{\perp}}{\delta V}$$



$$dS \cos \theta = dS_{\perp}$$



$$\delta S_{\perp} = \delta S / \cos \theta$$



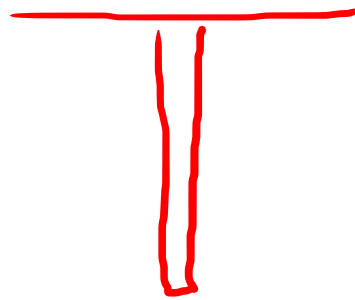
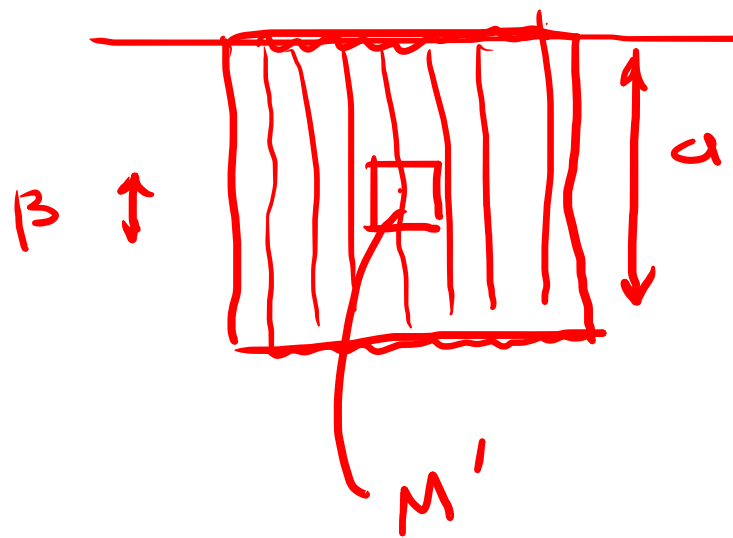
$$\underline{T + \rho_0 g S L_1 = \rho g S L}$$

$$\rho L^2 = \rho_0 L_1 (2L - L_1)$$

$$L_1^2 - 2L L_1 + \frac{\rho_0}{\rho} L^2 = 0$$

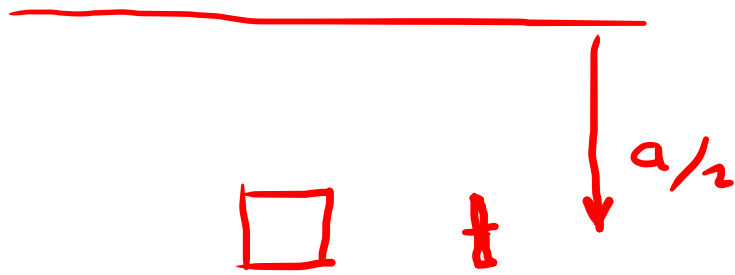
$$L_1 = \dots$$

$$\rho g S L \frac{L}{2} \sin \theta = \rho_0 g S L_1 \left(L - L_1 + \frac{L_1}{2} \right) \sin \theta$$



$$\frac{ML^2}{3}$$

$$M' \left[\frac{B^2}{12} + \left(\frac{a}{2} \right)^2 \right]$$



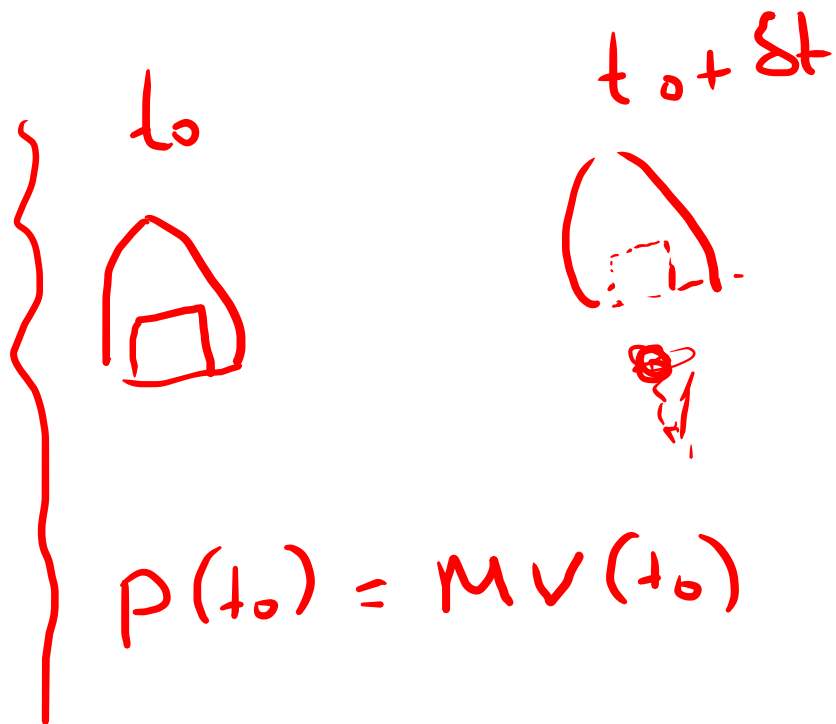
$$I_0 = \frac{Ma^2}{3}$$

$$I' = M \frac{B^2}{a^2} [\quad]$$

$$\frac{I_0 - I'}{I_0} = \frac{\frac{a^2}{3} - \frac{B^2}{a^2} [\quad]}{\frac{a^2}{3}} = 1 - \frac{3B^2}{a^2} [\quad]$$



$$\frac{dp}{dt} = M \frac{dv}{dt} + v_{rel} \frac{dM}{dt} = -Mg$$



$$t \in [t_0, t_0 + \delta t]$$

$$F = ma$$

$$p(t_0 + \delta t) = (M - \delta M)(v + \delta v) + \delta M(v - v_{rel})$$

$$-M(t_0)g = F(t_0) = \frac{\delta p}{\delta t}$$

235

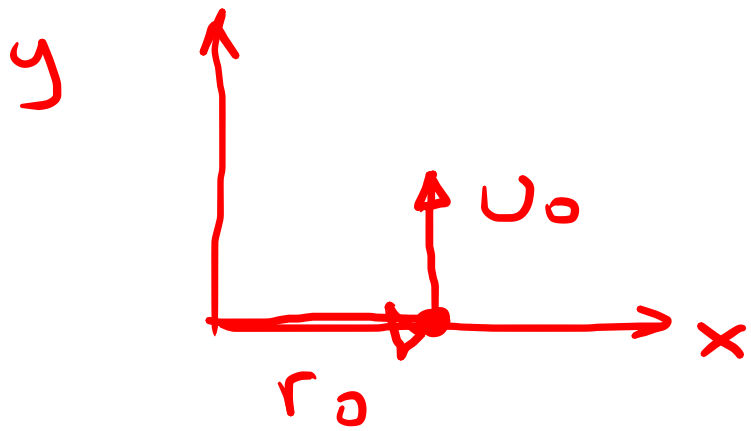
$$U = \frac{1}{2} m \omega^2 r^2$$

$$\vec{U}_0 \neq \vec{r}_0 \quad r_0 < r < U_0/\omega$$

.....

$$\vec{F} = -\vec{\nabla} U = -\frac{1}{2} m \omega^2 \underbrace{\vec{\nabla} (x^2 + y^2 + z^2)}$$

κεντρική $\vec{F} \parallel \vec{r}$ $\xrightarrow{2\vec{r}}$
 \rightarrow διατηρ. Γαργ.
 \rightarrow Διατηρ. ενέργειας
τροχιας



$$m \frac{d^2 x}{dt^2} = -m \omega^2 x$$

$$m \frac{d^2 y}{dt^2} = -m \omega^2 y$$

$$m \frac{d^2 z}{dt^2} = -m \omega^2 z$$

$$x(0) = r_0 \quad y(0) = 0 \quad z(0) = 0 \quad \dot{z}(t) = 0$$

$$v_x(0) = 0 \quad v_y(0) = U_0 \quad v_z(0) = 0$$

$$x = r_0 \cos \omega t \quad y = \frac{U_0}{\omega} \sin \omega t$$

$$-r_0 \leq x \leq r_0 \quad -\frac{U_0}{\omega} < y < \frac{U_0}{\omega}$$

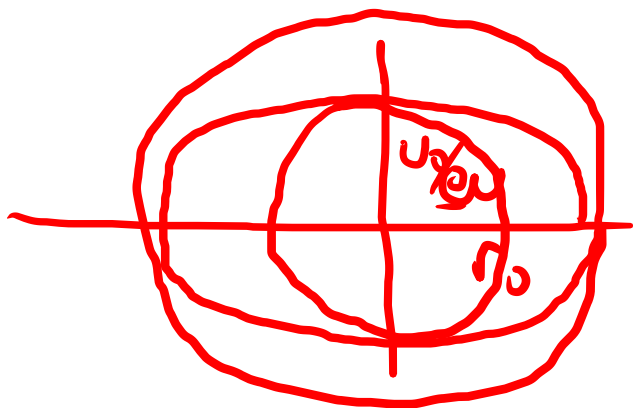
$$0 \leq \sqrt{x^2 + y^2} \leq \sqrt{r_0^2 + U_0^2 / \omega^2}$$

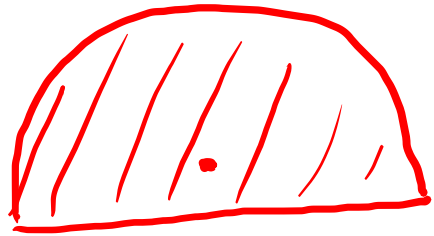
$$r = \sqrt{x^2 + y^2} = \sqrt{r_0^2 \cos^2 \omega t + \left(\frac{U_0}{\omega}\right)^2 \sin^2 \omega t}$$

$$\sqrt{r_0^2 (1 - \sin^2) + \frac{U_0^2}{\omega^2} \sin^2}$$

$$\sqrt{\frac{U_0^2}{\omega^2}} < \sqrt{r_0^2 - \underbrace{\left(r_0^2 - \frac{U_0^2}{\omega^2}\right)}_{\geq 0} \sin^2} < r_0$$

$$r_0 > \frac{U_0}{\omega}$$





$K M \rightarrow k m$

$$I = M R^2 \alpha$$

$$I' = M' R^2 \alpha = \frac{110}{100} M R^2 \alpha = \frac{110}{100} I$$