

PROBLEMS



Tutoring problem available (at instructor's discretion) in WileyPLUS and WebAssign

SSM

Worked-out solution available in Student Solutions Manual

WWW

Worked-out solution is at

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Number of dots indicates level of problem difficulty

ILW

Interactive solution is at



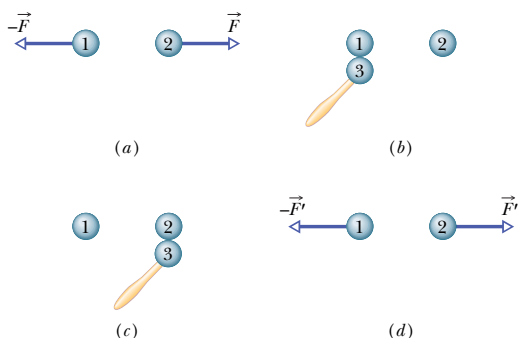
Additional information available in *The Flying Circus of Physics* and at flyingcircusofphysics.com

<http://www.wiley.com/college/halliday>

**sec. 21-4 Coulomb's Law**

•1 **SSM ILW** Of the charge  $Q$  initially on a tiny sphere, a portion  $q$  is to be transferred to a second, nearby sphere. Both spheres can be treated as particles. For what value of  $q/Q$  will the electrostatic force between the two spheres be maximized?

•2 Identical isolated conducting spheres 1 and 2 have equal charges and are separated by a distance that is large compared with their diameters (Fig. 21-21a). The electrostatic force acting on sphere 2 due to sphere 1 is  $\vec{F}$ . Suppose now that a third identical sphere 3, having an insulating handle and initially neutral, is touched first to sphere 1 (Fig. 21-21b), then to sphere 2 (Fig. 21-21c), and finally removed (Fig. 21-21d). The electrostatic force that now acts on sphere 2 has magnitude  $F'$ . What is the ratio  $F'/F$ ?



**Fig. 21-21** Problem 2.

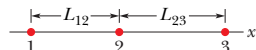
•3 **SSM** What must be the distance between point charge  $q_1 = 26.0 \mu\text{C}$  and point charge  $q_2 = -47.0 \mu\text{C}$  for the electrostatic force between them to have a magnitude of  $5.70 \text{ N}$ ?

•4 **ILW** In the return stroke of a typical lightning bolt, a current of  $2.5 \times 10^4 \text{ A}$  exists for  $20 \mu\text{s}$ . How much charge is transferred in this event?

•5 A particle of charge  $+3.00 \times 10^{-6} \text{ C}$  is  $12.0 \text{ cm}$  distant from a second particle of charge  $-1.50 \times 10^{-6} \text{ C}$ . Calculate the magnitude of the electrostatic force between the particles.

•6 **ILW** Two equally charged particles are held  $3.2 \times 10^{-3} \text{ m}$  apart and then released from rest. The initial acceleration of the first particle is observed to be  $7.0 \text{ m/s}^2$  and that of the second to be  $9.0 \text{ m/s}^2$ . If the mass of the first particle is  $6.3 \times 10^{-7} \text{ kg}$ , what are (a) the mass of the second particle and (b) the magnitude of the charge of each particle?

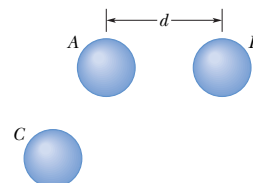
•7 In Fig. 21-22, three charged particles lie on an  $x$  axis. Particles 1 and 2 are fixed in place. Particle 3 is free to move, but the net



**Fig. 21-22** Problems 7 and 40.

electrostatic force on it from particles 1 and 2 happens to be zero. If  $L_{23} = L_{12}$ , what is the ratio  $q_1/q_2$ ?

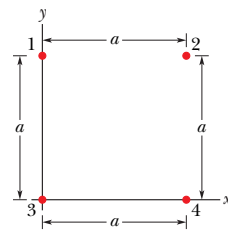
•8 In Fig. 21-23, three identical conducting spheres initially have the following charges: sphere  $A$ ,  $4Q$ ; sphere  $B$ ,  $-6Q$ ; and sphere  $C$ ,  $0$ . Spheres  $A$  and  $B$  are fixed in place, with a center-to-center separation that is much larger than the spheres.



**Fig. 21-23** Problems 8 and 65.

Two experiments are conducted. In experiment 1, sphere  $C$  is touched to sphere  $A$  and then (separately) to sphere  $B$ , and then it is removed. In experiment 2, starting with the same initial states, the procedure is reversed: Sphere  $C$  is touched to sphere  $B$  and then (separately) to sphere  $A$ , and then it is removed. What is the ratio of the electrostatic force between  $A$  and  $B$  at the end of experiment 2 to that at the end of experiment 1?

•9 **SSM WWW** Two identical conducting spheres, fixed in place, attract each other with an electrostatic force of  $0.108 \text{ N}$  when their center-to-center separation is  $50.0 \text{ cm}$ . The spheres are then connected by a thin conducting wire. When the wire is removed, the spheres repel each other with an electrostatic force of  $0.0360 \text{ N}$ . Of the initial charges on the spheres, with a positive net charge, what was (a) the negative charge on one of them and (b) the positive charge on the other?



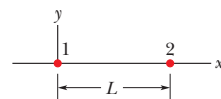
**Fig. 21-24** Problems 10, 11, and 70.

•10 **ILW** In Fig. 21-24, four particles form a square. The charges are  $q_1 = q_4 = Q$  and  $q_2 = q_3 = q$ . (a) What is  $Q/q$  if the net electrostatic force on particles 1 and 4 is zero? (b) Is there any value of  $q$  that makes the net electrostatic force on each of the four particles zero? Explain.

•11 **ILW** In Fig. 21-24, the particles have charges  $q_1 = -q_2 = 100 \text{ nC}$  and  $q_3 = -q_4 = 200 \text{ nC}$ , and distance  $a = 5.0 \text{ cm}$ . What are the (a)  $x$  and (b)  $y$  components of the net electrostatic force on particle 3?

•12 Two particles are fixed on an  $x$  axis. Particle 1 of charge  $40 \mu\text{C}$  is located at  $x = -2.0 \text{ cm}$ ; particle 2 of charge  $Q$  is located at  $x = 3.0 \text{ cm}$ . Particle 3 of charge magnitude  $20 \mu\text{C}$  is released from rest on the  $y$  axis at  $y = 2.0 \text{ cm}$ . What is the value of  $Q$  if the initial acceleration of particle 3 is in the positive direction of (a) the  $x$  axis and (b) the  $y$  axis?

•13 **ILW** In Fig. 21-25, particle 1 of charge  $+1.0 \mu\text{C}$  and particle 2 of charge  $-3.0 \mu\text{C}$  are held at separation  $L = 10.0 \text{ cm}$  on an  $x$  axis. If particle 3 of unknown charge  $q_3$  is to be located such that the net electrostatic force on it from particles 1 and 2 is zero, what must be the (a)  $x$  and (b)  $y$  coordinates of particle 3?



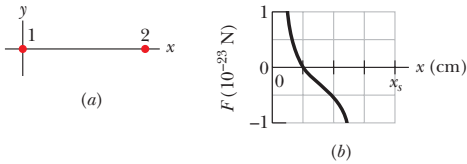
**Fig. 21-25** Problems 13, 19, 30, 58, and 67.

\*\* View All Solutions Here \*\*

**••14** Three particles are fixed on an  $x$  axis. Particle 1 of charge  $q_1$  is at  $x = -a$ , and particle 2 of charge  $q_2$  is at  $x = +a$ . If their net electrostatic force on particle 3 of charge  $+Q$  is to be zero, what must be the ratio  $q_1/q_2$  when particle 3 is at (a)  $x = +0.500a$  and (b)  $x = +1.50a$ ?

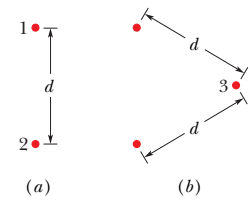
**••15** The charges and coordinates of two charged particles held fixed in an  $xy$  plane are  $q_1 = +3.0 \mu\text{C}$ ,  $x_1 = 3.5 \text{ cm}$ ,  $y_1 = 0.50 \text{ cm}$ , and  $q_2 = -4.0 \mu\text{C}$ ,  $x_2 = -2.0 \text{ cm}$ ,  $y_2 = 1.5 \text{ cm}$ . Find the (a) magnitude and (b) direction of the electrostatic force on particle 2 due to particle 1. At what (c)  $x$  and (d)  $y$  coordinates should a third particle of charge  $q_3 = +4.0 \mu\text{C}$  be placed such that the net electrostatic force on particle 2 due to particles 1 and 3 is zero?

**••16** In Fig. 21-26a, particle 1 (of charge  $q_1$ ) and particle 2 (of charge  $q_2$ ) are fixed in place on an  $x$  axis,  $8.00 \text{ cm}$  apart. Particle 3 (of charge  $q_3 = +8.00 \times 10^{-19} \text{ C}$ ) is to be placed on the line between particles 1 and 2 so that they produce a net electrostatic force  $\vec{F}_{3,\text{net}}$  on it. Figure 21-26b gives the  $x$  component of that force versus the coordinate  $x$  at which particle 3 is placed. The scale of the  $x$  axis is set by  $x_s = 8.0 \text{ cm}$ . What are (a) the sign of charge  $q_1$  and (b) the ratio  $q_2/q_1$ ?



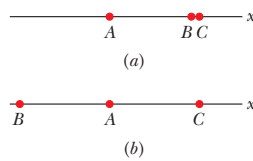
**Fig. 21-26** Problem 16.

**••17** In Fig. 21-27a, particles 1 and 2 have charge  $20.0 \mu\text{C}$  each and are held at separation distance  $d = 1.50 \text{ m}$ . (a) What is the magnitude of the electrostatic force on particle 1 due to particle 2? In Fig. 21-27b, particle 3 of charge  $20.0 \mu\text{C}$  is positioned so as to complete an equilateral triangle. (b) What is the magnitude of the net electrostatic force on particle 1 due to particles 2 and 3?



**Fig. 21-27** Problem 17.

**••18** In Fig. 21-28a, three positively charged particles are fixed on an  $x$  axis. Particles  $B$  and  $C$  are so close to each other that they can be considered to be at the same distance from particle  $A$ . The net force on particle  $A$  due to particles  $B$  and  $C$  is  $2.014 \times 10^{-23} \text{ N}$  in the negative direction of the  $x$  axis. In Fig. 21-28b, particle  $B$  has been moved to the opposite side of  $A$  but is still at the same distance from it. The net force on  $A$  is now  $2.877 \times 10^{-24} \text{ N}$  in the negative direction of the  $x$  axis. What is the ratio  $q_C/q_B$ ?

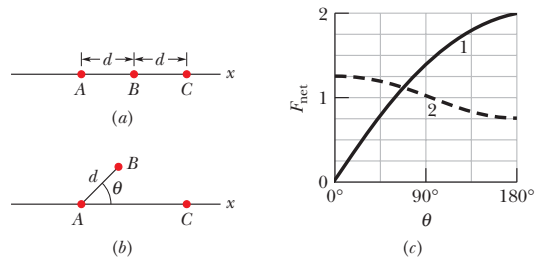


**Fig. 21-28** Problem 18.

**••19** In Fig. 21-25, particle 1 of charge  $+q$  and particle 2 of charge  $+4.00q$  are held at separation  $L = 9.00 \text{ cm}$  on an  $x$  axis. If particle 3 of charge  $q_3$  is to be located such that the three particles remain in place when released, what must be the (a)  $x$  and (b)  $y$  coordinates of particle 3, and (c) the ratio  $q_3/q$ ?

**••20** Figure 21-29a shows an arrangement of three charged particles separated by distance  $d$ . Particles  $A$  and  $C$  are fixed on the  $x$  axis, but particle  $B$  can be moved along a circle centered on parti-

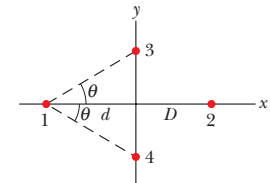
cle  $A$ . During the movement, a radial line between  $A$  and  $B$  makes an angle  $\theta$  relative to the positive direction of the  $x$  axis (Fig. 21-29b). The curves in Fig. 21-29c give, for two situations, the magnitude  $F_{\text{net}}$  of the net electrostatic force on particle  $A$  due to the other particles. That net force is given as a function of angle  $\theta$  and as a multiple of a basic amount  $F_0$ . For example on curve 1, at  $\theta = 180^\circ$ , we see that  $F_{\text{net}} = 2F_0$ . (a) For the situation corresponding to curve 1, what is the ratio of the charge of particle  $C$  to that of particle  $B$  (including sign)? (b) For the situation corresponding to curve 2, what is that ratio?



**Fig. 21-29** Problem 20.

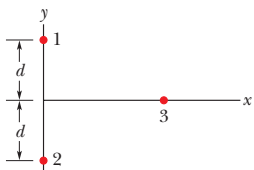
**••21** A nonconducting spherical shell, with an inner radius of  $4.0 \text{ cm}$  and an outer radius of  $6.0 \text{ cm}$ , has charge spread nonuniformly through its volume between its inner and outer surfaces. The volume charge density  $\rho$  is the charge per unit volume, with the unit coulomb per cubic meter. For this shell  $\rho = b/r$ , where  $r$  is the distance in meters from the center of the shell and  $b = 3.0 \mu\text{C}/\text{m}^3$ . What is the net charge in the shell?

**••22** Figure 21-30 shows an arrangement of four charged particles, with angle  $\theta = 30.0^\circ$  and distance  $d = 2.00 \text{ cm}$ . Particle 2 has charge  $q_2 = +8.00 \times 10^{-19} \text{ C}$ ; particles 3 and 4 have charges  $q_3 = q_4 = -1.60 \times 10^{-19} \text{ C}$ . (a) What is distance  $D$  between the origin and particle 2 if the net electrostatic force on particle 1 due to the other particles is zero? (b) If particles 3 and 4 were moved closer to the  $x$  axis but maintained their symmetry about that axis, would the required value of  $D$  be greater than, less than, or the same as in part (a)?



**Fig. 21-30** Problem 22.

**••23** In Fig. 21-31, particles 1 and 2 of charge  $q_1 = q_2 = +3.20 \times 10^{-19} \text{ C}$  are on a  $y$  axis at distance  $d = 17.0 \text{ cm}$  from the origin. Particle 3 of charge  $q_3 = +6.40 \times 10^{-19} \text{ C}$  is moved gradually along the  $x$  axis from  $x = 0$  to  $x = +5.0 \text{ m}$ . At what values of  $x$  will the magnitude of the electrostatic force on the third particle from the other two particles be (a) minimum and (b) maximum? What are the (c) minimum and (d) maximum magnitudes?



**Fig. 21-31** Problem 23.

**sec. 21-5 Charge Is Quantized**

**•24** Two tiny, spherical water drops, with identical charges of  $-1.00 \times 10^{-16} \text{ C}$ , have a center-to-center separation of  $1.00 \text{ cm}$ . (a) What is the magnitude of the electrostatic force acting between them? (b) How many excess electrons are on each drop, giving it its charge imbalance?

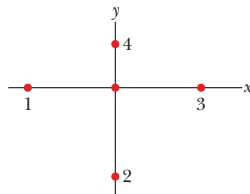
**•25 ILW** How many electrons would have to be removed from a coin to leave it with a charge of  $+1.0 \times 10^{-7} \text{ C}$ ?

**•26** What is the magnitude of the electrostatic force between a singly charged sodium ion ( $\text{Na}^+$ , of charge  $+e$ ) and an adjacent singly charged chlorine ion ( $\text{Cl}^-$ , of charge  $-e$ ) in a salt crystal if their separation is  $2.82 \times 10^{-10} \text{ m}$ ?

**•27 SSM** The magnitude of the electrostatic force between two identical ions that are separated by a distance of  $5.0 \times 10^{-10} \text{ m}$  is  $3.7 \times 10^{-9} \text{ N}$ . (a) What is the charge of each ion? (b) How many electrons are “missing” from each ion (thus giving the ion its charge imbalance)?

**•28** A current of  $0.300 \text{ A}$  through your chest can send your heart into fibrillation, ruining the normal rhythm of heartbeat and disrupting the flow of blood (and thus oxygen) to your brain. If that current persists for  $2.00 \text{ min}$ , how many conduction electrons pass through your chest?

**•29** In Fig. 21-32, particles 2 and 4, of charge  $-e$ , are fixed in place on a  $y$  axis, at  $y_2 = -10.0 \text{ cm}$  and  $y_4 = 5.00 \text{ cm}$ . Particles 1 and 3, of charge  $-e$ , can be moved along the  $x$  axis. Particle 5, of charge  $+e$ , is fixed at the origin. Initially particle 1 is at  $x_1 = -10.0 \text{ cm}$  and particle 3 is at  $x_3 = 10.0 \text{ cm}$ . (a) To what  $x$  value must particle 1 be moved to rotate the direction of the net electric force  $\vec{F}_{\text{net}}$  on particle 5 by  $30^\circ$  counterclockwise? (b) With particle 1 fixed at its new position, to what  $x$  value must you move particle 3 to rotate  $\vec{F}_{\text{net}}$  back to its original direction?

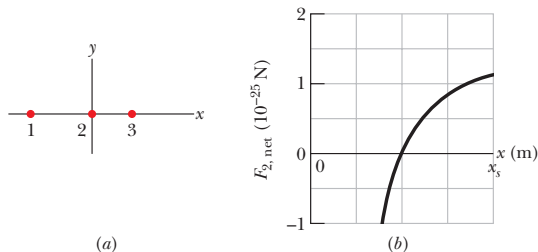


**Fig. 21-32** Problem 29.

**•30** In Fig. 21-25, particles 1 and 2 are fixed in place on an  $x$  axis, at a separation of  $L = 8.00 \text{ cm}$ . Their charges are  $q_1 = +e$  and  $q_2 = -27e$ . Particle 3 with charge  $q_3 = +4e$  is to be placed on the line between particles 1 and 2, so that they produce a net electrostatic force  $\vec{F}_{3,\text{net}}$  on it. (a) At what coordinate should particle 3 be placed to minimize the magnitude of that force? (b) What is that minimum magnitude?

**•31 ILW** Earth’s atmosphere is constantly bombarded by *cosmic ray protons* that originate somewhere in space. If the protons all passed through the atmosphere, each square meter of Earth’s surface would intercept protons at the average rate of  $1500$  protons per second. What would be the electric current intercepted by the total surface area of the planet?

**•32** Figure 21-33a shows charged particles 1 and 2 that are fixed in place on an  $x$  axis. Particle 1 has a charge with a magnitude of  $|q_1| = 8.00e$ . Particle 3 of charge  $q_3 = +8.00e$  is initially on the  $x$  axis near particle 2. Then particle 3 is gradually moved in the positive direction of

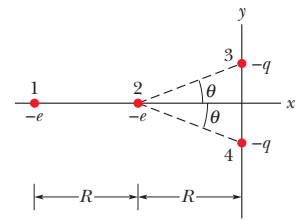


**Fig. 21-33** Problem 32.

the  $x$  axis. As a result, the magnitude of the net electrostatic force  $\vec{F}_{2,\text{net}}$  on particle 2 due to particles 1 and 3 changes. Figure 21-33b gives the  $x$  component of that net force as a function of the position  $x$  of particle 3. The scale of the  $x$  axis is set by  $x_s = 0.80 \text{ m}$ . The plot has an asymptote of  $F_{2,\text{net}} = 1.5 \times 10^{-25} \text{ N}$  as  $x \rightarrow \infty$ . As a multiple of  $e$  and including the sign, what is the charge  $q_2$  of particle 2?

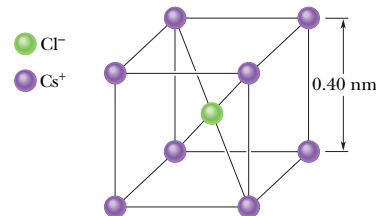
**•33** Calculate the number of coulombs of positive charge in  $250 \text{ cm}^3$  of (neutral) water. (*Hint:* A hydrogen atom contains one proton; an oxygen atom contains eight protons.)

**•34** Figure 21-34 shows electrons 1 and 2 on an  $x$  axis and charged ions 3 and 4 of identical charge  $-q$  and at identical angles  $\theta$ . Electron 2 is free to move; the other three particles are fixed in place at horizontal distances  $R$  from electron 2 and are intended to hold electron 2 in place. For physically possible values of  $q \leq 5e$ , what are the (a) smallest, (b) second smallest, and (c) third smallest values of  $\theta$  for which electron 2 is held in place?



**Fig. 21-34** Problem 34.

**•35 SSM** In crystals of the salt cesium chloride, cesium ions  $\text{Cs}^+$  form the eight corners of a cube and a chlorine ion  $\text{Cl}^-$  is at the cube’s center (Fig. 21-35). The edge length of the cube is  $0.40 \text{ nm}$ . The  $\text{Cs}^+$  ions are each deficient by one electron (and thus each has a charge of  $+e$ ), and the  $\text{Cl}^-$  ion has one excess electron (and thus has a charge of  $-e$ ). (a) What is the magnitude of the net electrostatic force exerted on the  $\text{Cl}^-$  ion by the eight  $\text{Cs}^+$  ions at the corners of the cube? (b) If one of the  $\text{Cs}^+$  ions is missing, the crystal is said to have a *defect*; what is the magnitude of the net electrostatic force exerted on the  $\text{Cl}^-$  ion by the seven remaining  $\text{Cs}^+$  ions?



**Fig. 21-35** Problem 35.

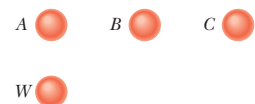
**sec. 21-6 Charge Is Conserved**

**•36** Electrons and positrons are produced by the nuclear transformations of protons and neutrons known as *beta decay*. (a) If a proton transforms into a neutron, is an electron or a positron produced? (b) If a neutron transforms into a proton, is an electron or a positron produced?

**•37 SSM** Identify X in the following nuclear reactions: (a)  $^1\text{H} + ^9\text{Be} \rightarrow \text{X} + \text{n}$ ; (b)  $^{12}\text{C} + ^1\text{H} \rightarrow \text{X}$ ; (c)  $^{15}\text{N} + ^1\text{H} \rightarrow ^4\text{He} + \text{X}$ . Appendix F will help.

**Additional Problems**

**38** Figure 21-36 shows four identical conducting spheres that are actually well separated from one another. Sphere W (with an initial charge of zero) is touched to sphere



**Fig. 21-36** Problem 38.

\*\* View All Solutions Here \*\*

$A$  and then they are separated. Next, sphere  $W$  is touched to sphere  $B$  (with an initial charge of  $-32e$ ) and then they are separated. Finally, sphere  $W$  is touched to sphere  $C$  (with an initial charge of  $+48e$ ), and then they are separated. The final charge on sphere  $W$  is  $+18e$ . What was the initial charge on sphere  $A$ ?

**39 SSM** In Fig. 21-37, particle 1 of charge  $+4e$  is above a floor by distance  $d_1 = 2.00$  mm and particle 2 of charge  $+6e$  is on the floor, at distance  $d_2 = 6.00$  mm horizontally from particle 1. What is the  $x$  component of the electrostatic force on particle 2 due to particle 1?

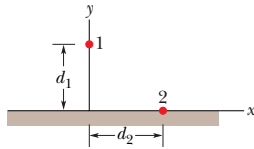


Fig. 21-37 Problem 39.

**40** In Fig. 21-22, particles 1 and 2 are fixed in place, but particle 3 is free to move. If the net electrostatic force on particle 3 due to particles 1 and 2 is zero and  $L_{23} = 2.00L_{12}$ , what is the ratio  $q_1/q_2$ ?

**41** (a) What equal positive charges would have to be placed on Earth and on the Moon to neutralize their gravitational attraction? (b) Why don't you need to know the lunar distance to solve this problem? (c) How many kilograms of hydrogen ions (that is, protons) would be needed to provide the positive charge calculated in (a)?

**42** In Fig. 21-38, two tiny conducting balls of identical mass  $m$  and identical charge  $q$  hang from nonconducting threads of length  $L$ . Assume that  $\theta$  is so small that  $\tan \theta$  can be replaced by its approximate equal,  $\sin \theta$ . (a) Show that

$$x = \left( \frac{q^2 L}{2\pi\epsilon_0 mg} \right)^{1/3}$$

gives the equilibrium separation  $x$  of the balls. (b) If  $L = 120$  cm,  $m = 10$  g, and  $x = 5.0$  cm, what is  $|q|$ ?

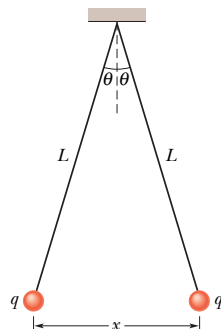


Fig. 21-38 Problems 42 and 43.

**43** (a) Explain what happens to the balls of Problem 42 if one of them is discharged (loses its charge  $q$  to, say, the ground). (b) Find the new equilibrium separation  $x$ , using the given values of  $L$  and  $m$  and the computed value of  $|q|$ .

**44 SSM** How far apart must two protons be if the magnitude of the electrostatic force acting on either one due to the other is equal to the magnitude of the gravitational force on a proton at Earth's surface?

**45** How many megacoulombs of positive charge are in 1.00 mol of neutral molecular-hydrogen gas ( $H_2$ )?

**46** In Fig. 21-39, four particles are fixed along an  $x$  axis, separated by distances  $d = 2.00$  cm. The charges are  $q_1 = +2e$ ,  $q_2 = -e$ ,  $q_3 = +e$ , and  $q_4 = +4e$ , with  $e = 1.60 \times 10^{-19}$  C. In unit-vector notation, what is the net electrostatic force on (a) particle 1 and (b) particle 2 due to the other particles?

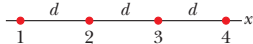


Fig. 21-39 Problem 46.

**47** Point charges of  $+6.0 \mu\text{C}$  and  $-4.0 \mu\text{C}$  are placed on an  $x$  axis, at  $x = 8.0$  m and  $x = 16$  m, respectively. What charge must be placed at  $x = 24$  m so that any charge placed at the origin would experience no electrostatic force?

**48** In Fig. 21-40, three identical conducting spheres form an equilateral triangle of side length  $d = 20.0$  cm. The sphere radii are much smaller than  $d$ , and the sphere charges are  $q_A = -2.00$  nC,  $q_B = -4.00$  nC, and  $q_C = +8.00$  nC. (a) What is the magnitude of the electrostatic force between spheres  $A$  and  $C$ ? The following steps are then taken:  $A$  and  $B$  are connected by a thin wire and then disconnected;  $B$  is grounded by the wire, and the wire is then removed;  $B$  and  $C$  are connected by the wire and then disconnected. What now are the magnitudes of the electrostatic force (b) between spheres  $A$  and  $C$  and (c) between spheres  $B$  and  $C$ ?

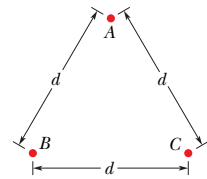


Fig. 21-40 Problem 48.

**49** A neutron consists of one "up" quark of charge  $+2e/3$  and two "down" quarks each having charge  $-e/3$ . If we assume that the down quarks are  $2.6 \times 10^{-15}$  m apart inside the neutron, what is the magnitude of the electrostatic force between them?

**50** Figure 21-41 shows a long, nonconducting, massless rod of length  $L$ , pivoted at its center and balanced with a block of weight  $W$  at a distance  $x$  from the left end. At the left and right ends of the rod are attached small conducting spheres with positive charges  $q$  and  $2q$ , respectively. A distance  $h$  directly beneath each of these spheres is a fixed sphere with positive charge  $Q$ . (a) Find the distance  $x$  when the rod is horizontal and balanced. (b) What value should  $h$  have so that the rod exerts no vertical force on the bearing when the rod is horizontal and balanced?

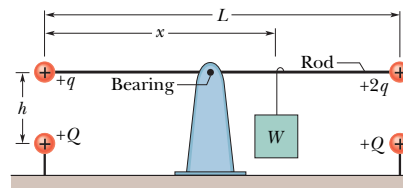


Fig. 21-41 Problem 50.

**51** A charged nonconducting rod, with a length of 2.00 m and a cross-sectional area of  $4.00 \text{ cm}^2$ , lies along the positive side of an  $x$  axis with one end at the origin. The volume charge density  $\rho$  is charge per unit volume in coulombs per cubic meter. How many excess electrons are on the rod if  $\rho$  is (a) uniform, with a value of  $-4.00 \mu\text{C}/\text{m}^3$ , and (b) nonuniform, with a value given by  $\rho = bx^2$ , where  $b = -2.00 \mu\text{C}/\text{m}^5$ ?


**52** A particle of charge  $Q$  is fixed at the origin of an  $xy$  coordinate system. At  $t = 0$  a particle ( $m = 0.800$  g,  $q = 4.00 \mu\text{C}$ ) is located on the  $x$  axis at  $x = 20.0$  cm, moving with a speed of 50.0 m/s in the positive  $y$  direction. For what value of  $Q$  will the moving particle execute circular motion? (Neglect the gravitational force on the particle.)

**53** What would be the magnitude of the electrostatic force between two 1.00 C point charges separated by a distance of (a) 1.00 m and (b) 1.00 km if such point charges existed (they do not) and this configuration could be set up?

**54** A charge of  $6.0 \mu\text{C}$  is to be split into two parts that are then separated by 3.0 mm. What is the maximum possible magnitude of the electrostatic force between those two parts?

\*\* View All Solutions Here \*\*

**55** Of the charge  $Q$  on a tiny sphere, a fraction  $\alpha$  is to be transferred to a second, nearby sphere. The spheres can be treated as particles. (a) What value of  $\alpha$  maximizes the magnitude  $F$  of the electrostatic force between the two spheres? What are the (b) smaller and (c) larger values of  $\alpha$  that put  $F$  at half the maximum magnitude?

**56**  If a cat repeatedly rubs against your cotton slacks on a dry day, the charge transfer between the cat hair and the cotton can leave you with an excess charge of  $-2.00 \mu\text{C}$ . (a) How many electrons are transferred between you and the cat?

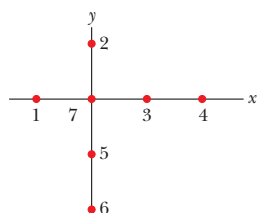
You will gradually discharge from the floor, but if instead of waiting, you immediately reach toward a faucet, a painful spark can suddenly appear as your fingers near the faucet. (b) In that spark, do electrons flow from you to the faucet or vice versa? (c) Just before the spark appears, do you induce positive or negative charge in the faucet? (d) If, instead, the cat reaches a paw toward the faucet, which way do electrons flow in the resulting spark? (e) If you stroke a cat with a bare hand on a dry day, you should take care not to bring your fingers near the cat's nose or you will hurt it with a spark. Considering that cat hair is an insulator, explain how the spark can appear.

**57** We know that the negative charge on the electron and the positive charge on the proton are equal. Suppose, however, that these magnitudes differ from each other by 0.00010%. With what force would two copper coins, placed 1.0 m apart, repel each other? Assume that each coin contains  $3 \times 10^{22}$  copper atoms. (*Hint:* A neutral copper atom contains 29 protons and 29 electrons.) What do you conclude?

**58** In Fig. 21-25, particle 1 of charge  $-80.0 \mu\text{C}$  and particle 2 of charge  $+40.0 \mu\text{C}$  are held at separation  $L = 20.0 \text{ cm}$  on an  $x$  axis. In unit-vector notation, what is the net electrostatic force on particle 3, of charge  $q_3 = 20.0 \mu\text{C}$ , if particle 3 is placed at (a)  $x = 40.0 \text{ cm}$  and (b)  $x = 80.0 \text{ cm}$ ? What should be the (c)  $x$  and (d)  $y$  coordinates of particle 3 if the net electrostatic force on it due to particles 1 and 2 is zero?

**59** What is the total charge in coulombs of 75.0 kg of electrons?

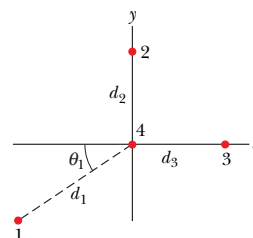
**60** In Fig. 21-42, six charged particles surround particle 7 at radial distances of either  $d = 1.0 \text{ cm}$  or  $2d$ , as drawn. The charges are  $q_1 = +2e$ ,  $q_2 = +4e$ ,  $q_3 = +e$ ,  $q_4 = +4e$ ,  $q_5 = +2e$ ,  $q_6 = +8e$ ,  $q_7 = +6e$ , with  $e = 1.60 \times 10^{-19} \text{ C}$ . What is the magnitude of the net electrostatic force on particle 7?



**Fig. 21-42** Problem 60.

**61** Three charged particles form a triangle: particle 1 with charge  $Q_1 = 80.0 \text{ nC}$  is at  $xy$  coordinates  $(0, 3.00 \text{ mm})$ , particle 2 with charge  $Q_2$  is at  $(0, -3.00 \text{ mm})$ , and particle 3 with charge  $q = 18.0 \text{ nC}$  is at  $(4.00 \text{ mm}, 0)$ . In unit-vector notation, what is the electrostatic force on particle 3 due to the other two particles if  $Q_2$  is equal to (a)  $80.0 \text{ nC}$  and (b)  $-80.0 \text{ nC}$ ?

**62 SSM** In Fig. 21-43, what are the (a) magnitude and (b) direction of the net electrostatic force on particle 4 due to the other three particles? All four particles are fixed in the  $xy$  plane, and  $q_1 = -3.20 \times 10^{-19} \text{ C}$ ,  $q_2 = +3.20 \times 10^{-19} \text{ C}$ ,  $q_3 = +6.40 \times 10^{-19} \text{ C}$ ,  $q_4 = +3.20 \times 10^{-19} \text{ C}$ ,  $\theta_1 = 35.0^\circ$ ,  $d_1 = 3.00 \text{ cm}$ , and  $d_2 = d_3 = 2.00 \text{ cm}$ .



**Fig. 21-43** Problem 62.

**63** Two point charges of  $30 \text{ nC}$  and  $-40 \text{ nC}$  are held fixed on an  $x$  axis, at the origin and at  $x = 72 \text{ cm}$ , respectively. A particle with a charge of  $42 \mu\text{C}$  is released from rest at  $x = 28 \text{ cm}$ . If the initial acceleration of the particle has a magnitude of  $100 \text{ km/s}^2$ , what is the particle's mass?

**64** Two small, positively charged spheres have a combined charge of  $5.0 \times 10^{-5} \text{ C}$ . If each sphere is repelled from the other by an electrostatic force of  $1.0 \text{ N}$  when the spheres are  $2.0 \text{ m}$  apart, what is the charge on the sphere with the smaller charge?

**65** The initial charges on the three identical metal spheres in Fig. 21-23 are the following: sphere  $A$ ,  $Q$ ; sphere  $B$ ,  $-Q/4$ ; and sphere  $C$ ,  $Q/2$ , where  $Q = 2.00 \times 10^{-14} \text{ C}$ . Spheres  $A$  and  $B$  are fixed in place, with a center-to-center separation of  $d = 1.20 \text{ m}$ , which is much larger than the spheres. Sphere  $C$  is touched first to sphere  $A$  and then to sphere  $B$  and is then removed. What then is the magnitude of the electrostatic force between spheres  $A$  and  $B$ ?

**66** An electron is in a vacuum near Earth's surface and located at  $y = 0$  on a vertical  $y$  axis. At what value of  $y$  should a second electron be placed such that its electrostatic force on the first electron balances the gravitational force on the first electron?

**67 SSM** In Fig. 21-25, particle 1 of charge  $-5.00q$  and particle 2 of charge  $+2.00q$  are held at separation  $L$  on an  $x$  axis. If particle 3 of unknown charge  $q_3$  is to be located such that the net electrostatic force on it from particles 1 and 2 is zero, what must be the (a)  $x$  and (b)  $y$  coordinates of particle 3?

**68** Two engineering students, John with a mass of  $90 \text{ kg}$  and Mary with a mass of  $45 \text{ kg}$ , are  $30 \text{ m}$  apart. Suppose each has a  $0.01\%$  imbalance in the amount of positive and negative charge, one student being positive and the other negative. Find the order of magnitude of the electrostatic force of attraction between them by replacing each student with a sphere of water having the same mass as the student.

**69** In the radioactive decay of Eq. 21-13, a  $^{238}\text{U}$  nucleus transforms to  $^{234}\text{Th}$  and an ejected  $^4\text{He}$ . (These are nuclei, not atoms, and thus electrons are not involved.) When the separation between  $^{234}\text{Th}$  and  $^4\text{He}$  is  $9.0 \times 10^{-15} \text{ m}$ , what are the magnitudes of (a) the electrostatic force between them and (b) the acceleration of the  $^4\text{He}$  particle?

**70** In Fig. 21-24, four particles form a square. The charges are  $q_1 = +Q$ ,  $q_2 = q_3 = q$ , and  $q_4 = -2.00Q$ . What is  $q/Q$  if the net electrostatic force on particle 1 is zero?