

Why deep networks work

① GPUs

② Big data → Available.
→ Data augmentation.

③ Activation functions (ReLU's)

④ Dropout method.

⑤ Pooling.

5	1	2	5	4	7
6	2	1	4	7	6
3	4	2	6	3	5
3	2	6	5	11	4
10	7	3	4	5	3
10	2	1	1	1	4

6	5	7
4	6	11
10	4	5

Max
pooling

3,5	3	6
...
.

Average
pooling.

Convolution + ReLU + Pooling.

1	6	-3	2	5
-6	-1	4	1	5
7	-5	7	3	1
3	2	-4	5	2
1	-5	2	-3	6

Input

Convolution:

$$\begin{bmatrix} 1 & 6 \\ -6 & -1 \end{bmatrix} * \begin{bmatrix} 2 & 1 \\ -1 & -2 \end{bmatrix} = 1 \cdot 2 + 6 \cdot 1 + (-6) \cdot (-1) + (-1) \cdot (-2) = 16$$

$$\begin{bmatrix} 6 & -3 \\ -1 & 4 \end{bmatrix} * \begin{bmatrix} 2 & 1 \\ -1 & -2 \end{bmatrix} = 12 - 3 + 1 - 8 = 2$$

2	1
-1	-2

Kernel

Result

16	2	-10	-2
-10	7	-4	2
2	3	11	6
17	1	1	-1

ReLU
→

16	2	0	0
0	0	0	2
2	3	11	6
17	1	1	0

↙
Max Pooling

16	2
17	11

(output)

↘
Average pooling

4,5	0,5
5,75	4,5

(output)

On MNIST database.

- ① 1 hidden layer of 100 neurons
(fully connected) (sigmoid a.f.) 97,8%.
- ② ① + 1 conv. layer + max pooling.
(sigmoid a.f.) 98,78%.
- ③ ② but with 2 conv. layers
+ pooling. 99,06%.
- ④ ③ + ReLU + R_2 regularisation 99,23%.

⑤ ④ + augmented (shifted) patterns 99,37%.

⑥ ⑤ + dropout + 2 layers in the classifier part 99,6%.

⑦ ⑥ + Ensembling. 99,7%.