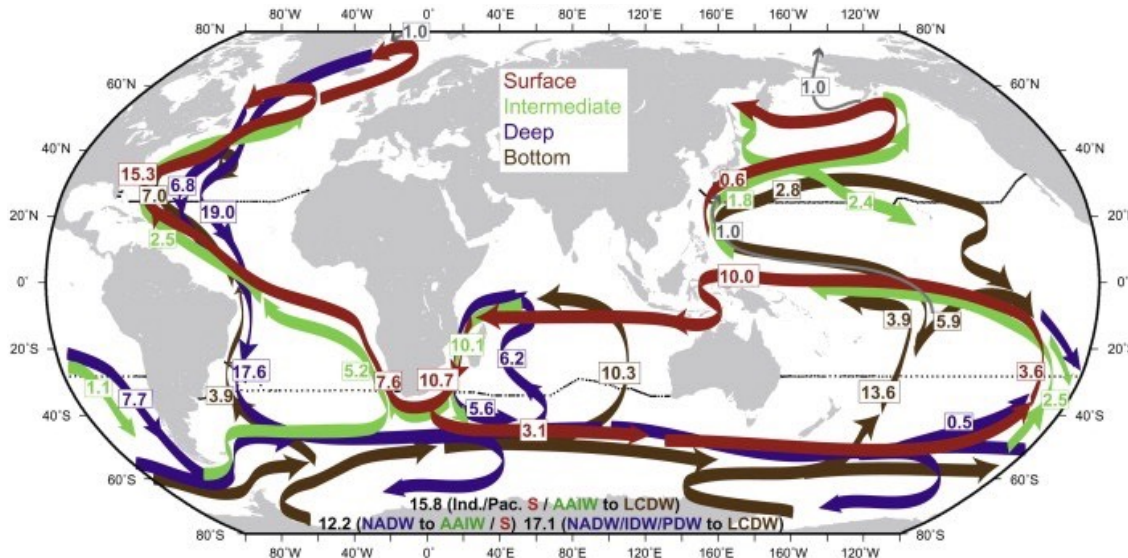
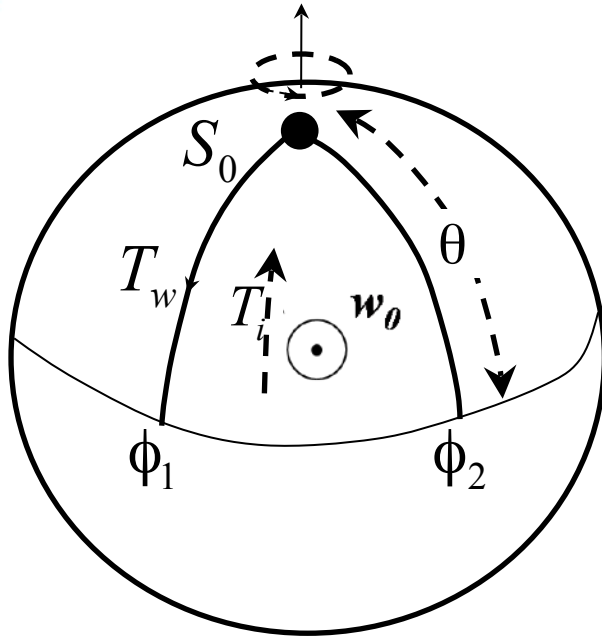


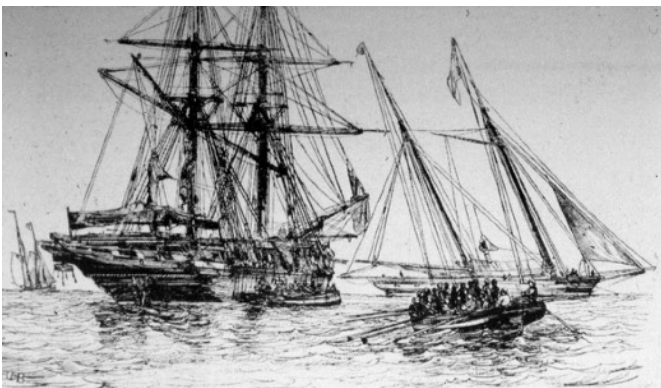


# 8. Deep convection and the thermohaline circulation

## 8. Η δημιουργία βαθιών νερών και η θερμοαλατική κυκλοφορία



- Βαθιές υδάτινες μάζες - Deep water masses
- Δημιουργία βαθιών νερών - Deep convection
- Θερμοαλατική κυκλοφορία - Thermohaline circulation



1721-1806

In 1751 **Henry Ellis**, the captain of a slave-trading ship, on his route from Africa to America, stopped at the tropical Atlantic and made deep water measurements (asked by the English Reverend Stephen Hales, using wooden bucket equipped with valves to capture water at selected depths). In his letter, he reported that

*“the cold increased regularly, in proportion to the depths, till it descended to 3900 feet: from whence the mercury in the thermometer came up at 53 degrees (\*11.67°C) ...*

*The warmth of the water upon the surface, and that of the air, was at that time by the thermometer 84 degrees (\*28.89°C).”*

...

*“This experiment, which seem’d at first by mere food for curiosity, became in the interim very useful to us. By its means we supplied our cold bath, and cooled our wines or water at pleasure; which is vastly agreeable to us in the burning climate”*

(Ellis, 1751)

in which I cannot perfectly agree with him, I think forces any body is better acquainted with the subject of electricity than himself.

XXXII. A Letter to the Rev. Dr. Hales, F.R.S. from Captain Henry Ellis, F.R.S. dated Jan. 7, 1750-51, at Cape Monte Africa, Ship Earl of Halifax.

S I R,  
I MAKE use of this opportunity of writing to you, lest from the vanity I have of having such a correspondent, that the desire of contributing to his satisfaction, who esteems it his greatest happiness to promote the interest of mankind. At yours and Lord Halifax's recommendation, I had your ventilator fixed on board of my ship, at Bristol. The following is a detail of the experiments, which I made to prove their utility.

1. I took a wax-candle, of eight to the pound, and drew it thro' a mold, to make it of one thickness from end to end; then weighed it exactly, and lighted it in the ship's hold; where I found it lasted 67 grains in 30 minutes; that place not being ventilated during 24 hours: but after six hours ventilation it lasted 94+1 grains in the same time.

2. I carried with me into the hold a plate of silver, well polished, and a lantern and candle, all blinded, except a round hole of about two inches diameter. I placed the plate at six feet distance from it; and with such

D d 2

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in most ships is very moist, in ours is quite dry. Our cargo arms, which are kept in upright chests, without wrappers, come out as bright as from a recent polish. Far is a ventilator from being inconvenient aboard of us; on the contrary, 'tis good exercise for our slaves, and a means of preserving our cargo and lives.

Upon the passage, I made several trials, with the bucket sea-gauge, in latitude 25°-13' north; longitude 25°-12' west. I charged it, and let it down to different depths, from 160 feet to 5346 feet; when I discovered, by a small thermometer of Fahrenheit's, made by Mr. Bird, which went down in it, that the cold increased regularly, in proportion to the depths, till it descended to 3900 feet: from whence the mercury in the thermometer came up at 53 degrees; and tho' I afterwards sink it to the depth of 5346 feet, that is a mile and 66 feet, it came up no lower. The warmth of the water upon the surface, and that of the air, was at that time by the thermometer 84 degrees. I doubt not but that the water was a degree or two colder, when it enter'd the bucket, at the greatest depth, but in coming up had acquired some warmth; for I found, that the water, which came up in the bucket, having stood 43 minutes in the air (the time of winding it up) the mercury rose above 5 degrees. When the air had render'd it equally warm with the water on the surface, I tried their weight, by weighing equal quantities very exactly, as also by the hydrometer, and found from great depths the heaviest, and consequently the saltiest water.

This

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depths, was a common household pail or bucket, with two heads in it; which heads had each a round hole in the middle, near four inches diameter, which were cover'd with valves which open'd upwards; and that they might both open and shut together, there was a small iron rod fixed to the upper part of the lower valve, and at the other end to the under part of the upper valve: so that, as the bucket descended with its sinking weight into the sea, both the valves open'd by the force of the water, which had by that means a free passage thro' the bucket. But when the bucket was drawn up, then both the valves were shut by the force of the water at the upper part of the bucket; by which means the bucket was brought up full of the lowest sea-water, to which it had descended.

When the bucket was drawn up, the hole at the bottom was stopp'd with a cork, to keep the water in, when the valves were open'd, to come at the mercurial thermometer, which being tied to an upright stick, could readily be unsifted, by pulling out a loose nail, which went into the upper end of stick, which was fasten'd at its lower end in the same manner.

But great care must be taken to make an observation of the degree the mercury stands at, before the lower part of the thermometer is taken out of the water; else it would immediately be alter'd by the different temperature of the air.

In order to keep the bucket in a right position, there are four cords fixed to it, which reach about three feet below it, to which the sinking weight is to be fixed.

Captain

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such obliquity, that the rays from the light should fall on its surface at an angle of 45 degrees. I then fixed a white paper screen, at the same distance from the plate, and under the same angle with the lantern, so that the reflected rays might fall upon it also. This being done, I observed, that the reflection from the plate distinctly was but 17° 30' with an un-ventilated hold; it being turned the colour of tarnish'd lead; whereas, when the air was replaced by 4 hours ventilation, it continued to reflect light, and retain its brightness 4 hours 47 minutes.

3. The ship's bell, whose diameter is 14 inches, I had brought into the hold, when ventilation had been omitted 13 hours. Having hung it under the lower deck, I took out the clapper, and having suspended it also by threads, which, with its own length, made 44 inches; the angle, which the rim of the bell made, with a line let fall perpendicular from the pin, on which the clapper hung, was equal to 34° 0'. I then held the clapper at the same angle, on the other side of the line, in order that the strokes at different times might be with the same force; when, letting it go, it struck the bell. In its return I catch'd it, and counting the vibrations, I heard them distinctly but three times; whereas, when the hold was well ventilated, it vibrated five times; but its vibrations were not so quick in the latter, as in the former case. I took all possible precautions, that these experiments might be fairly tried, to prevent deception; but always found them to produce the same effects.

We are at present very healthy, tho' our number is 130, not one being sick aboard. Our hold, which

in

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This experiment, which seem'd at first but mere food for curiosity, became in the interim very useful to us. By its means we supplied our cold bath, and cooled our wines or water at pleasure; which is vastly agreeable to us in this burning climate.

I intend, in our passage to the West Indies, to find a mile deeper than I have done, having a sufficient quantity of line. But I cannot attempt my method to find the depth of the sea, for want of apparatus. My business at present affords me very little time for speculation. However, I cannot omit observing to you a phenomenon, which I saw last night, and never before, that I remember; and that was the two arches of the sea, with their colours distinct, by moon-light. Having already presumed much on your patience, and my inclination,

I am, &c.

Hen. Ellis.

A Letter to the President, from Stephen Hales, D. D. & F. R. S.

S I R, Tedington, June 8, 1751.

Read June 13, 1751. I HAVE here inclosed, at his desire, a copy of a letter from Captain Ellis, who published an account of his voyage to Hudson's Bay.

The bucket sea-gauge, which he mentions, and which I provided for him, to find the different degrees of coolness and saltness of the sea, at different depths,

3

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Captain Robinson, who is lately arrived from India, says, he found so much benefit by ventilators, that he will never go a voyage without them; and that he lost but two men in two years.

There are many other instances of the benefit of ventilators in ships, not only to the health and lives, but also to the provisions, &c.

I am, Sir, with great respect,

Your obliged humble servant,

Stephen Hales.

XXXIII. Observations on the Roman Colonies and Stations in Cheshire and Lancashire, by Thomas Percival Esq; communicated by Hugh Lord Willoughby of Parham, F. R. S.

Read June 13, 1751. IN the second iter of Antonine's Itinerary, we find, after several other stations mentioned Eboracum

Calcaria M. P. IX. Camulodunum M. P. XX. Tho' with various names. Mamucium M. P. XXVIII. readings of the Condate M. P. XXVIII.

Deven M. P. XII.

It is agreed, that Deven is Chester, and that Mamucium or Manucium or Mancunium, is Manchester, by the common consent of all antiquarians. But where Con-

date





1753-1814

Based on Ellis's temperature profile, **Count Rumford** (Sir Benjamin Thompson), an American-born British scientist, deduced a scheme of the overturning circulation. In 1800, he wrote:

*"It appears to me to be extremely difficult, if not quite impossible, to account for this degree of cold at the bottom of the sea in the torrid zone, on any other sup- position than that of cold currents from the poles."*

Rumford further reasoned that this cold current at depth

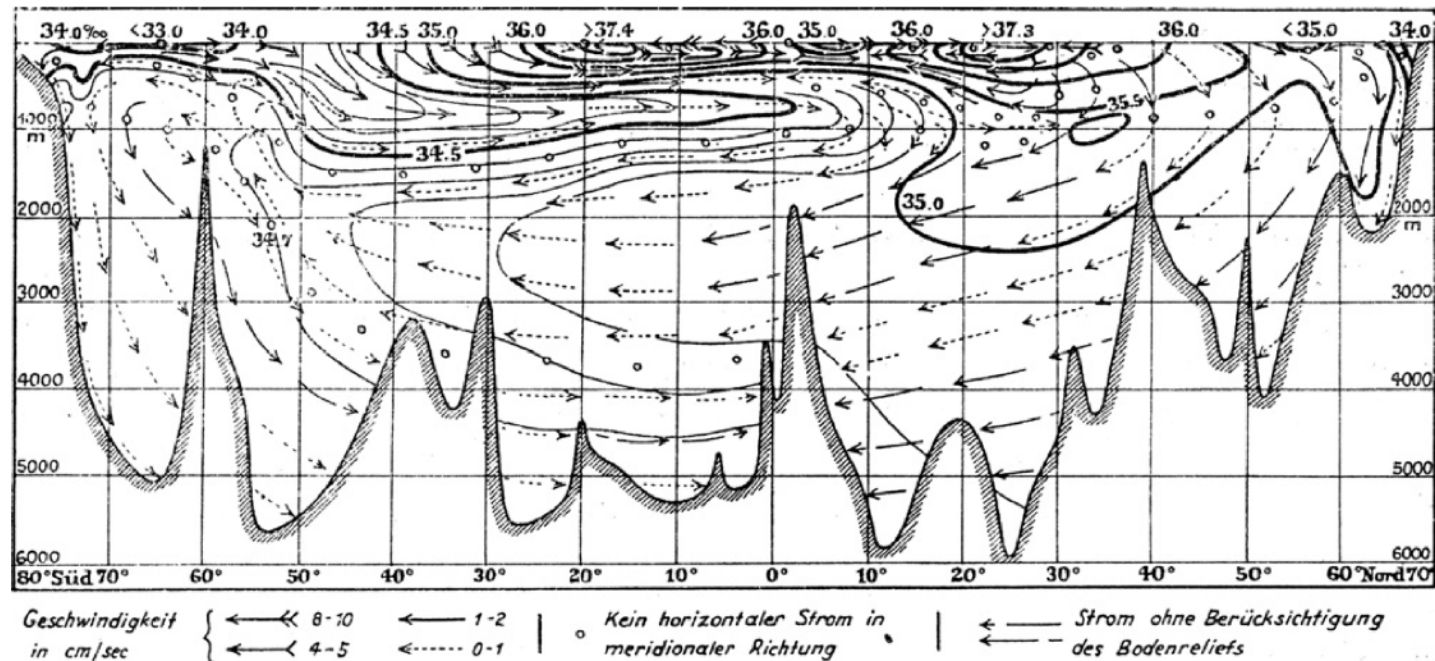
*"must necessarily produce a current at the surface in an opposite direction"*

(Rumford, 1800).

Measurements along 20°W during the German Atlantic **Meteor Expeditions** from 1925–1927, captured plumes of saline waters from the surface waters of the northern North Atlantic and relatively fresh waters of Antarctic origin (Merz, 1925).



METEOR



Rumford, B., Count of. 1800. Essay VII, The propagation of heat in fluids. Pp. 197–386 in Essays, Political, Economical, and Philosophical, A New Edition 2. London.

Merz, A. 1925. Die Deutsche Atlantische Expedition auf dem Vermessungs- und Forschungsschi "Meteor." Bericht. Sitzungsberichte der Preussischen Akademie der Wissenschaften, Physikalische-Mathematische Klasse:562–586.



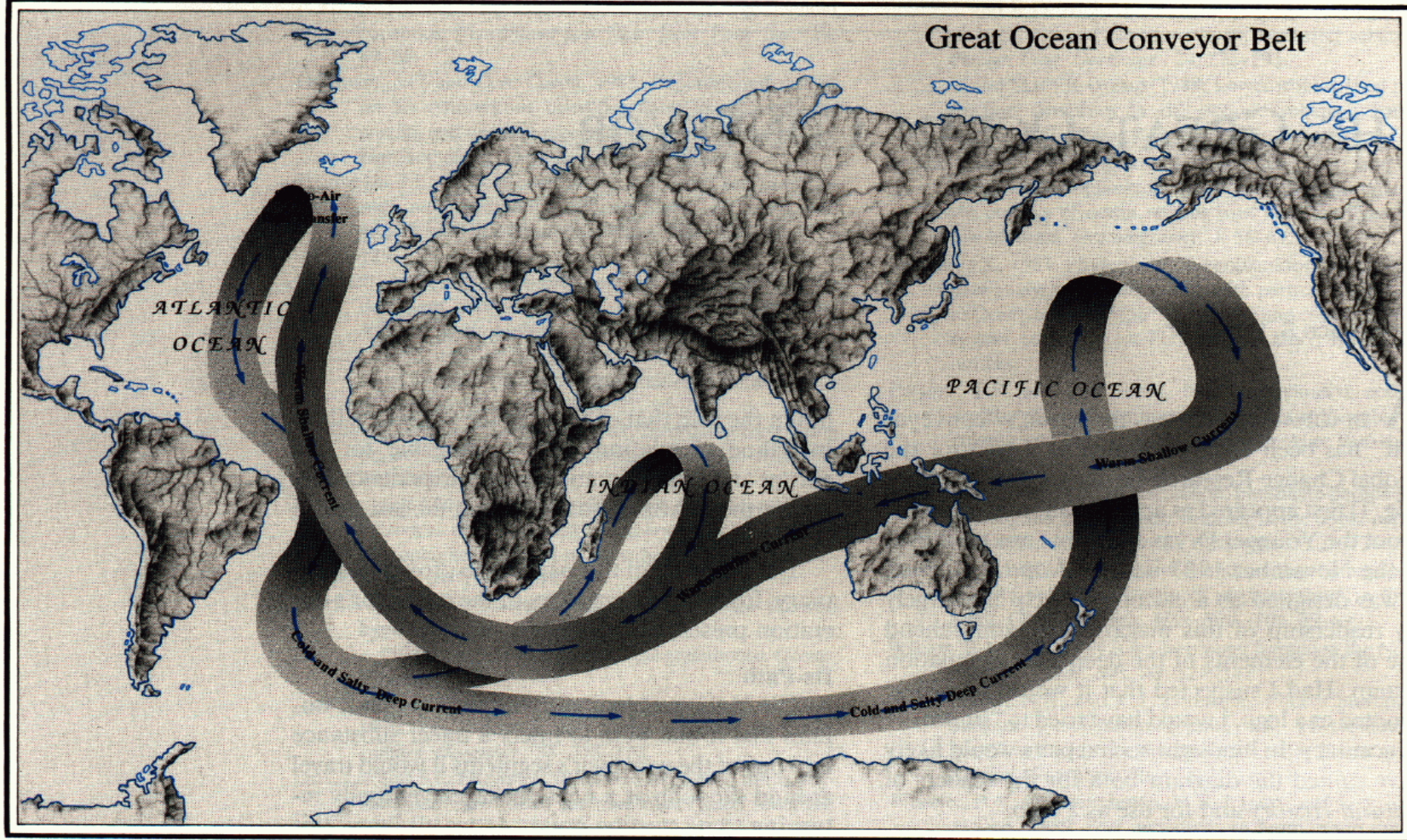
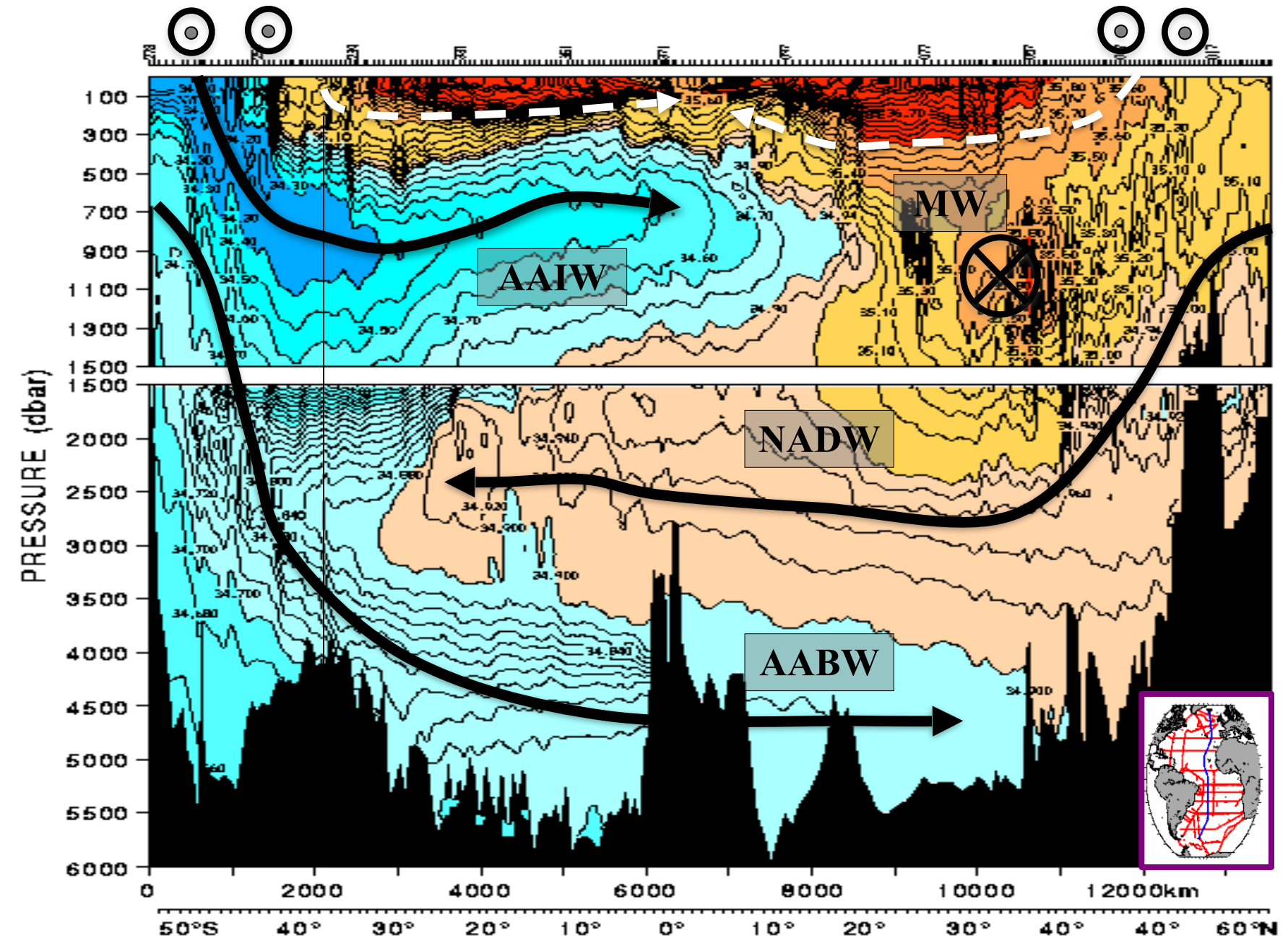


Fig. 1: The great ocean conveyor logo (Broecker, 1987). (Illustration by Joe Le Monnier, *Natural History Magazine*.)

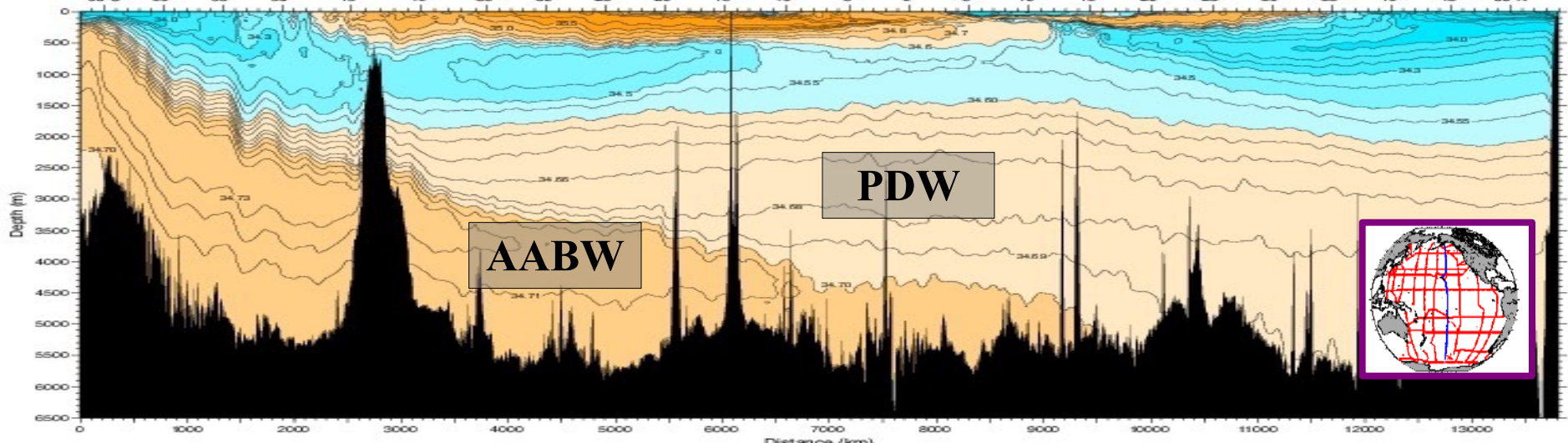
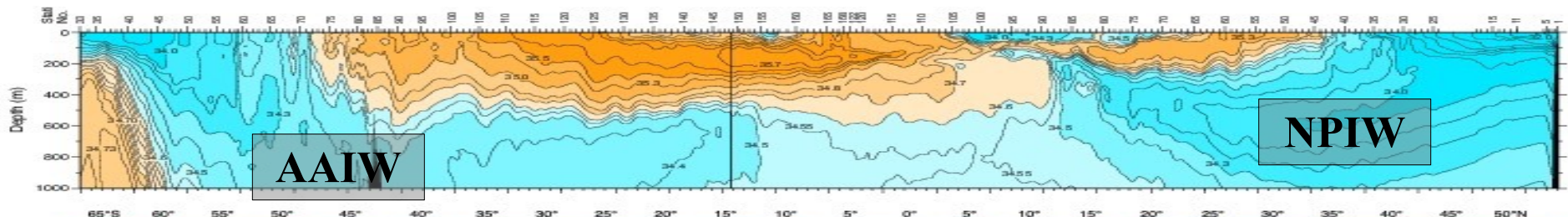
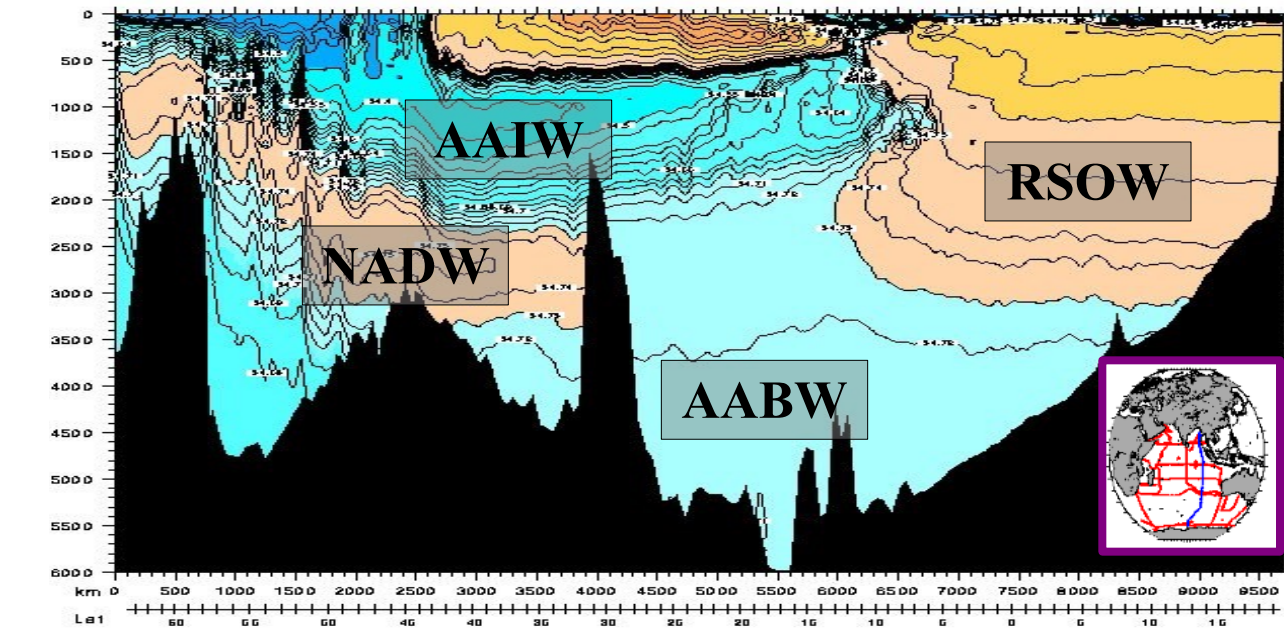


# Atlantic Main Water Masses (on salinity section)



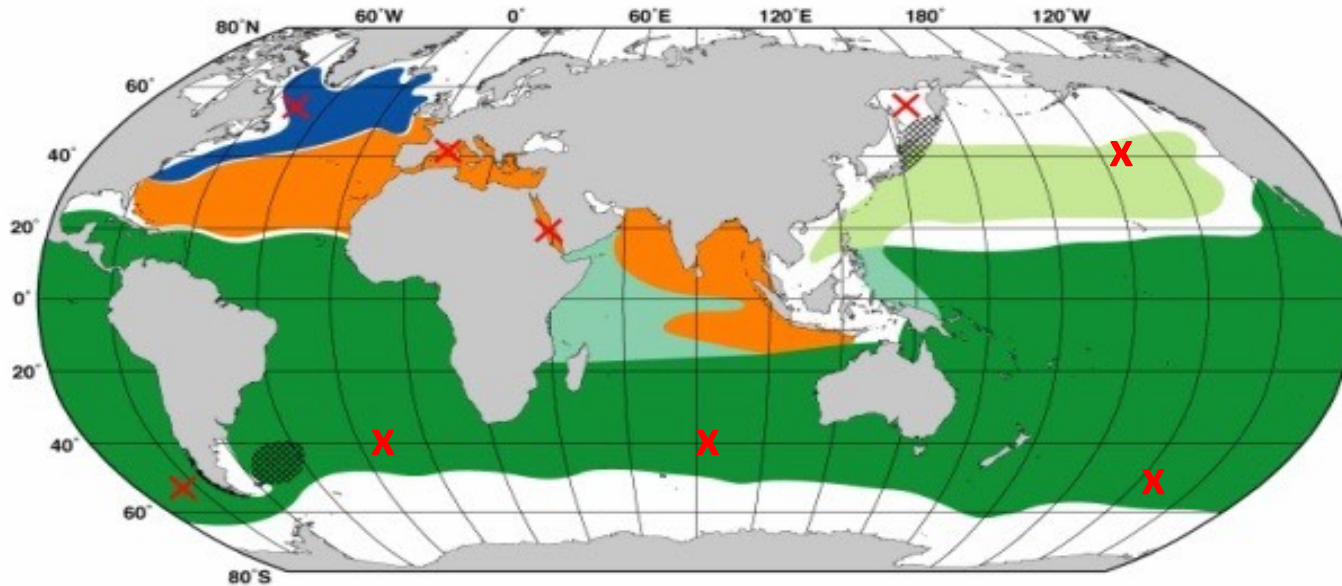


# Indian and Pacific Main Water Masses



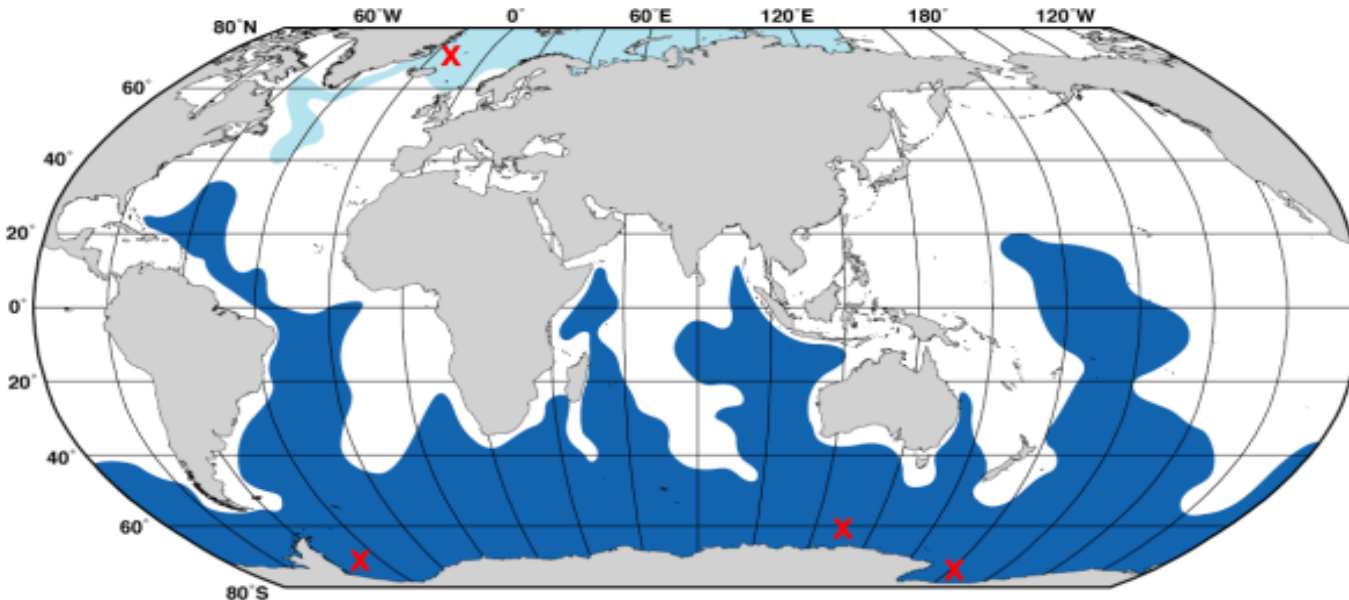


# The Water mass formation processes



## CONDITIONS

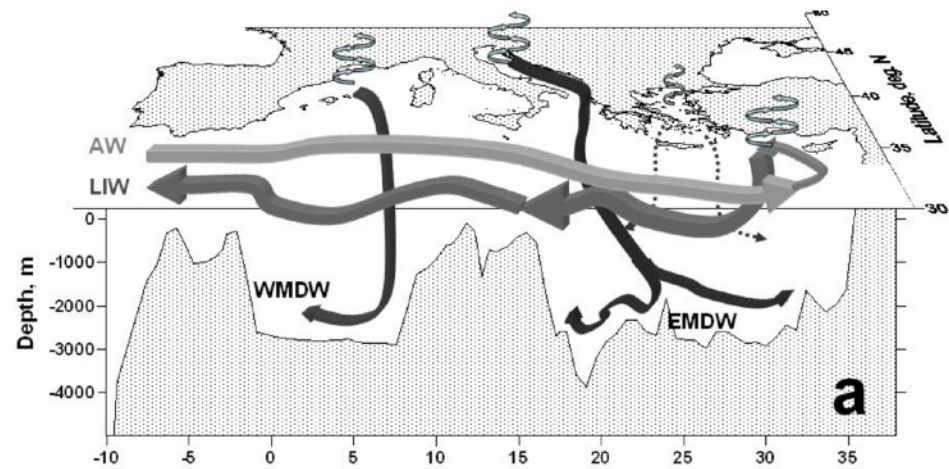
1. Intense heat and freshwater losses
2. Relatively weak stratification
3. Trapping



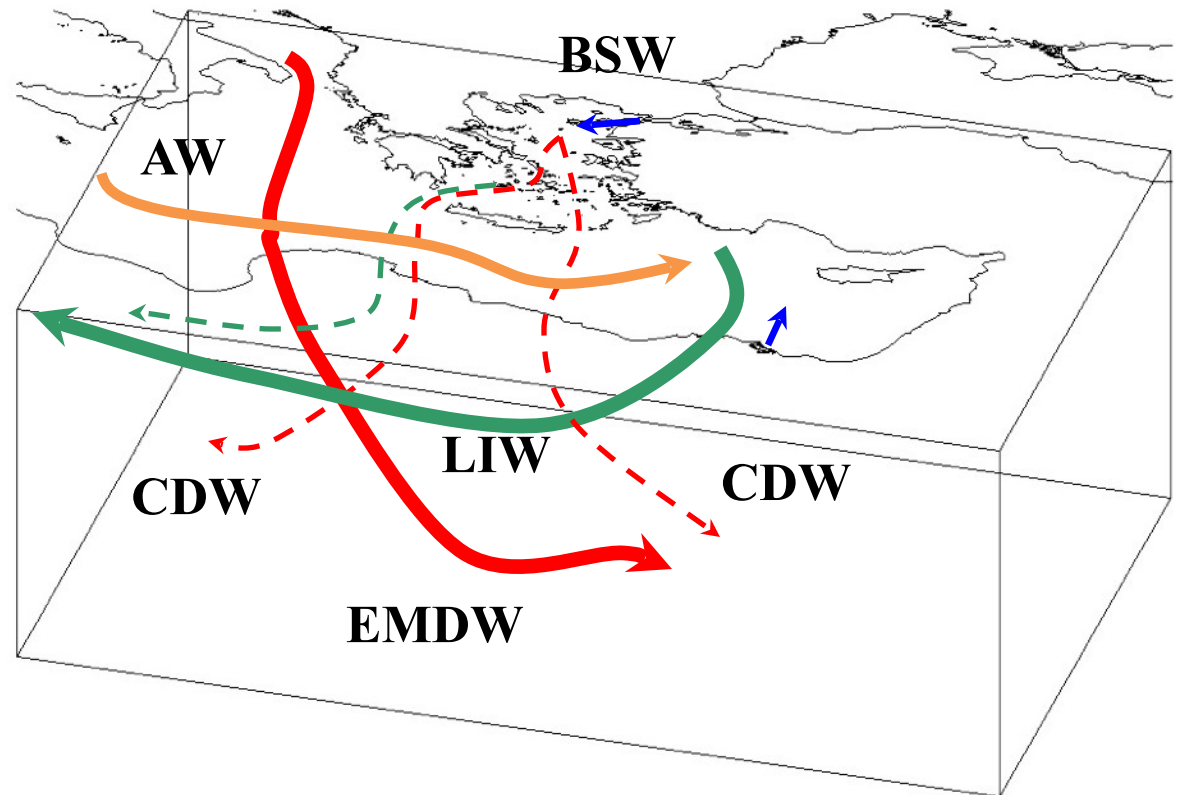
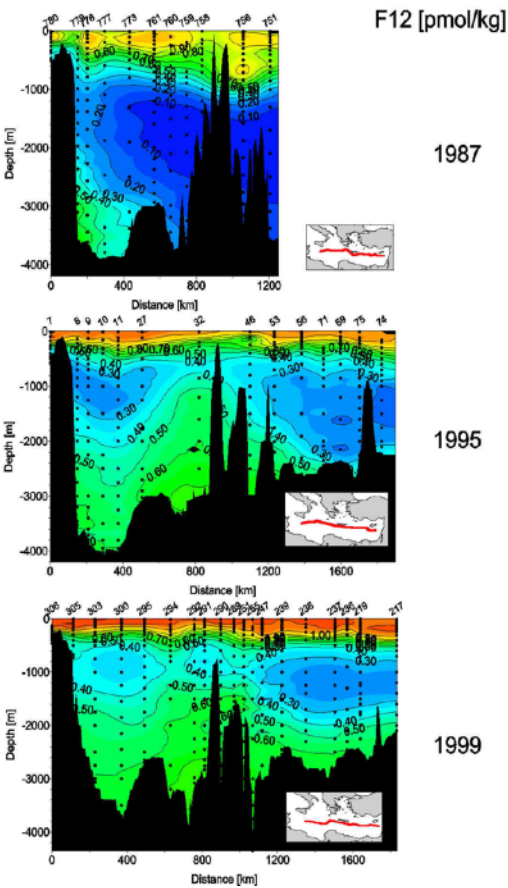
## AREAS

1. Arctic regions
2. Semi-enclosed seas
3. Continental shelf
4. Cyclonic features

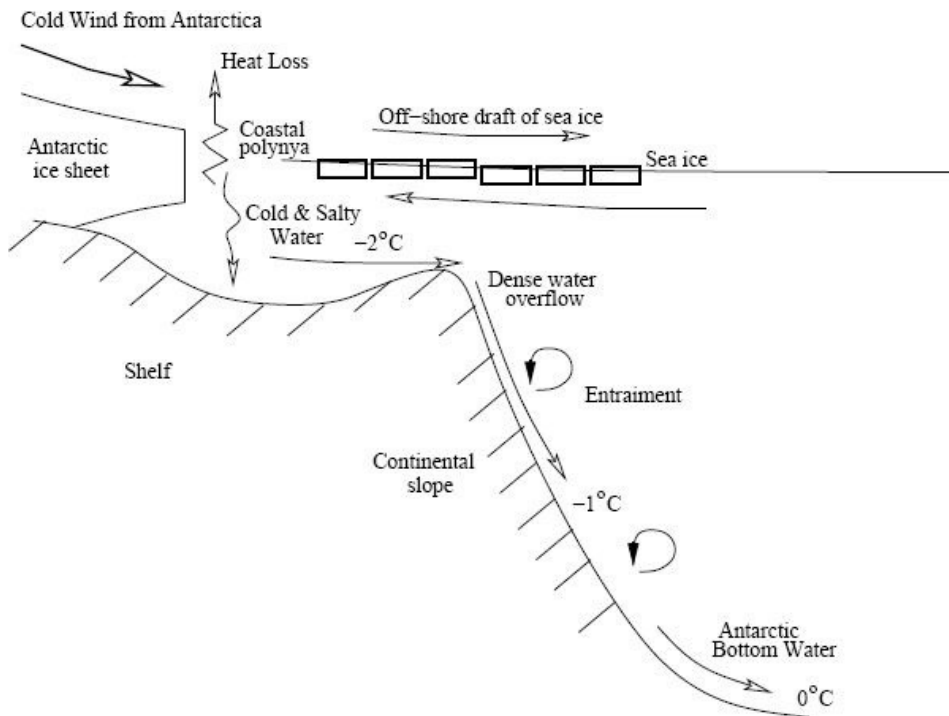
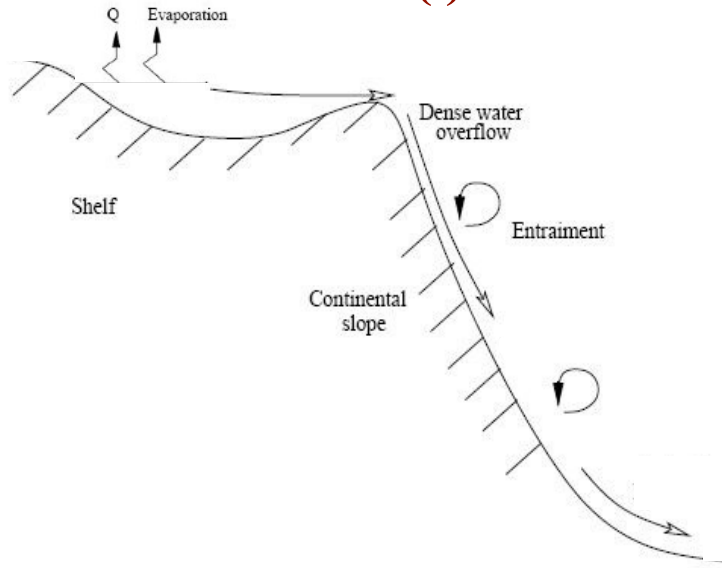




## The Mediterranean Sea water masses



## (i) Shelf convection



## Shelf water mass formation

- Strong heat loss and/or evaporative rates over the relatively shallow water column on the continental shelf can lead to formation of very dense waters.
- Entrainment on the continental slope changes dramatically the new water mass temperature and salinity properties and gives the water mass its final characteristics.

## Arctic/Antarctic shelf water mass formation

- Winds blowing offshore open the ice sheet, forming a polynya.
- Salt addition to the water column, related to ice formation increases the water salinity.
- Large heat fluxes ( $\sim 1000 \text{ W m}^{-2}$ ) from the exposed ocean drives bottom water formation.
- Entrainment changes the water mass properties.



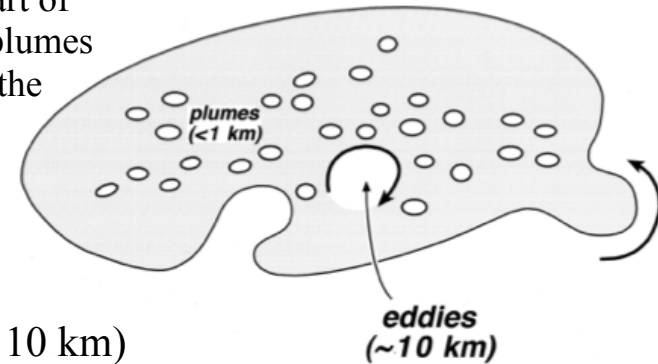
## (ii) Open ocean convection

### 1. Pre-conditioning (order of 100 km)

During preconditioning the gyre-scale cyclonic circulation with its “doming” isopycnals, brings weakly stratified waters of the interior close to the surface. Buoyancy loss is preconditioning the “trapped” water.

### 2. Deep convection (order of 1 km)

Subsequent cooling events may then initiate deep convection in which a substantial part of the fluid column overturns in numerous plumes that distribute the dense surface water in the vertical.



### 3. Lateral exchange (order of 10 km)

With the cessation of strong forcing, or if the cooling continues for many days, the predominantly vertical heat transfer on the convective scale gives way to horizontal transfer associated with eddying on geostrophic scales as the mixed patch laterally exchanges fluid with its surroundings.

### 4. Re-stratification

The mixed fluid disperses under the influence of gravity and rotation, spreading out at its neutrally buoyant level and leading, on a timescale of weeks to months, to the disintegration of the mixed patch and reoccupation of the convection site by the stratified fluid of the periphery.

Χειμώνας

Καλοκαίρι

Lateral  
exchange -  
Restratification  
(weeks)

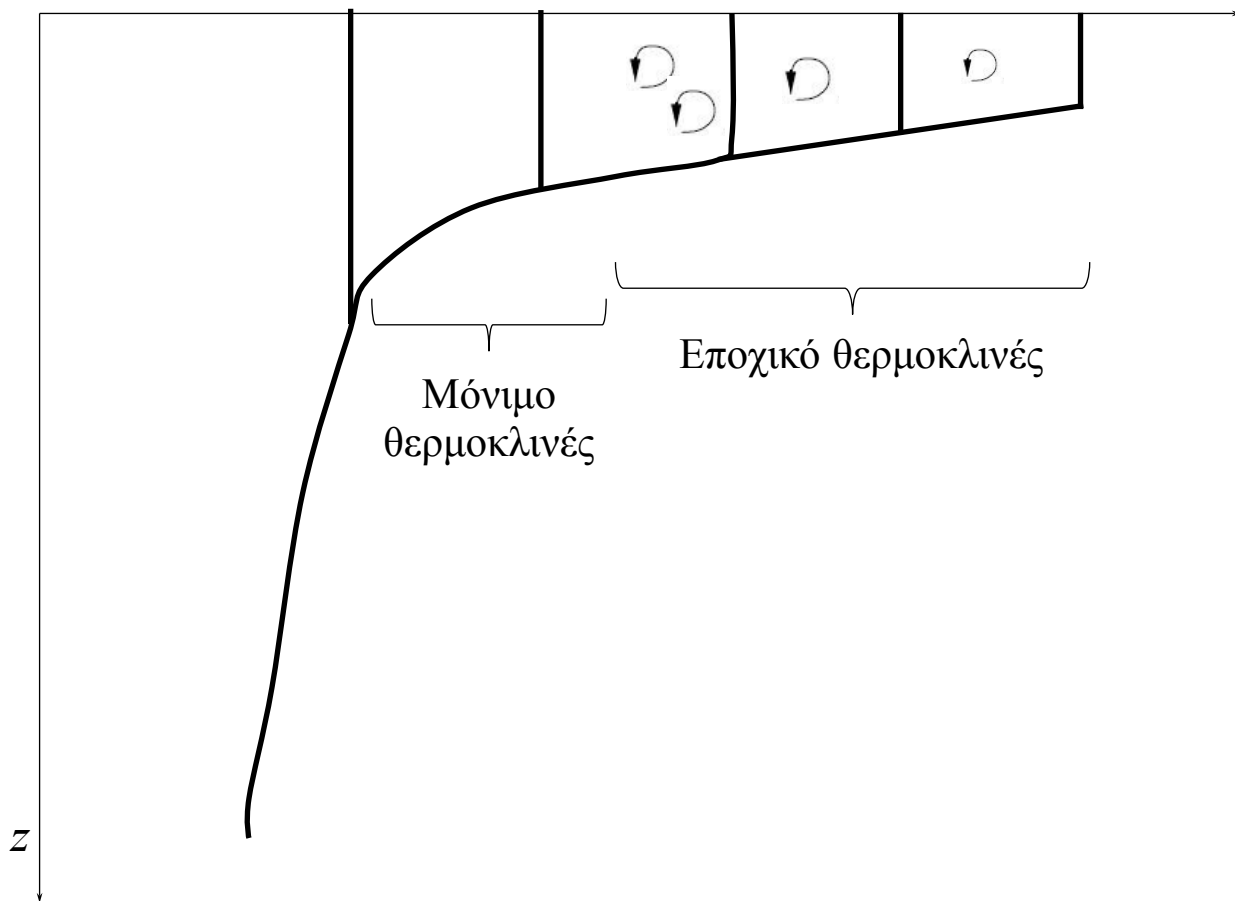
Forcing:

$$Q(\dot{H}, E), \vec{\tau}$$

Deep  
convection  
(weeks)

Preconditioning  
(months)

$T$

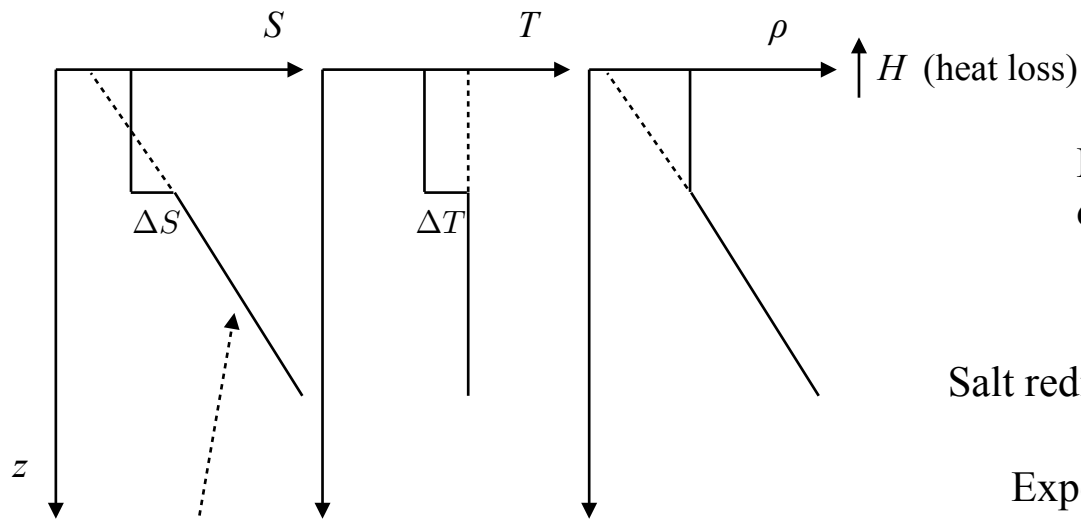


**Mixed-Layer**  
(στρώμα ανάμιξης)

**Thermocline**  
(θερμοκλινές)

**Deep waters**





**Turner, 1973**

Heat/salt balances in a uniform mixed layer of depth  $d$  at time  $t$

$$\text{Heat loss} \longrightarrow Ht = -\rho c_p d \Delta T \quad (1)$$

$$\text{Salt redistribution} \longrightarrow g\beta\Delta S = \frac{1}{2}dN_s^2 \quad (2)$$

Experimental observations show that:

$$\alpha\Delta T = -\beta\Delta S \quad (3)$$

Buoyancy flux (due to heat flux) can be written as:  $B = \frac{g\alpha H}{\rho c_p} \quad (4)$

Combining (1),(2),(3) and (4):  $(1) \Rightarrow d = -\frac{Ht}{\rho c_p \Delta T} \stackrel{(3)}{=} -\frac{Ht}{\rho c_p \left( \frac{-\beta\Delta S}{\alpha} \right)} =$

$$= \frac{Ht\alpha}{\rho c_p \beta \Delta S} \stackrel{(2)}{=} \frac{Ht 2g\alpha}{\rho c_p d N_s^2} = \frac{2t}{d N_s^2} \left( \frac{g\alpha H}{\rho c_p} \right) \Rightarrow d^2 = \frac{2Bt}{N_s^2}$$

$= B \quad (4)$

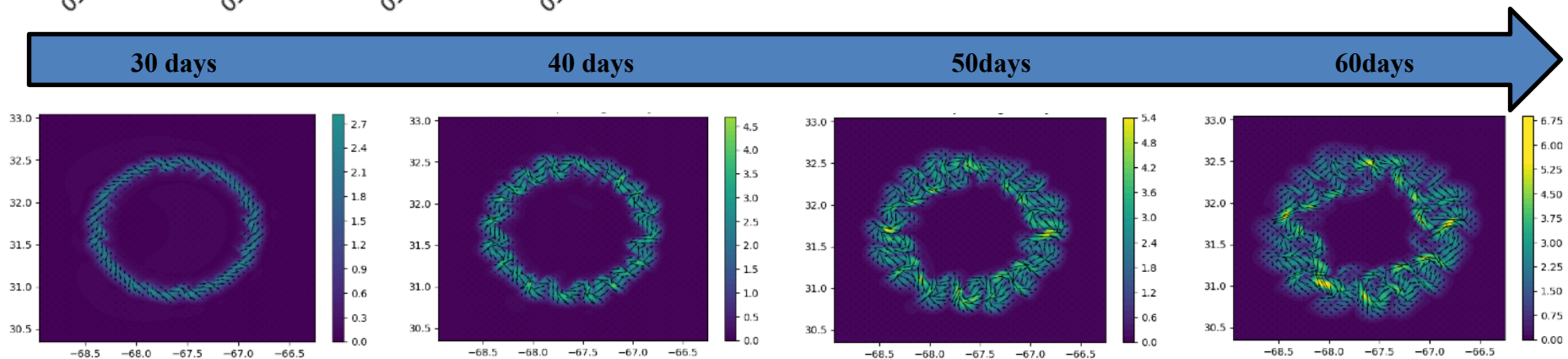
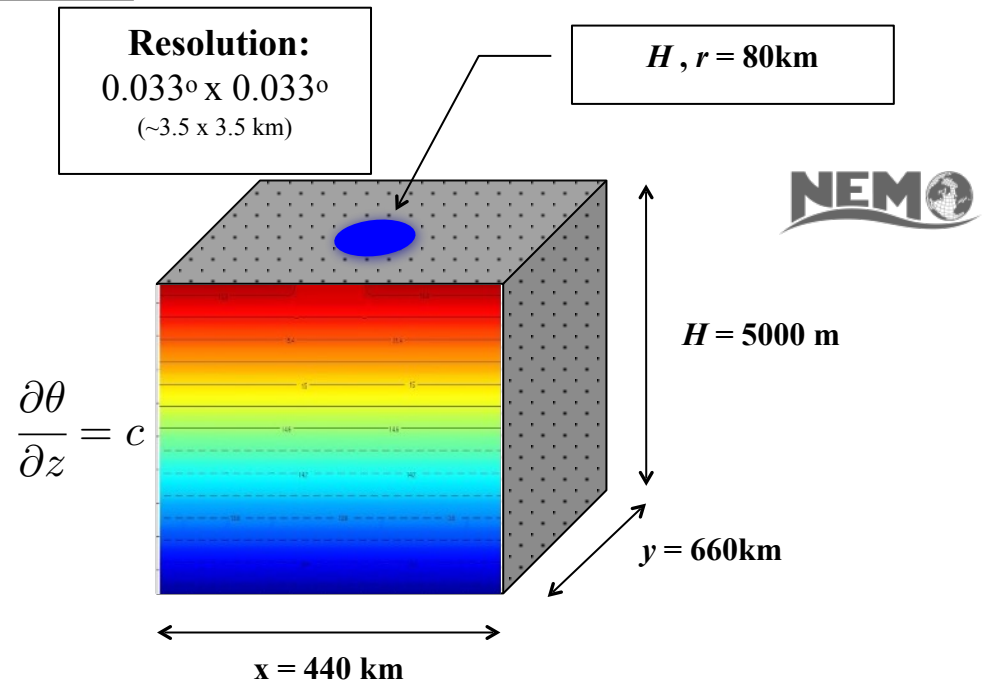
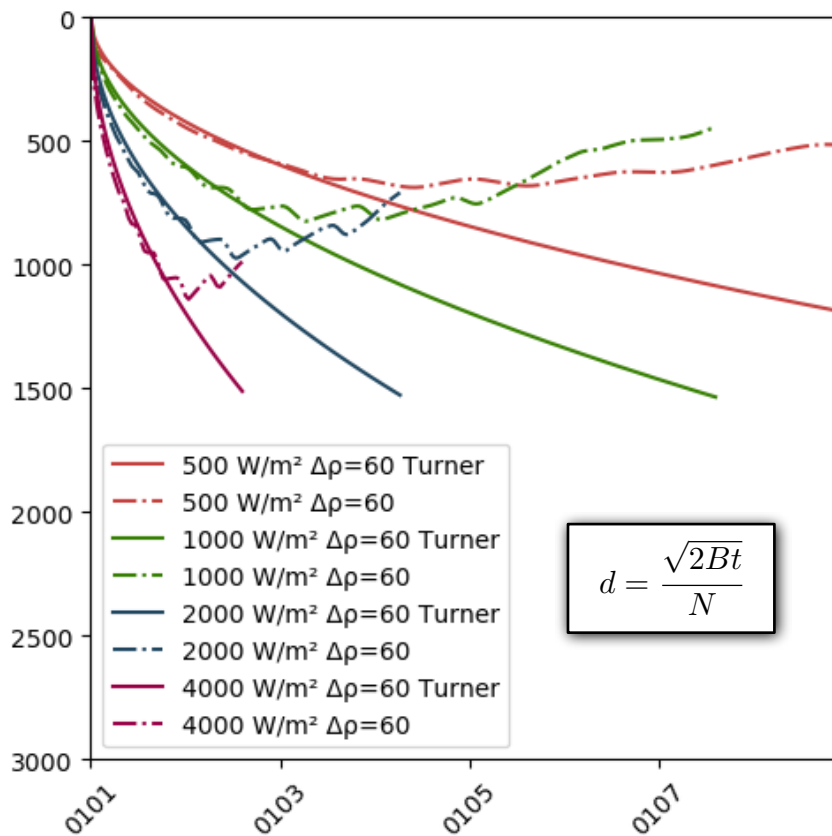
$$\alpha \equiv -\frac{1}{\rho} \frac{\partial \rho}{\partial T} \quad \text{Thermal expansion coefficient}$$

$$\beta \equiv \frac{1}{\rho} \frac{\partial \rho}{\partial S} \quad \text{Haline contraction coefficient}$$

$$c_p \quad \text{Heat capacity}$$

$$\Rightarrow d = \frac{\sqrt{2Bt}}{N_s}$$

# An example: Compare 1-D approach with 3-D results





# Vorticity (στροβιλισμός) reduced gravity form

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -g' \frac{\partial h}{\partial x} + f v \quad (1)$$

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \quad (3)$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -g' \frac{\partial h}{\partial y} - f u \quad (2)$$

$$\frac{\partial}{\partial x} (2) - \frac{\partial}{\partial y} (1)$$

$$\begin{aligned} & \frac{\partial}{\partial t} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) + \frac{\partial u}{\partial x} \frac{\partial v}{\partial x} + u \frac{\partial^2 v}{\partial x \partial x} + \frac{\partial v}{\partial x} \frac{\partial v}{\partial y} + v \frac{\partial^2 v}{\partial x \partial y} - \\ & - \frac{\partial u}{\partial y} \frac{\partial u}{\partial x} - u \frac{\partial^2 u}{\partial y \partial x} - \frac{\partial v}{\partial y} \frac{\partial u}{\partial y} - v \frac{\partial^2 u}{\partial y \partial y} = \\ & = -g' \frac{\partial^2 h}{\partial x \partial y} + g' \frac{\partial^2 h}{\partial x \partial y} - f \frac{\partial u}{\partial x} - u \frac{\partial f}{\partial x} - f \frac{\partial v}{\partial y} - v \frac{\partial f}{\partial y} \end{aligned}$$

$(u, v \not\propto z)$   
 $f \not\propto x$

$$= \frac{df}{dt}$$

$$\frac{\partial}{\partial t} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) + u \frac{\partial}{\partial x} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) + v \frac{\partial}{\partial y} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) +$$

$$+ \frac{\partial u}{\partial x} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) + \frac{\partial v}{\partial y} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) =$$

$$= -f \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) - \frac{df}{dt}$$

**planetary vorticity**

$$= \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right)$$

$$= \frac{d}{dt} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right)$$

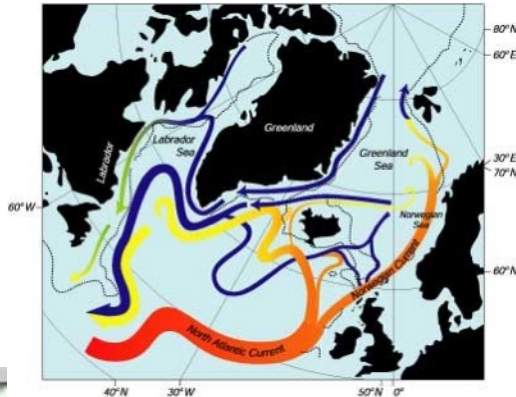
Defining **relative vorticity**:  $\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = \zeta$  (ocean velocity curl)

$$\frac{d\zeta}{dt} + \zeta \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = -f \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) - \frac{df}{dt}$$

$$\frac{d}{dt} (f + \zeta) = - (f + \zeta) \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)$$



# The pathways of deep waters in the abyssal ocean



For large scale motions  $R_o \ll 1$

Starting from

$$\frac{d}{dt}(f + \zeta) = -(f + \zeta) \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)$$

and using the continuity equation  $\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = -\frac{\partial w}{\partial z}$

$$\frac{d}{dt}(f + \zeta) = -(f + \zeta) \left( -\frac{\partial w}{\partial z} \right)$$

Scaling

$$\left. \begin{aligned} \zeta &= \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = O\left(\frac{U}{L}\right) \\ f &= O(f_0) \end{aligned} \right\} \frac{\zeta}{f} = O\left(\frac{U}{f_0 l}\right) = O(R_o) \ll 1$$

Ignoring  $\zeta$  and

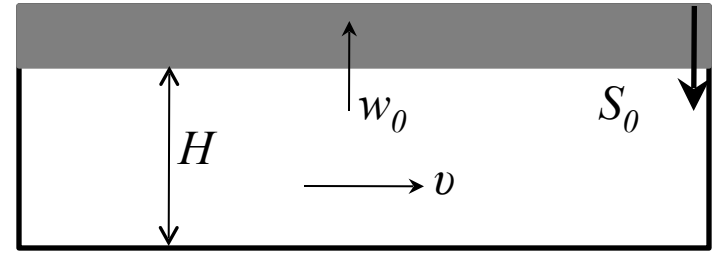
$$\frac{df}{dt} = \frac{\partial f}{\partial t} + u \frac{\partial f}{\partial x} + v \frac{\partial f}{\partial y} + w \frac{\partial f}{\partial z} = \beta v$$

$$\Rightarrow \beta v = f \left( \frac{\partial w}{\partial z} \right)$$

# Abyssal Circulation (Stommel-Arons Theory)

Potential vorticity  
conservation:

$$\beta v = f \frac{\partial w}{\partial z}$$



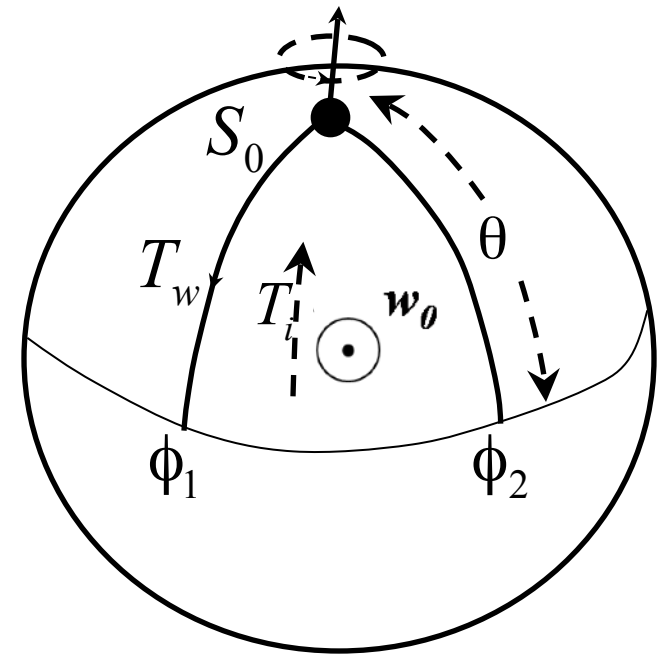
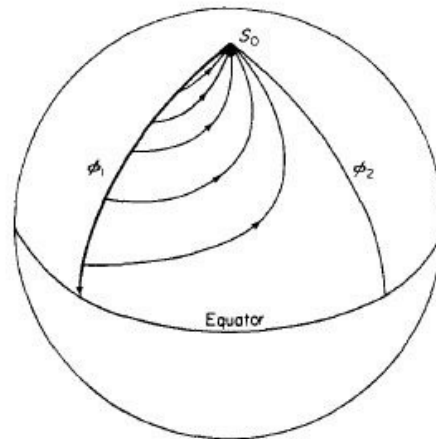
$$\frac{2\Omega \cos \theta}{R_{earth}} v = 2\Omega \sin \theta \frac{\partial w}{\partial z}$$

$$\frac{\partial w}{\partial z} \approx \frac{w_{top} - w_{bot}}{H} = \frac{w_0}{H}$$

$$v = \frac{w_0 R}{H} \tan \theta$$

Continuity

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$$





# “Half Ocean solution”

Conservation of volume:

$$S_0 + T_i = T_u + T_w$$

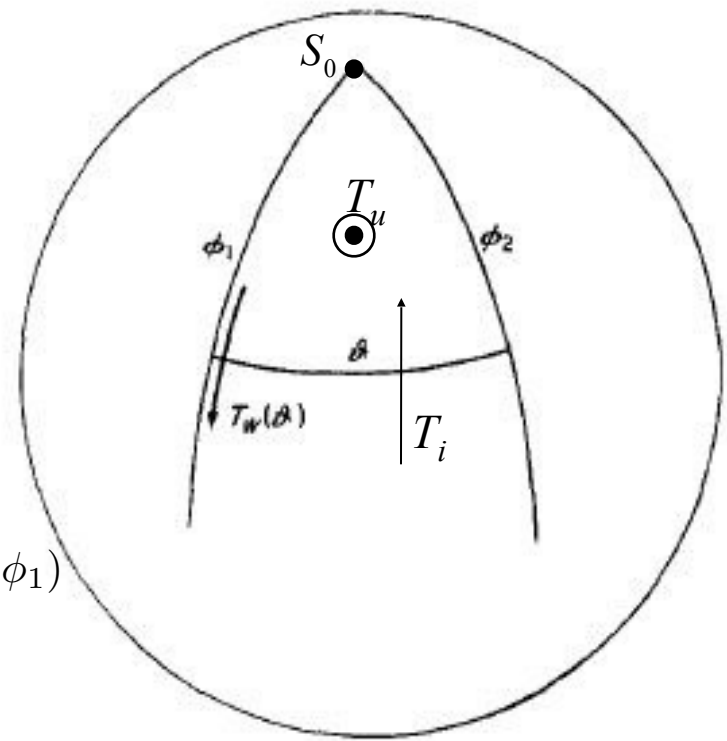
$$T_i = \int_{\phi_1}^{\phi_2} H v R \cos \theta \, d\phi = w_0 R^2 \sin \theta (\phi_2 - \phi_1)$$

$$T_u = \int^{\pi/2} \theta \int_{\phi_1}^{\phi_2} w_0 R^2 \cos \theta \, d\phi \, d\theta = w_0 R^2 (1 - \sin \theta) (\phi_2 - \phi_1)$$

$$\text{and } T_u(\text{domain}) = w_0 R^2 (\phi_2 - \phi_1) = S_0$$

$$\begin{aligned} T_w &= S_0 + w_0 R^2 \sin \theta (\phi_2 - \phi_1) - w_0 R^2 (1 - \sin \theta) (\phi_2 - \phi_1) = \\ &= S_0 + \underbrace{w_0 R^2 (\phi_2 - \phi_1)}_{S_0} (\sin \theta - 1 + \sin \theta) \end{aligned}$$

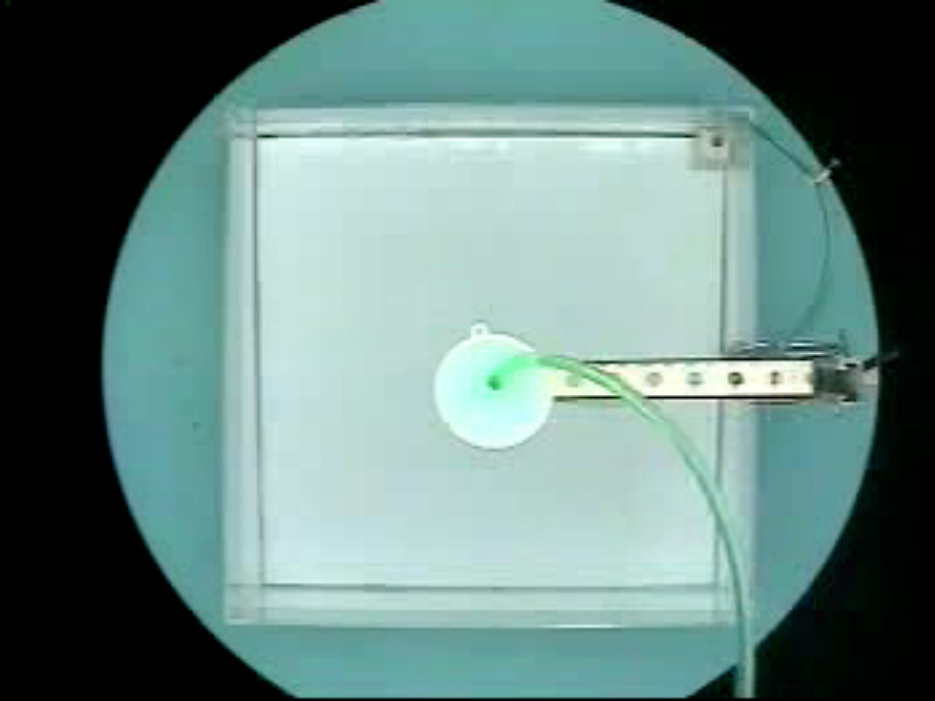
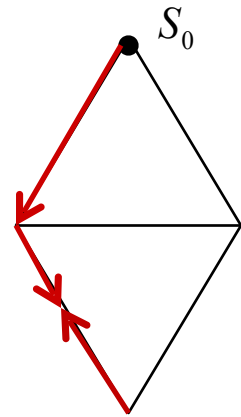
$$T_w = 2S_0 \sin \theta$$



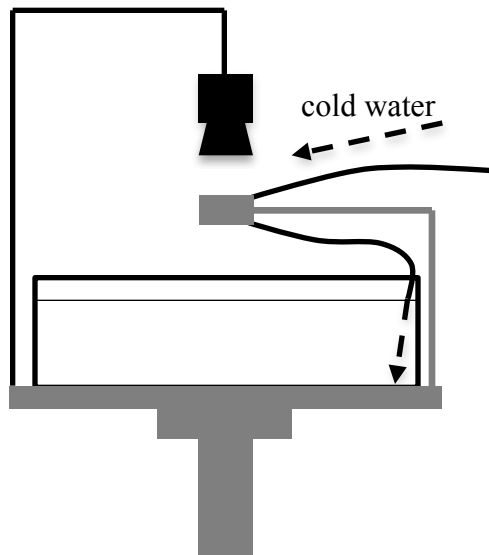
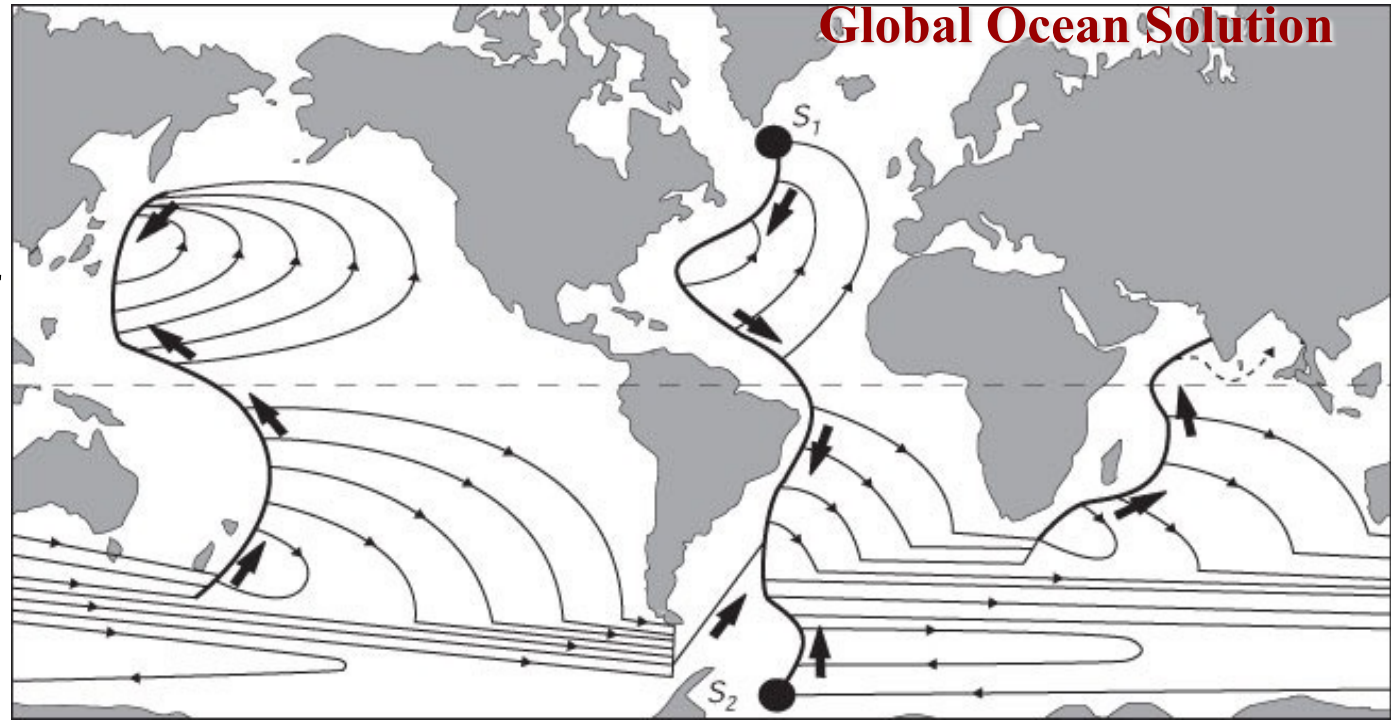
## “Whole” basin solution

$$S_0 = 2w_0 R^2 (\phi_2 - \phi_1)$$

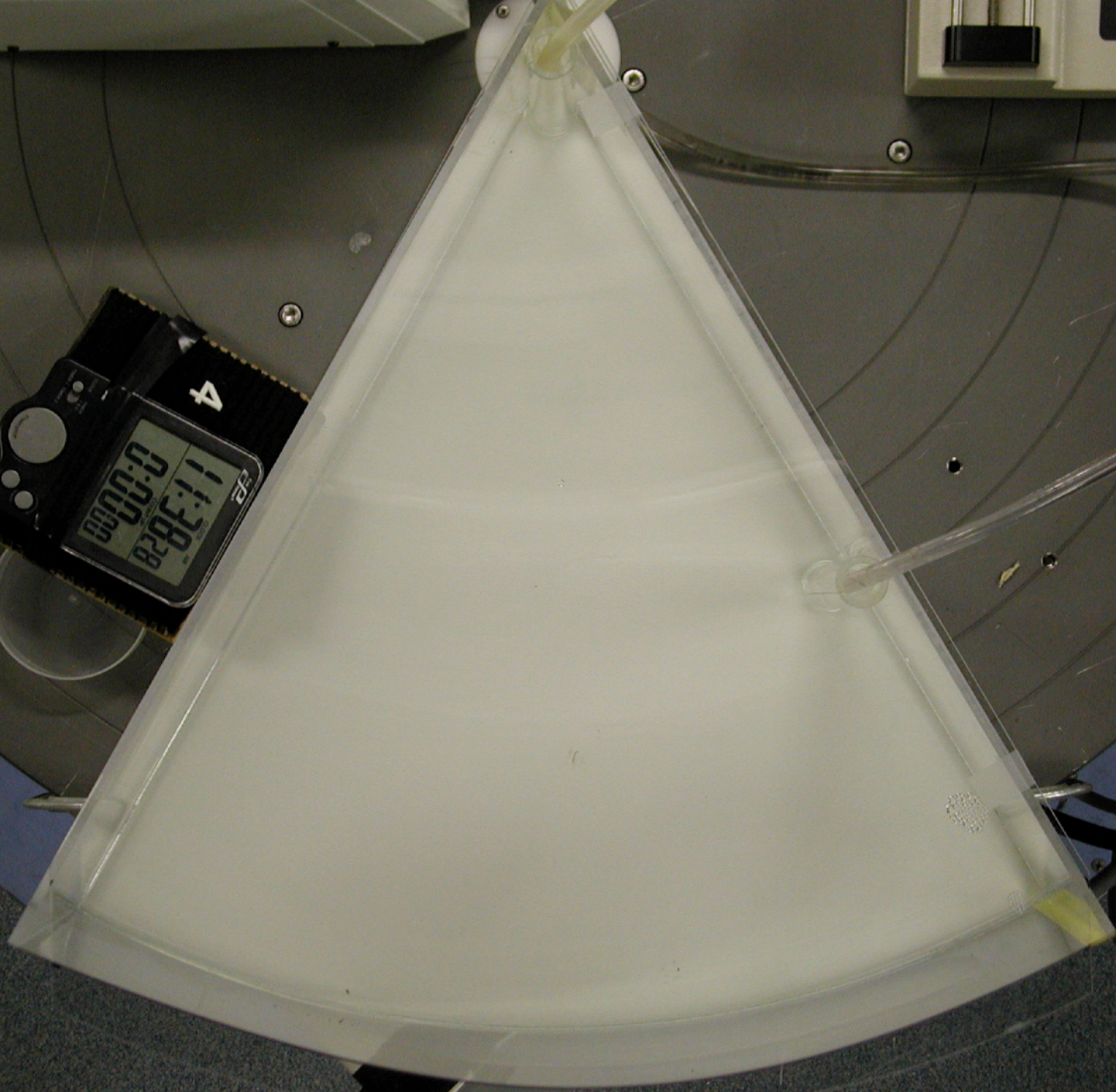
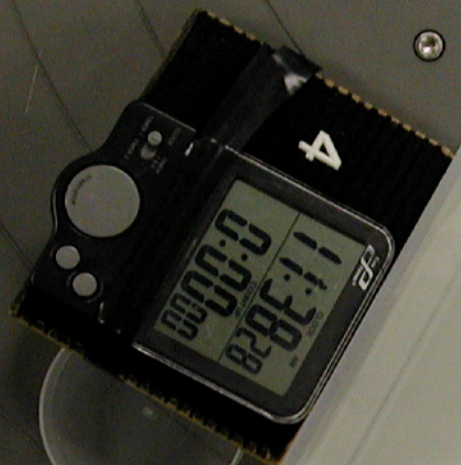
$$T_w = S_0 \left( \frac{1}{2} + \sin \theta \right)$$



## Global Ocean Solution



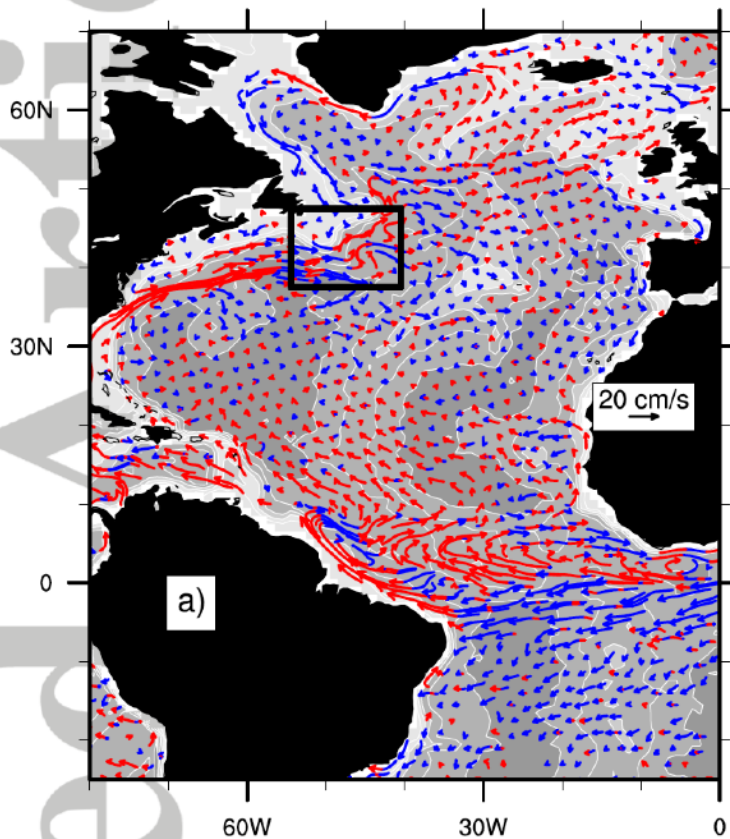




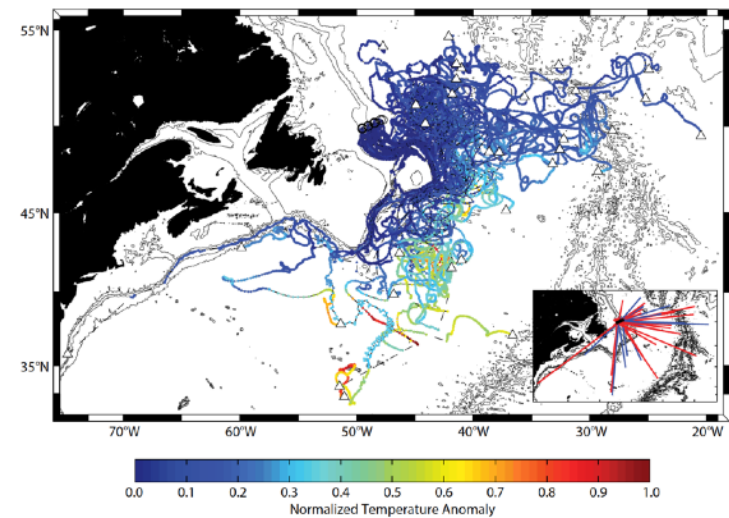
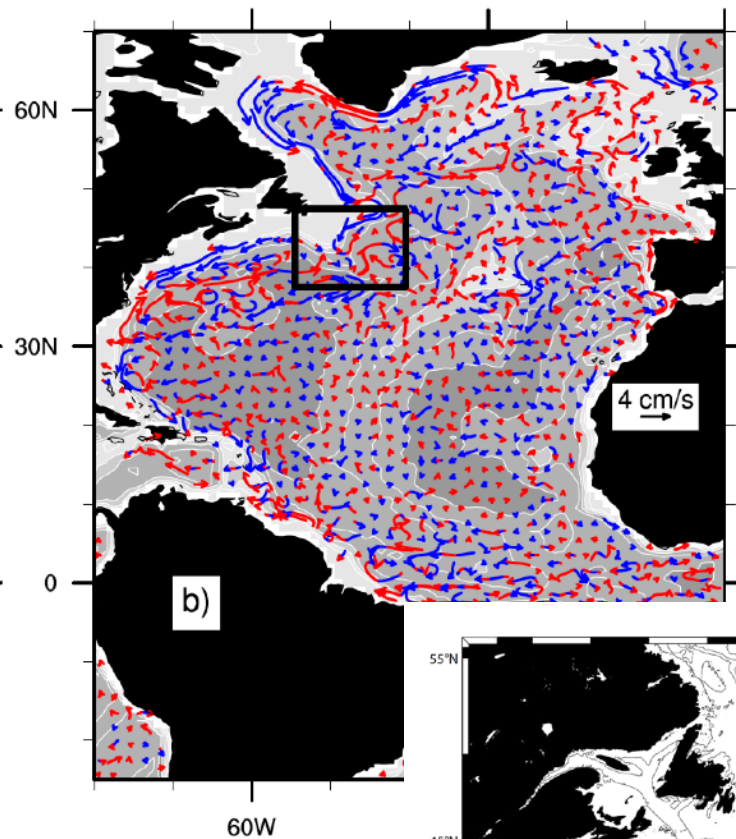


# Pathways

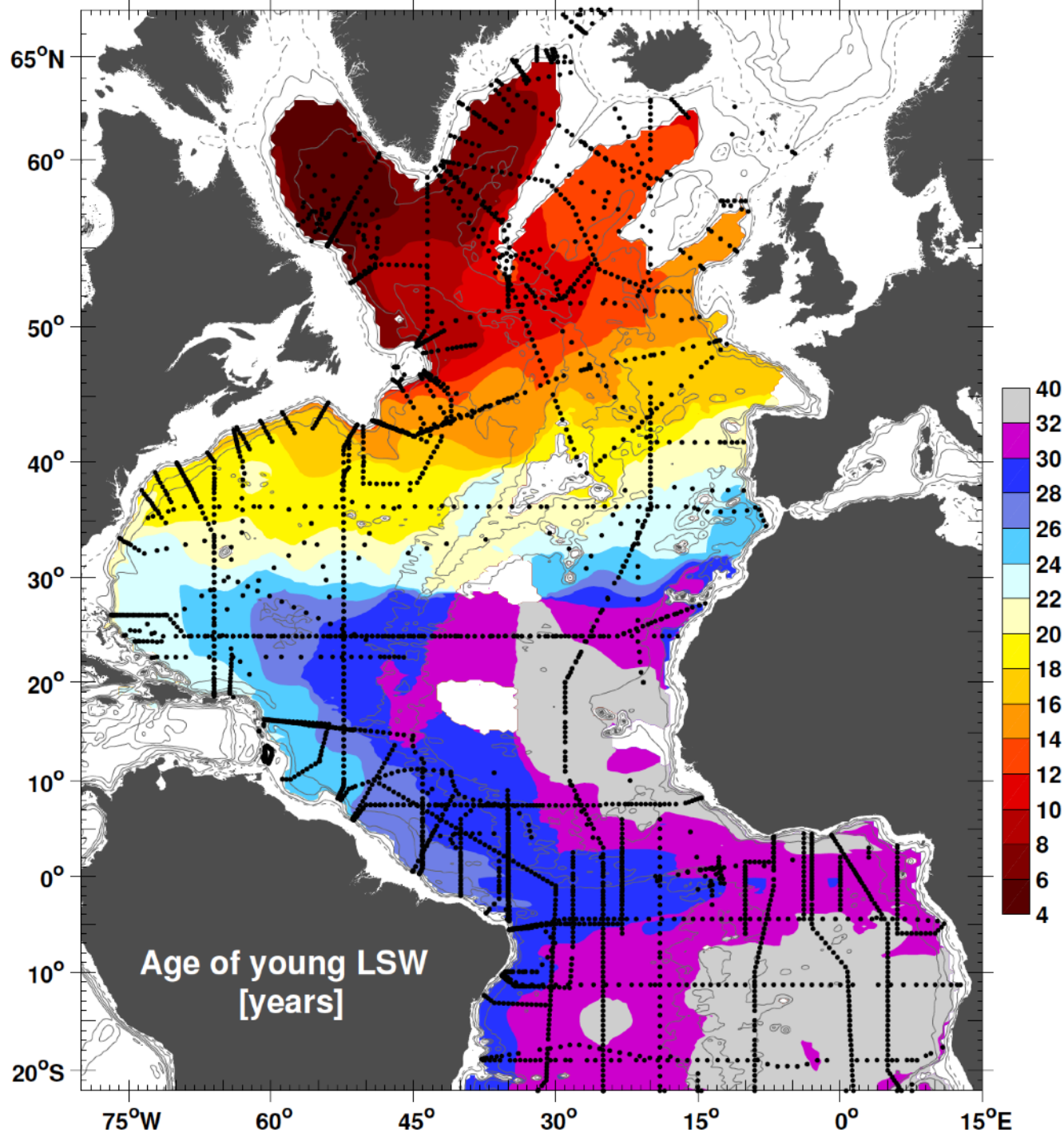
Currents at the surface from drifters



Currents at 1000 m from Argo



Bower, A. S., M. S. Lozier, S. F. Gary, and C. W. Boning (2009), Interior pathways of the North Atlantic meridional overturning circulation, *Nature*, 459, 243–247.  
 Lumpkin, R., S. A. Grodsky, L. Centurioni, M.-H. Rio, J. A. Carton, and D. Lee (2013), Removing spurious low-frequency variability in drifter velocities, *Journal of Atmospheric and Oceanic Technology*, 30 (2), 353–360.  
 Ollitrault, M., and A. Colin de Verdiere (2014), The ocean general circulation near 1000-m depth, *J. Phys. Oceanogr.*, 44 (1), 384–409, doi:10.1175/JPO-D-13-030.1.



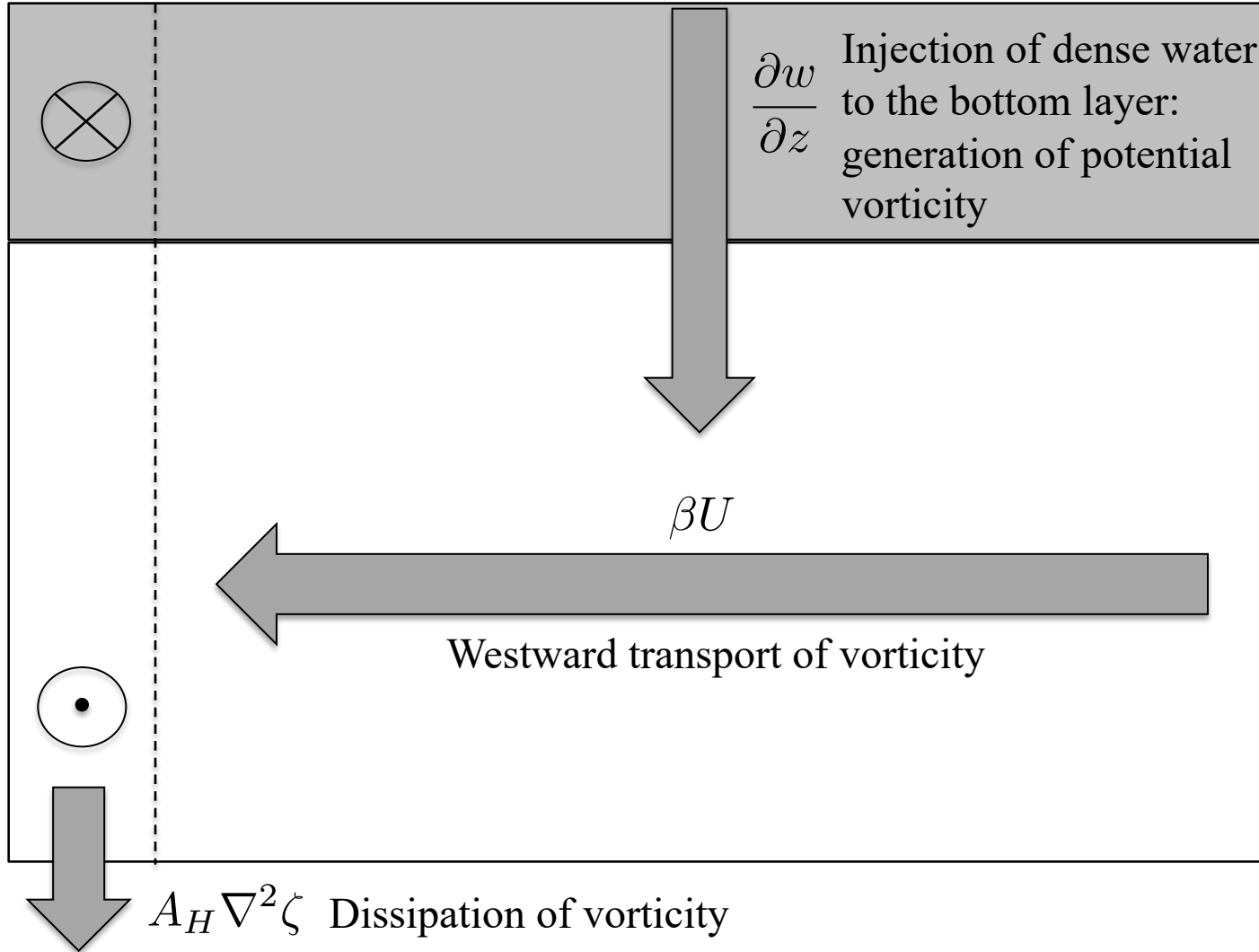
## Tracers

Map of tracer age of the Labrador Sea Water (LSW) layer calculated from CFC concentrations for LSW younger than 40 years.

Rhein, M., D. Kieke, and R. Steinfeldt (2015), Advection of North Atlantic Deep Water from the Labrador Sea to the southern hemisphere, *Journal of Geophysical Research: Oceans*, 120(4), 2471–2487, doi:10.1002/2014JC010605.



Atmospheric thermohaline forcing:  
Intense  $Q_H$  and  $E$



Which mechanism is transporting vorticity/energy **westwards**? (see large-scale waves)

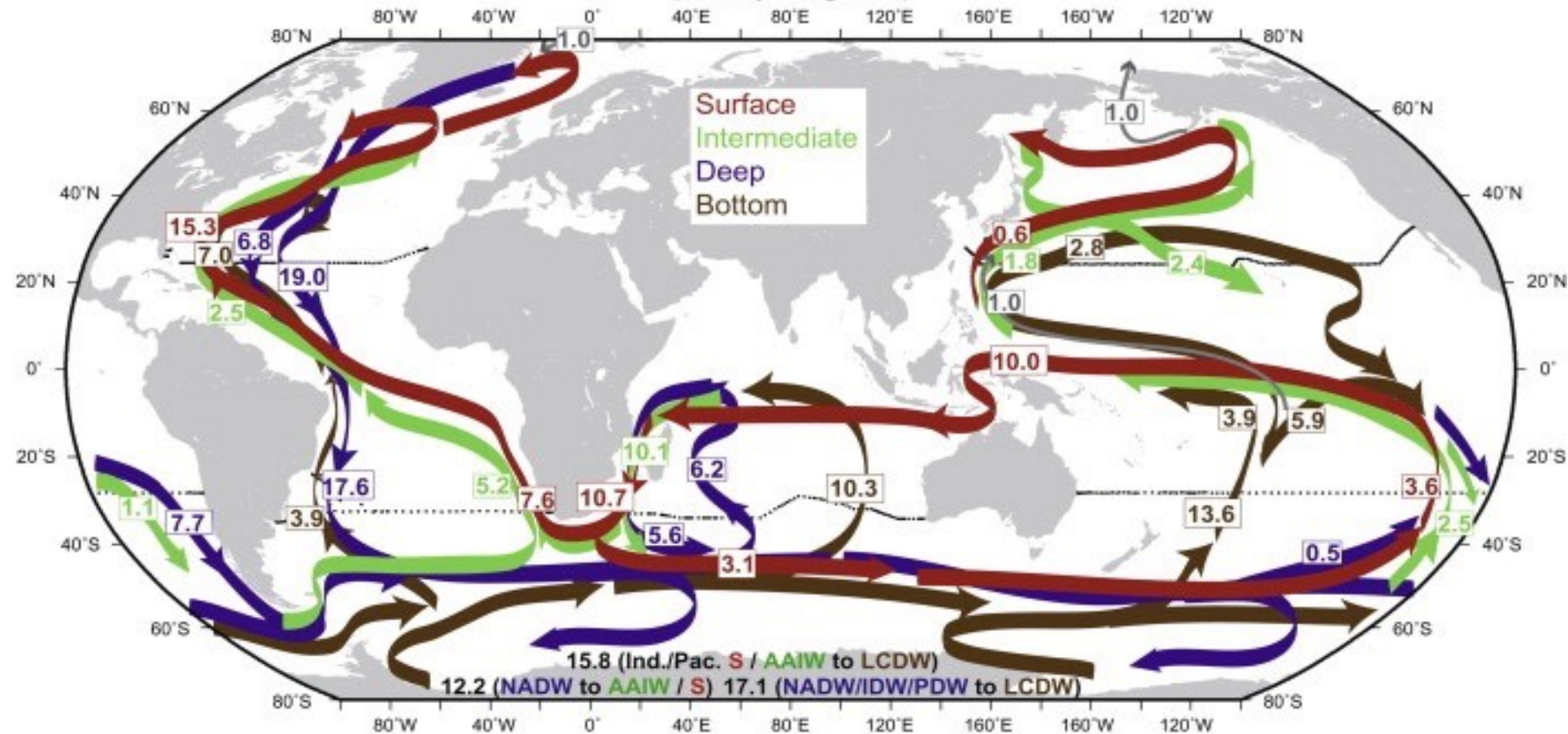
Western boundary

Interior



# The “conveyor belt” The “overturning circulation”

Intermediate and deep overturning volume transports (Sv)  
(Zonally-integrated)



# The thermohaline routes

