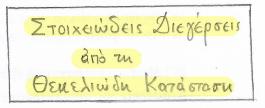
$$\begin{split} \hat{H}_{\Delta\Sigma} &= \begin{pmatrix} E_2 & \emptyset \\ \emptyset & E_1 \end{pmatrix} = E_2 \hat{S}_+ \hat{S}_- + E_A \hat{S}_- \hat{S}_+ \\ &= E_2 |2 \rangle \langle 2| + E_A |A \rangle \langle A| \\ &= E_2 \hat{a}_{12}^+ \hat{a}_{12} + E_A \hat{a}_M^+ \hat{a}_{14} \\ &:= E_2 \hat{c}_2^+ \hat{c}_2^- + E_A \hat{c}_A^+ \hat{c}_A^- \\ |X \rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix} \langle X| = (\alpha^* \beta^*) \\ |X \rangle = |0 \rangle = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \langle 1| = \langle 0| = (0 \ 0) \\ |4 \rangle = |A \rangle = \begin{pmatrix} 0 \\ 4 \end{pmatrix} \langle 4| = \langle 2| = (A \ 0) \\ |A \rangle = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 4 \end{pmatrix} (0 \ A) = \begin{pmatrix} 0 \\ 0 \ A \end{pmatrix} \\ \hat{a}_{14}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 4 \end{pmatrix} (0 \ A) = \begin{pmatrix} 0 \\ 0 \ A \end{pmatrix} \\ \hat{a}_{22}^+ = |2 \rangle \langle 2| = \begin{pmatrix} 1 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} A \ 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 4 \end{pmatrix} (0 \ A) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = |A \rangle \langle A| = \begin{pmatrix} 0 \\ 0 \end{pmatrix} (A \ 0) = \begin{pmatrix} 0 & 0 \\ 0 \ 0 \end{pmatrix} \\ \hat{a}_{12}^+ = A_{24} A \\ \hat{a}_$$

 $\hat{a}_{\mu\nu} = |\mu\rangle\langle\nu|$ $\hat{a}^{\dagger}_{\mu\nu} = |\nu\rangle\langle\mu|$



elementary excitations from the ground state

$$\hat{c}_i = \hat{a}_{1i} = |1\rangle \langle i|$$
$$\hat{c}_i^{\dagger} = \hat{a}_{1i}^{\dagger} = |i\rangle \langle 1|$$

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$$\hat{a}_{22} = \hat{a}_{22} \quad \hat{a}_{21} = \hat{a}_{12}$$

 $\hat{a}_{12} = \hat{a}_{21} \quad \hat{a}_{11} = \hat{a}_{11}$

$$\begin{split} \hat{H}_{TT} &= \begin{pmatrix} F_3 & \phi & \phi \\ \phi & F_2 & \phi \\ \phi & \phi & F_4 \end{pmatrix} = F_3 |3\rangle \langle 3| + F_2 |2\rangle \langle 2| + F_4 |4\rangle \langle 4| \\ &= F_3 \hat{\alpha}_{13}^4 \hat{\alpha}_{43} + F_2 \hat{\alpha}_{14}^4 \hat{\alpha}_{44} + \hat{\alpha}_{44} \hat{\alpha}_{44} \\ &:= F_3 \hat{c}_3^4 \hat{c}_3^4 + F_2 \hat{c}_2^4 \hat{c}_2^2 + F_4 \hat{c}_4^4 \hat{\alpha}_{44} \\ &:= F_3 \hat{c}_3^4 \hat{c}_3^4 + F_2 \hat{c}_2^4 \hat{c}_2^2 + F_4 \hat{c}_4^4 \hat{c}_4^4 \\ \hat{\beta} \\ \end{pmatrix} \\ &| \rangle = |\phi\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle = \begin{pmatrix} \phi \\ \phi \\ \phi \end{pmatrix} & \langle 4| = (\phi & \phi) \\ \\ |1\rangle &$$

$$\hat{\partial}_{23} = |2\rangle \langle 2| = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \begin{pmatrix} n \phi \phi \\ 0 \end{pmatrix} = \begin{pmatrix} 0 & \phi \phi \\ 1 & \phi \phi \\ 0 & \phi \phi \end{pmatrix} = \hat{\partial}_{32}$$

$$\hat{\partial}_{23}^{+} = |3\rangle \langle 2| = \begin{pmatrix} n \\ \phi \\ 0 \end{pmatrix} \begin{pmatrix} \phi & n \phi \\ 0 \end{pmatrix} = \begin{pmatrix} 0 & n \phi \\ 0 & \phi \phi \\ 0 \end{pmatrix} = \hat{\partial}_{32}$$

$$= \begin{pmatrix} 0 & n \phi \\ 0 & \phi \phi \\ 0 & \phi \phi \end{pmatrix} = \hat{\partial}_{32}$$

$$\hat{a}_{33} = \hat{a}_{33} \quad \hat{a}_{32} = \hat{a}_{23} \quad \hat{a}_{32} = \hat{a}_{23} \quad \hat{a}_{31} = \hat{a}_{13} \quad \hat{a}_{31} = \hat{a}_{13} \quad \hat{a}_{22} = \hat{a}_{22} \quad \hat{a}_{21} = \hat{a}_{12} \quad \hat{a}_{21} = \hat{a}_{21} \quad \hat{a}$$

$$\begin{split} \hat{H}_{\Delta\Sigma} &= \begin{pmatrix} E_{1} & \varphi \\ \varphi & E_{2} \end{pmatrix} = E_{2} |2\rangle \langle 2| + E_{1} |1\rangle \langle 1| \\ &= E_{2} \hat{a}_{12}^{+} \hat{a}_{12} + E_{1} \hat{a}_{14}^{+} \hat{a}_{14} \\ &= E_{2} \hat{c}_{2}^{+} \hat{c}_{2}^{+} + E_{1} \hat{c}_{1}^{+} \hat{c}_{1} \\ \hat{a}_{\mu\nu} &= |\mu\rangle \langle \nu| \\ \hat{a}_{\mu\nu}^{+} &= |\mu\rangle \langle \mu| \\ \hat{a}_{\mu\nu}^{+} &=$$

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$$\hat{c}_{i} = \hat{a}_{1i} = |1\rangle \langle i|$$

 $\hat{c}_{i}^{\dagger} = \hat{a}_{1i}^{\dagger} = |i\rangle \langle 1|$

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$$|1\rangle = \begin{pmatrix} 1\\ 0\\ 0 \end{pmatrix} \qquad |2\rangle = \begin{pmatrix} 0\\ 1\\ 0 \end{pmatrix} \qquad |3\rangle = \begin{pmatrix} 0\\ 0\\ 1 \end{pmatrix}$$

 $\hat{a}_{n} = |n\rangle\langle n| = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} n & 0 & 0 \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} = \hat{a}_{1n}$ $\hat{\partial}_{22} = \lfloor 2 \rangle \langle 2 \rfloor = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \begin{pmatrix} 0 \land 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} = \hat{\partial}_{22}$

$$\hat{\partial}_{33} = |3\rangle \langle 3| = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} 0 & 0 & 1 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \hat{\partial}_{33}^{+}$$

$$\hat{\partial}_{12} = |1\rangle \langle 2| = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} 0 & 1 & 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} = \hat{\partial}_{21}^{+}$$

$$\hat{\partial}_{13}^{+} = |2\rangle \langle 1| = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} 0 & 0 & 1 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} = \hat{\partial}_{21}^{+}$$

$$\hat{\partial}_{13}^{+} = |3\rangle \langle 2| = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \begin{pmatrix} 0 & 0 & 1 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 \end{pmatrix} = \hat{\partial}_{31}^{+}$$

$$\hat{\partial}_{23}^{+} = |3\rangle \langle 2| = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} = \hat{\partial}_{32}^{+}$$

$$\begin{array}{c} \underline{no\overline{u}} \neq 1 \ \overline{\sigma tov \ niveka}; \\ \hat{a}_{11} = \hat{a}_{11} \ \hat{a}_{12} = \hat{a}_{21}^{\dagger} \ \hat{a}_{12} = \hat{a}_{21}^{\dagger} \ \hat{a}_{13} = \hat{a}_{31}^{\dagger} \\ \hat{a}_{21} = \hat{a}_{12}^{\dagger} \ \hat{a}_{22} = \hat{a}_{22}^{\dagger} \ \hat{a}_{23} = \hat{a}_{32}^{\dagger} \\ \hat{a}_{31} = \hat{a}_{13}^{\dagger} \ \hat{a}_{32} = \hat{a}_{23}^{\dagger} \ \hat{a}_{33} = \hat{a}_{32}^{\dagger} \\ \end{array}$$

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