LECTURE 2 MICROECONOMIC THEORY CONSUMER THEORY Consumer Choice

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Consumer choice

(in the spirit of the choice-based approach)

Fundamental decision unit: the consumer

Definition (Market)

The "place" where demand and supply meet. A setting in which consumers can buy products at known prices (or, equivalently, trade goods at known exchange rates).

Question: How do consumers make constrained choices?

Consumer choice: decision theory when individuals face given market prices.

Consumer choice: basic concepts Commodities

- Commodities (goods and services) what is available for purchase in the market
 - Finite number L of divisible goods (commodities)

 - \mathbb{R}^{L}_{+} is the commodity space $X \subset \mathbb{R}^{L}_{+}$ is the consumption set
 - $x \in X$ is a consumption vector or consumption bundle



Consumer choice: basic concepts Consumption set

- □ The number of commodities is finite and equal to *L* (indexed by $\ell = 1, ..., L$).
- A commodity vector (or commodity bundle) is a list of amounts of the different commodities,





Consumer choice: basic concepts Consumption set

The consumption set (X): subset of the commodity space. Limitations may result from physical or institutional restrictions. Elements of X are bundles that an individual may

consume given the context's physical constraints.

EXAMPLES

Consumption of bread and leisure: $X = \left\{ (b, l) \in \mathbb{R}^2_+ : l \leq 24 \right\}$

Minimum consumption of white or brown bread (survival consumption): $X = \{(w, b) \in \mathbb{R}^2_+ : w + b \ge 4\}$

 $X = \mathbb{R}^L_+ = \left\{ x \in \mathbb{R}^L \colon x_l \ge 0, \ l = 1 \dots L \right\}$





























Consumer choice: basic concepts Budget set	
 Consumer's problem: Given <i>p</i> and <i>w</i>, "choose a consumption bundle <i>x</i> from <i>B_{p,w}</i>". When all wealth is exhausted: the set 	
$\{x \in R_{+}^{L} : p \cdot x = w\}$ of just affordable bundles is called budget hyperpla – If <i>L</i> =2 it is called the budget line.	ne
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The Walrasian budget set is convex.

Let $x^{"} = ax+(1-a)x'$. If x and x' are elements of the budget set (i.e. if $x \cdot p \le w$ and $x' \cdot p \le w$), then for a in [0,1] $p \cdot x^{"} = a(p \cdot x) + (1 - a)(p \cdot x') \le w$ and x" is also element of the budget set, i.e. $x^{"} \in B$.

Proof?

Intuition: linear combinations of consumption bundles that belong to the budget set, are also affordable.

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Consumer choice: basic concepts Demand function



- How much a consumer will buy?
- How much a consumer will buy when prices are at the market equilibrium?
- How much a consumer would want to buy at every reasonable combination of income and prices?

Consumer choice: basic concepts Demand function

2 important properties of the demand correspondence
 Homogeneity of degree 0
 Walras' law is satisfied.

Definition (Homogeneity of degree 0)

A demand function x(p, w) is homogeneous of degree 0 if

 $x(\alpha p, \alpha w) = x(p, w)$ for any (p, w) and $\alpha > 0$

- Homogeneity of degree zero means that the absolute level of prices and wealth doesn't matter. No money illusion.
- Only the relative values have an effect













Consumer choice: comparative statics

- □ Examples of Giffen goods: low quality goods consumed by consumers with low wealth levels.
- □ A poor consumer fulfills much of his dietary requirements with potatoes (low cost, filling food).
- □ Price of potatoes falls. Now he can afford to buy other, more desirable foods, and his consumption of potatoes may fall as a result.
- □ Wealth consideration involved (when the price of potatoes falls, the consumer is effectively wealthier)



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Consumer choice: comparative statics

2. By Walras' Law, $p \cdot x(p,w) = w$. Differentiation w.r.t. wealth w yields:

Intuition: Total expenditure must change by an amount equal to the

WARP and the law of demand

□ We assume the following:

(i) Weak Axiom of Revealed Preferences (Chapter 1) (ii) Homogeneity of degree 0 (iii) Walras' law

i.e. we impose more consistency on choices. In fact, these three assumptions will be satisfied when we derive the consumer's demand from the classical demand theory (see the preference-based approach, next chapter).

What are the implications?

WARP and the law of demand Definition (Weak Axiom (comparing two situations)) The demand function x(p, w) satisfies the WA if $\forall (p, w) \text{ and } \forall (p', w') \text{ we have the following property:}$ If $p \cdot x(p', w') \leq w$ and $x(p', w') \neq x(p, w)$ $\Rightarrow p' \cdot x(p, w) > w'$ **Intuition**: If the bundle x(p', w') is feasible when the agent faces price-wealth (p, w) and (by definition) the agent chooses x(p, w), this **reveals** a preference of the agent for x(p, w) over x(p', w'). Then, since the agent chooses x(p', w') when facing price-wealth (p', w'), it **must be** that he cannot afford x(p, w).

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WARP and the law of demand

- following slide shows some examples
- $\qquad x^* = x(p^*, w^*), \ x' = x(p', w'), \ and \ x^* \neq x'$
- remember our assumptions that x(p,w) is single-valued











Implications of the WARP

- Before we elaborate on the law of demand, an additional concept shall be introduced.
 - When the price of a commodity changes (e.g. increases) the consumer is affected in two ways:
 - Wo Ways:
 The commodity whose price has increased has become more expensive relative to other commodities.
 The consumer is impoverished (the purchasing power of his wealth has decreased).

Slutsky wealth compensation

· Price changes affect relative prices and the real value of wealth (income). Slutsky compensated price changes combine a price change with a (hypothetical) adjustment of wealth such that the previously demanded consumption bundle again is just affordable.¹

• Let $x^*=x(p^*,w^*)$. If the price vector changes to p', then the wealth compensation is defined as $\Delta w = \Delta p \cdot x^*$, where $\Delta p = (p^* - p^*)$.

¹ Conversely, a Hicks compensation would adjust wealth such that the old utility level can just be reached despite the price change.









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Law of (compensated) demand: implications

□ If consumer demand *x*(*p*,*w*) is a differentiable factor of prices and wealth, the law of *compensated* demand can be written as:

 $dp \bullet dx \leq 0$

What are the implications of this relation?

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Law of (compensated) demand: implications

- What does it mean to give the consumer a compensated price change?
- Let the initial consumption bundle be $\hat{x} = x(p,w)$, where *p* and *w* are the original prices and wealth.
- □ A compensated price change means that at any price, *p*, the original bundle is still available. Hence after the price change, wealth is changed to $\hat{w}^{=p\bullet} \hat{x}$.



Consider the consumer's demand for good *i*:

 $x_{i}^{c}=x_{i}\left(p,p\cdot\hat{x}\right)$

following a compensated change in the price of good *j*:

$$\begin{array}{lcl} \displaystyle \frac{d}{dp_j}\left(x_i\left(p,p\cdot\hat{x}\right)\right) &=& \displaystyle \frac{\partial x_i}{\partial p_j}+\frac{\partial x_i}{\partial w}\frac{\partial\left(p\cdot\hat{x}\right)}{\partial p_j} \\ \\ \displaystyle \frac{dx_i^c}{dp_j} &=& \displaystyle \frac{\partial x_i}{\partial p_j}+\frac{\partial x_i}{\partial w}\hat{x}_j. \end{array}$$





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Law of (compensated) demand: implications

- One nice mathematical property of negative semidefinite matrices:
 - The diagonal elements s_{ii} are non-positive (generally there will be strictly negative)
- This means that the change in demand for a good in response to a compensated price increase is negative (compensated law of demand)
- Why so much fuss about something so obvious?
- We derived this based only on the WARP and Walras' law.



- How does *s_{ii}* help us explain the existence of Giffen goods?
- Ordinarily if the price of a good increases, holding wealth constant, the demand of that good will decrease (law of demand). But not in the case of Giffen goods.
- Example: A consumer spends all of her money on two things: food and trips to Hawaii. Suppose the price of food increases. It may be that after the increase, the consumer can no longer afford the trip to Hawaii and therefore spends all of her money on food. The result is that the consumer actually buys more food than she did before the price increase.













Law of (compensated) demand: implications

Result

- In order for a good to be a Giffen good, it must be a strongly inferior good.
- A normal good can never be a Giffen good.

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Main points

- □ The *consumer* is the decision maker
- In the market economy prices are given (the consumer is a price-taker)
- Commodities are the objects of choice.
- □ The *consumption set* describes the *physical constraints* that limit the consumer's choices
- □ The *Walrasian budget set* describes the *economic constraints* that limit the consumer's choices.

Main points

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- □ The Walrasian demand function describes the consumer's choices (decision) subject to the above constraints.
- We studied the ways in which consumer demand changes when economic constraints vary (comparative statics)
- □ We studied the implication of the WARP for the consumer's demand function
- The WARP is essentially equivalent to the *law of compensated demand* (i.e. prices and demanded quantities move in opposite directions for price changes that leave real wealth unchanged).
- We studied several implications of the law of compensated demand.