LECTURE 2 MICROECONOMIC THEORY CONSUMER THEORY Consumer Choice

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Consumer choice

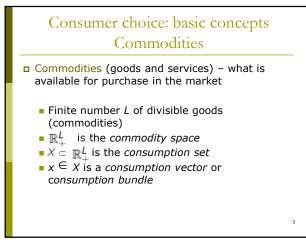
Fundamental decision unit: the consumer

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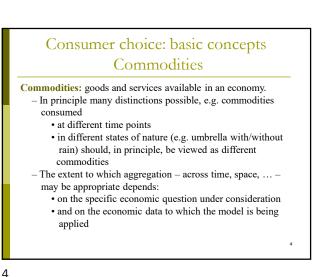
Definition (Market) The "place" where demand and supply meet. A setting in which consumers can buy products at known prices (or, equivalently, trade goods at known exchange rates).

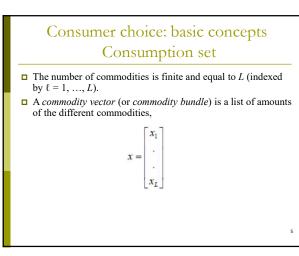
Question: How do consumers make constrained choices?

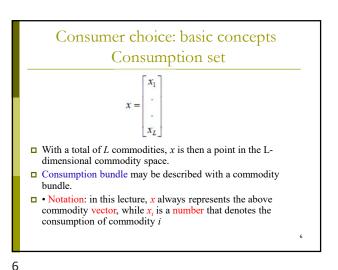
Consumer choice: decision theory when individuals face given market prices.











Consumer choice: basic concepts Consumption set

The consumption set (X): subset of the commodity space. Limitations may result from physical or institutional restrictions.

Elements of *X* are bundles that an individual may consume given the context's *physical constraints*.

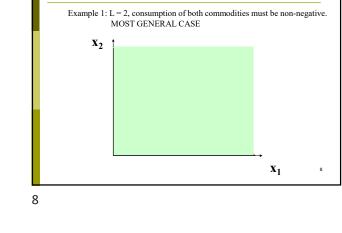
EXAMPLES

Consumption of bread and leisure: $X = \left\{ (b, l) \in \mathbb{R}^2_+ : l \leq 24 \right\}$

Minimum consumption of white or brown bread (survival consumption): $X = \{(w, b) \in \mathbb{R}^2_+ : w + b \ge 4\}$

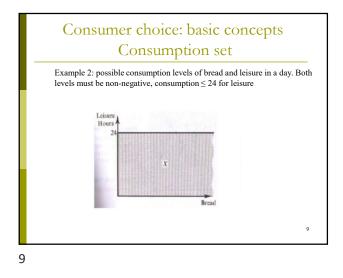
$$X = \mathbb{R}_+^L = \left\{ x \in \mathbb{R}^L \colon x_l \ge 0, \ l = 1 \dots L \right\}$$

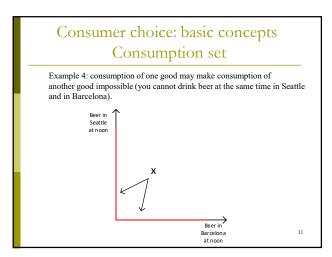


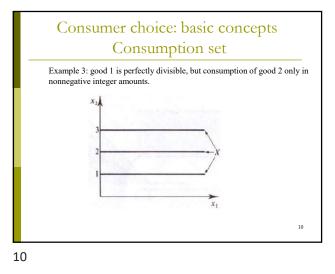


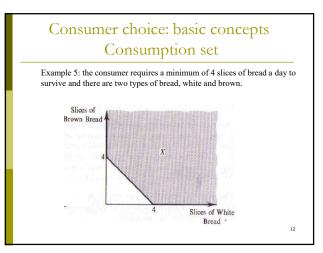
Consumer choice: basic concepts

Consumption set

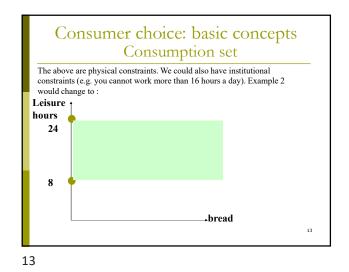




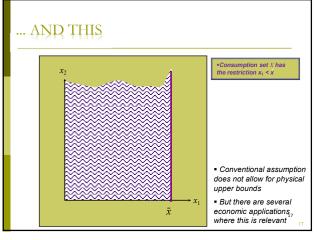


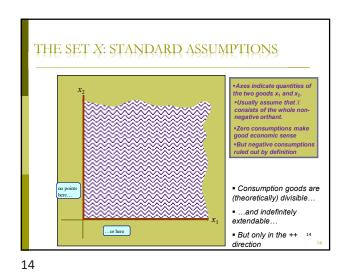


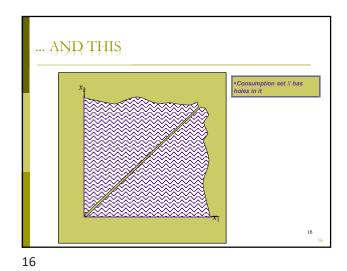


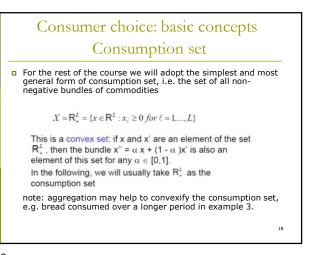


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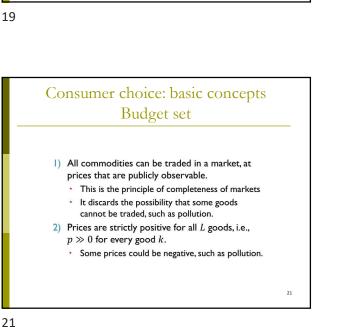


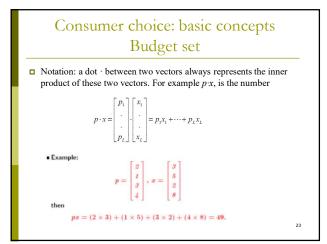


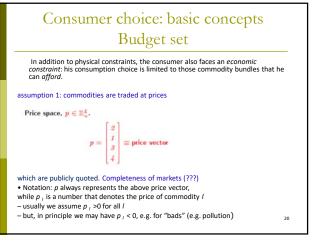
Consumer choice: basic concepts Consumption set

 Intuitively, a consumption set is convex if, for any two bundles that belong to the set, we can construct a straight line connecting them that lies completely within the set.

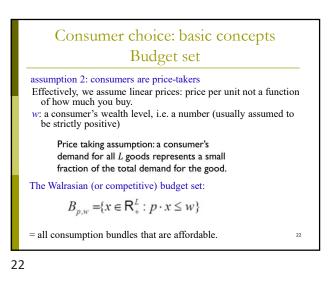
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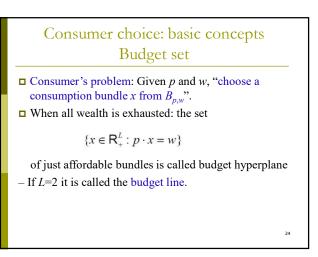


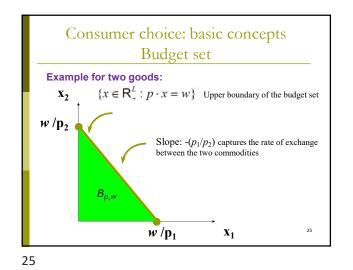


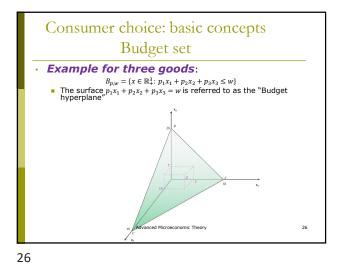


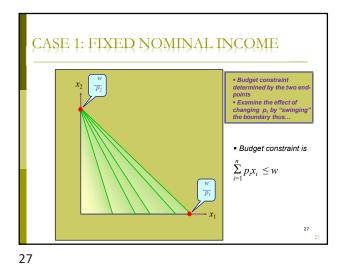
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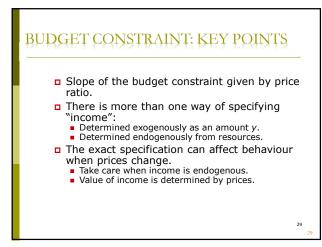


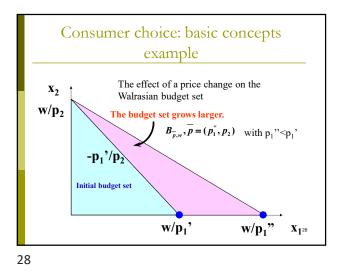












Consumer choice: basic concepts Budget set

The Walrasian budget set is convex.

Let x'' = ax+(1-a)x'. If x and x' are elements of the budget set (i.e. if $x \cdot p \le w$ and $x' \cdot p \le w$), then for a in [0,1] $p \cdot x'' = a(p \cdot x) + (1 - a)(p \cdot x') \le w$ and x'' is also element of the budget set, i.e. $x'' \in B$.

Proof?

Intuition: linear combinations of consumption bundles that belong to the budget set, are also affordable.

Consumer choice: basic concepts Demand function

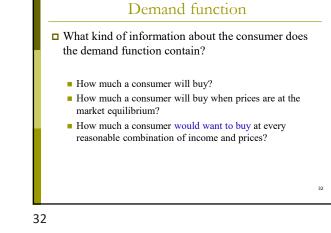
In the neoclassical model of consumer behavior, the demand function maps prices (p) and income (or wealth, w) into a commodity-choice vector x(p,w).

 In general, demand is a correspondence; x(p,w) ⊂ X, but we usually assume that x(p,w) contains only one point (singleton) so that demand is a function.

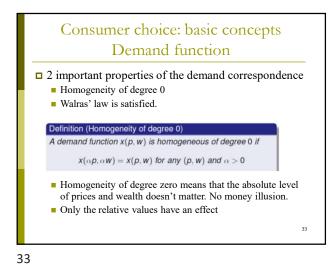
Price and wealth determine budget set, nothing more.

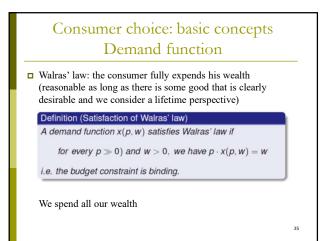
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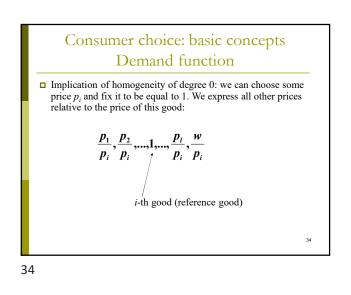
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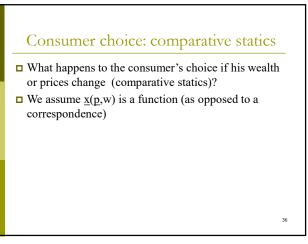


Consumer choice: basic concepts







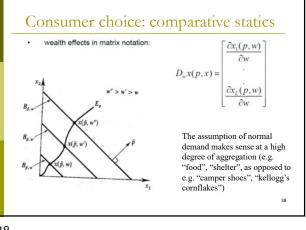


Consumer choice: comparative statics

Comparative Statics

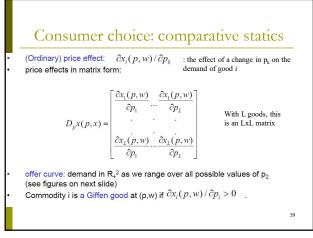
- Wealth (income) effect
 - the consumer's Engel function: demand as a function of wealth for given prices x(<u>p</u>,w)
 - Notation: due to the limitations of powerpoint I use underline instead of overline to denote fixed variables
 - wealth/income expansion path: its image in the commodity space RL⁺ (see figure on next slide)
 - ∂x_i(p,w)/∂w: wealth/income effect for the I-th commodity
 - commodity / is normal if $\partial x_i(p,w)/\partial w \ge 0$
- commodity / is inferior if $\partial x_i(p,w)/\partial w < 0$
- we say that demand is normal if every commodity is normal at all (p,w)

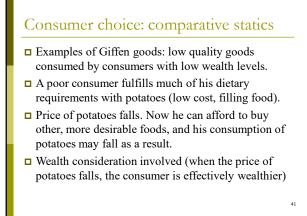
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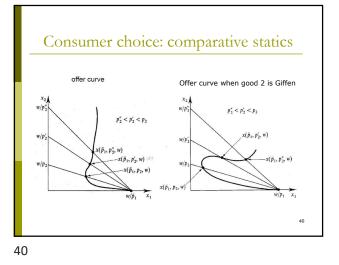


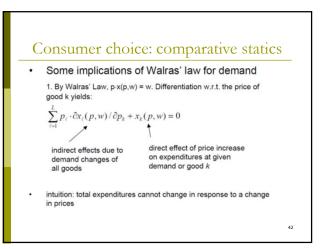
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37









Consumer choice: comparative statics

2. By Walras' Law, p-x(p,w) = w. Differentiation w.r.t. wealth w yields:

$$\sum_{\ell=1}^{L} p_{\ell} \cdot \partial x_{\ell}(p, w) / \partial w = 1$$

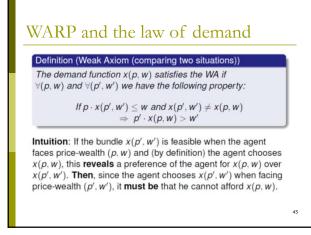
Intuition: Total expenditure must change by an amount equal to the wealth change.

43

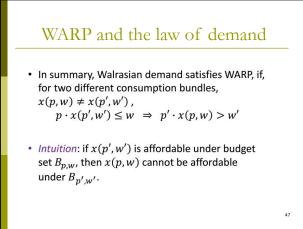
WARP and the law of demand • Ware assume the following: • Weak Axiom of Revealed Preferences (Chapter 1) • Di Omogeneity of degree 0 • Warras' haw Assumptions while satisfied when we derive the forsumer's demand from the classical demand theory (see the preference-based approach, next chapter). What me the implications?

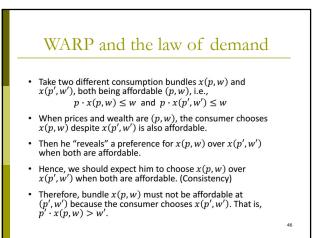
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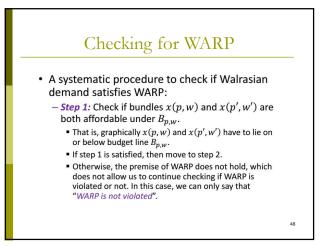
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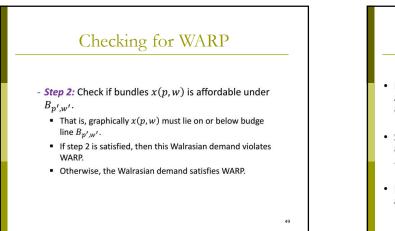


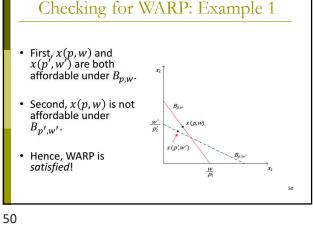
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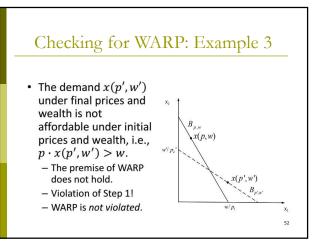


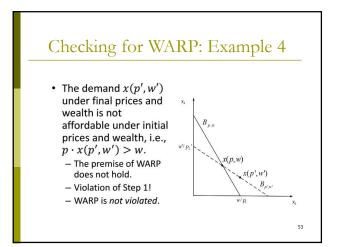


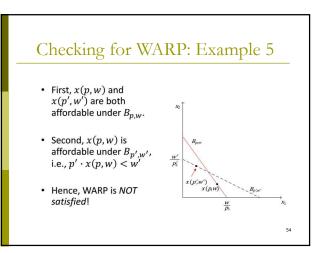


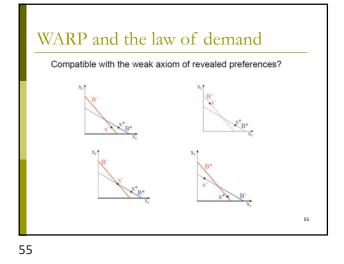
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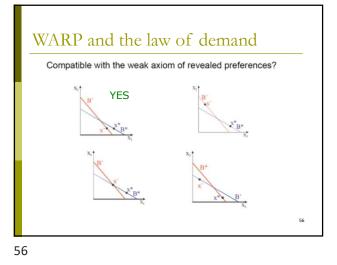


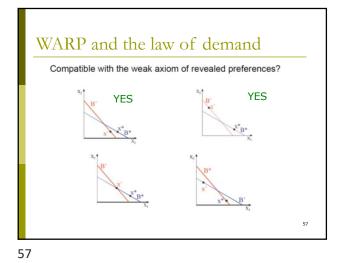


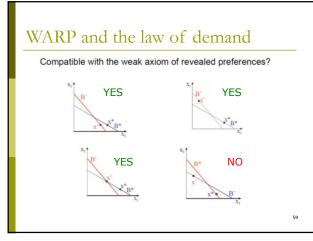


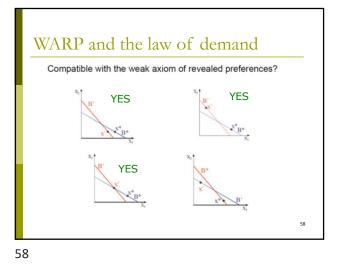


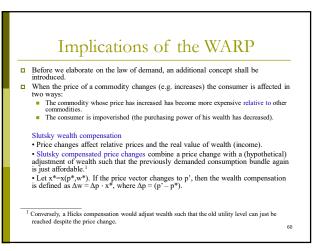


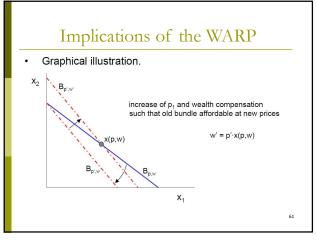




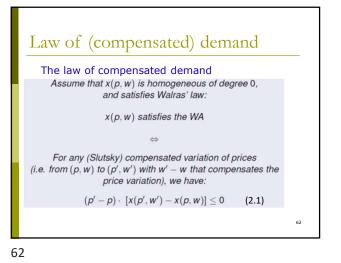


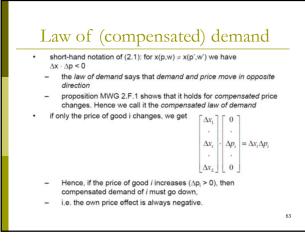




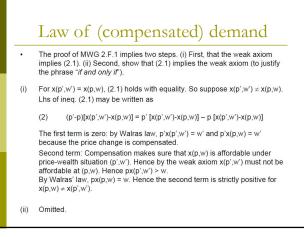


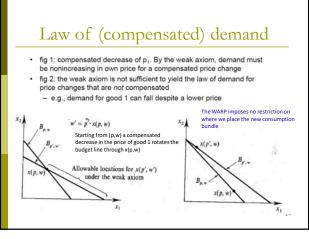
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63





64

Law of (compensated) demand: implications

□ If consumer demand *x*(*p*,*w*) is a differentiable factor of prices and wealth, the law of *compensated* demand can be written as:

 $dp \bullet dx \leq 0$

What are the implications of this relation?

Law of (compensated) demand: implications

- What does it mean to give the consumer a compensated price change?
- Let the initial consumption bundle be $\hat{x} = x(p,w)$, where *p* and *w* are the original prices and wealth.
- □ A compensated price change means that at any price, p, the original bundle is still available. Hence after the price change, wealth is changed to ŵ=p• x̂.

Law of (compensated) demand: implications

□ Consider the consumer's demand for good *i*:

$$x_i^c = x_i \left(p, p \cdot \hat{x} \right)$$

following a compensated change in the price of good *j*:

$$\begin{array}{lll} \displaystyle \frac{d}{dp_j} \left(x_i \left(p, p \cdot \hat{x} \right) \right) & = & \displaystyle \frac{\partial x_i}{\partial p_j} + \displaystyle \frac{\partial x_i}{\partial w} \displaystyle \frac{\partial \left(p \cdot \hat{x} \right)}{\partial p_j} \\ \\ \displaystyle \frac{dx_i^c}{dp_j} & = & \displaystyle \frac{\partial x_i}{\partial p_j} + \displaystyle \frac{\partial x_i}{\partial w} \hat{x}_j. \end{array}$$

Law of (compensated) demand:

implications

 $dx_1(p,w)$

 $dx_2(\underline{p},w)$

 $dx_i(\underline{p},w)$

 $dx_L(\underline{p}, w)$

 $dx^c = S dp$

We can arrange the dx_i^c into a vector by stacking the equations of the

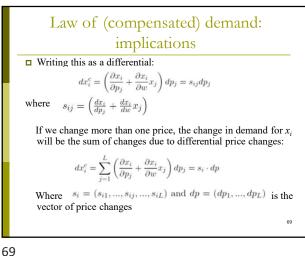
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d x

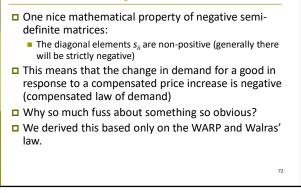
previous slide vertically. We get:

68

67



Law of (compensated) demand: implications Returning to the statement of the WARP: $dp \bullet dx^c \le 0$ Substituting in $dx^c = S \, dp$ we get: $dp \cdot S \cdot dp^T \le 0$ $(1xL) \cdot (LxL) \cdot (Lx1) = (1x1)$ This has a mathematical significance: it implies that matrix *S*, which we call the substitution matrix, is negative semi-definite (i.e. if you pre- and post- multiply it by the same vector, the result is always a non-positive number). where S is an L x L matrix with the element in the *i*th and *j*th column being s_{ij}.
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Law of (compensated) demand: implications





Law of (compensated) demand: implications

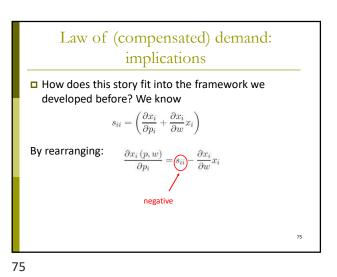
\square How does s_{ii} help us explain the existence of Giffen goods?

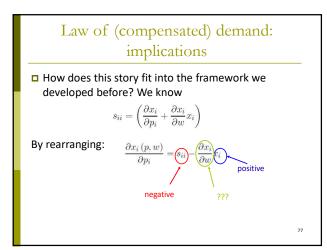
- Ordinarily if the price of a good increases, holding wealth constant, the demand of that good will decrease (law of demand). But not in the case of Giffen goods.
- Example: A consumer spends all of her money on two things: food and trips to Hawaii. Suppose the price of food increases. It may be that after the increase, the consumer can no longer afford the trip to Hawaii and therefore spends all of her money on food. The result is that the consumer actually buys more food than she did before the price increase.

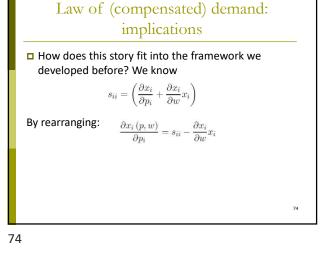
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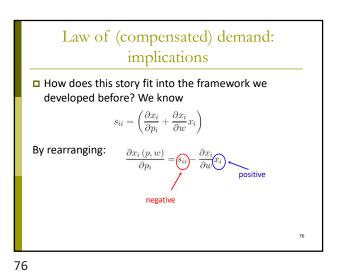
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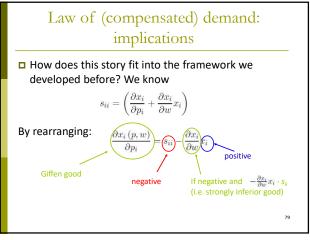




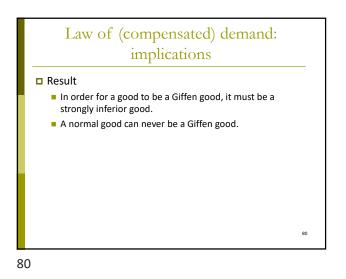


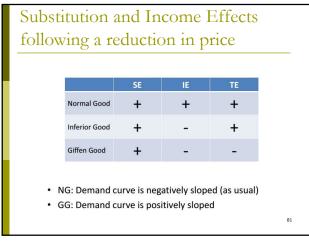


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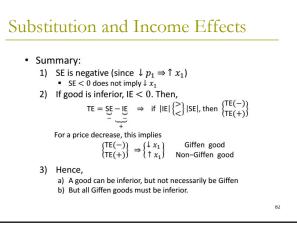
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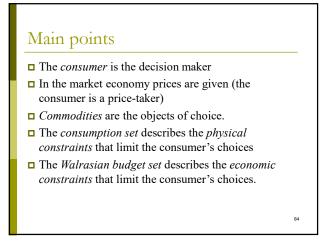
- Take an example of a tax which increases the price of a good.
- How can we measure the impact of the price change on consumers?
- *s_{ji}* is unobservable! We only observe uncompensated price changes!

But we can recover
$$s_{ii}$$
 from

$$s_{ii} = \left(\frac{\partial x_i}{\partial p_i} + \frac{\partial x_i}{\partial w}x_i\right)$$



82



Main points

- □ The *Walrasian demand function* describes the consumer's choices (decision) subject to the above constraints.
- □ We studied the ways in which consumer demand changes when economic constraints vary (*comparative statics*)
- We studied the implication of the WARP for the consumer's demand function
- The WARP is essentially equivalent to the *law of compensated demand* (i.e. prices and demanded quantities move in opposite directions for price changes that leave real wealth unchanged).
- We studied several implications of the law of compensated demand.