



THE BASICS OF PRODUCTION...

- We set out some of the elements needed for an analysis of the firm.
 - + Technical efficiency
 - + Returns to scale
 - + Convexity
 - Substitutability
 - Marginal products
- This is in the context of a single-output firm...
- ...and assuming a competitive environment.
- First we need the building blocks of a model...



MOTIVATION OF THE FIRM

- * Almost without exception we shall assume that the objective of the firm is to maximise profits: this assumes either that the firm is run by ownermanagers or that the firm correctly interprets shareholders' interests.
- More formally, we define the expression for profits as

$$\Pi = pq - \sum_{i=1}^{n} w_i z_i$$









PROPERTIES OF THE PRODUCTION FUNCTION

- * Let us examine more closely the production function given in $q \le \phi(\mathbf{z})$.
- We will call a particular vector of inputs a technique.
- It is useful to introduce two concepts relating to the techniques available for a particular output level q:

























ELASTICITY OF SUBSTITUTION

* Higher values of σ mean that the production function is more "flexible" in that there is a proportionately larger change in the production technique in response to a given proportionate change in the implicit relative valuation of the factors:

HOMOTHETIC CONTOURS

* With homothetic contours, each isoquant appears like a photocopied enlargement; along any ray through the origin all the tangents have the same slope so that the MRTS depends only on the relative proportions of the inputs used in the production process.



CONTOURS OF A HOMOGENEOUS FUNCTION

* An important subcase of the family of homothetic functions is the <u>homogeneous</u> production functions, for which the map looks the same but where the labelling of the contours has to satisfy the following rule: for any scalar t > 0 and any input vector $z \ge 0$:

$$\phi(tz) = t^r \phi(z)$$

where r is a positive scalar.

CONTOURS OF A HOMOGENEOUS FUNCTION

- × If $\varphi(.)$ satisfies the property in the above equation then it issaid to be homogeneous of degree r. Clearly the parameter r carries important information about the way output responds to a proportionate change in all inputs together:
- If r > 1, for example then doubling more inputs will more than double output.



























- × Technical efficiency
- × Returns to scale
- × Convexity
- × MRTS
- × Marginal product

WHAT NEXT?

- × Introduce the market
- * Optimisation problem of the firm
- × Method of solution
- × Solution concepts.