MICROECONOMICS

Principles and Analysis

CONSUMPTION BASICS

OVERVIEW...

The environment for the basic consumer optimisation problem.

a	sics
	The setting
	Budget sets
	U
l	
	Revealed
	Preference
	Axiomatic
	Approach

Consumption:

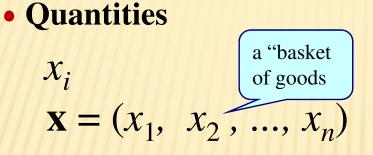
A METHOD OF ANALYSIS

- Some treatments of micro-economics handle consumer analysis first.
- But we have gone through the theory of the firm first for a good reason:
- We can learn a lot from the ideas and techniques in the theory of the firm...
- × ...and reuse them.

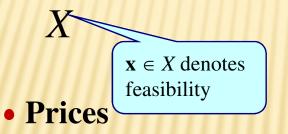
REUSING RESULTS FROM THE FIRM

- What could we learn from the way we analysed the firm....?
- **×** How to set up the description of the environment.
- **×** How to model optimization problems.
- How solutions may be carried over from one problem to the other
- × ...and more .

NOTATION



•amount of commodity *i* commodity vector



consumption set

 p_i $\mathbf{p} = (p_1, p_2, \dots, p_n)$ •price vector

•price of commodity *i*

y

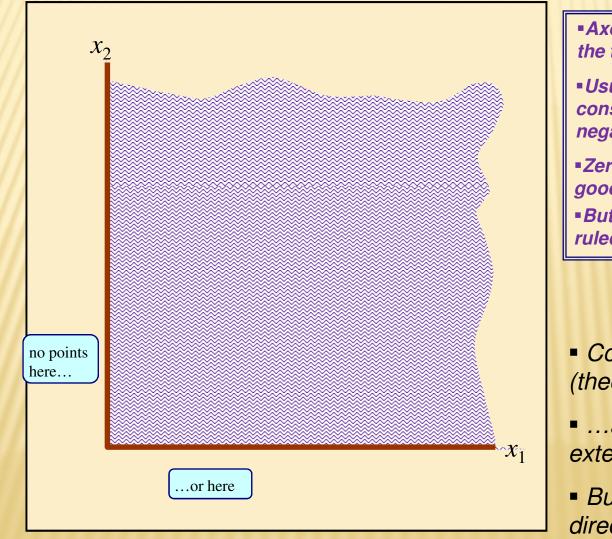
THINGS THAT SHAPE THE CONSUMER'S PROBLEM

- The set X and the number y are both important.
- But they are associated with two distinct types of constraint.
- **x** We'll save y for later and handle X now.
- * (And we haven't said anything yet about objectives...)

THE CONSUMPTION SET

- **×** The set *X* describes the basic entities of the consumption problem.
- Not a description of the consumer's opportunities.
 - + That comes later.
- Subsection Use it to make clear the type of choice problem we are dealing with; for example:
 - + Discrete versus continuous choice (refrigerators vs. contents of refrigerators)
 - + Is negative consumption ruled out?
- **x** " $x \in X$ " means "x belongs the set of logically feasible baskets."

THE SET X: STANDARD ASSUMPTIONS

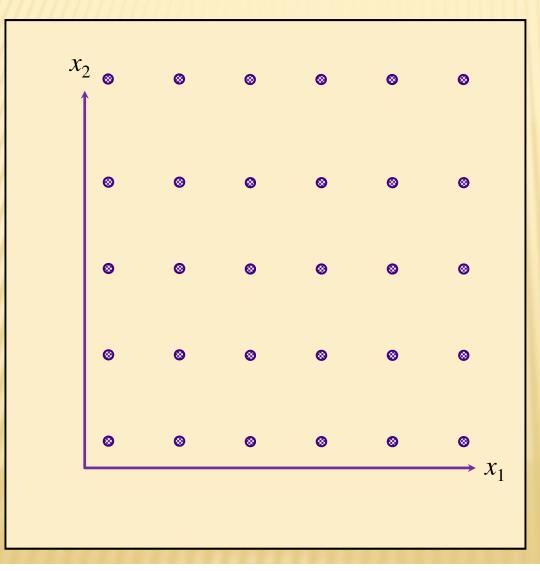


•Axes indicate quantities of the two goods x_1 and x_2 .

- Usually assume that X consists of the whole non-negative orthant.
- Zero consumptions make good economic sense
- But negative consumptions ruled out by definition

- Consumption goods are (theoretically) divisible...
- ...and indefinitely extendable...
- But only in the ++ direction

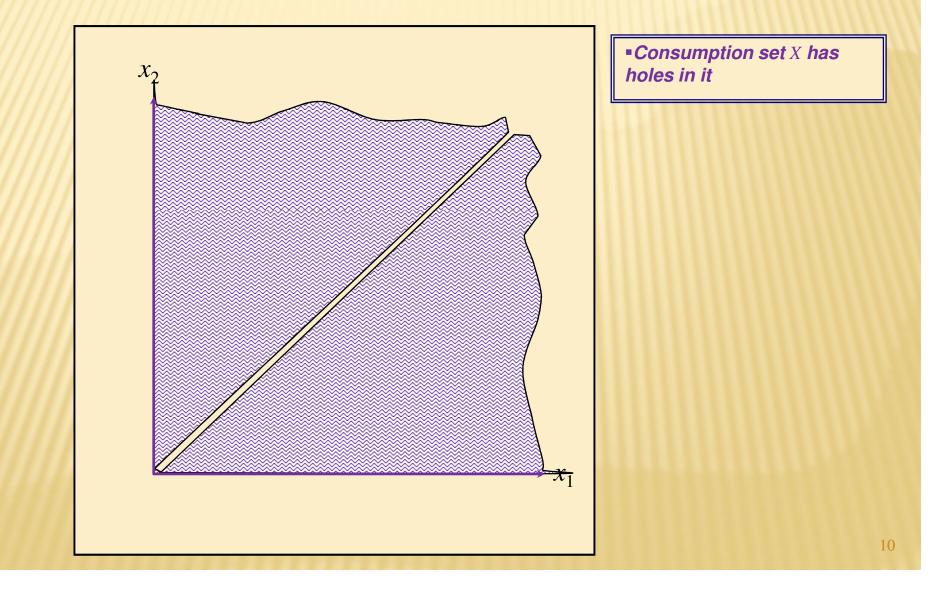
RULES OUT THIS CASE...



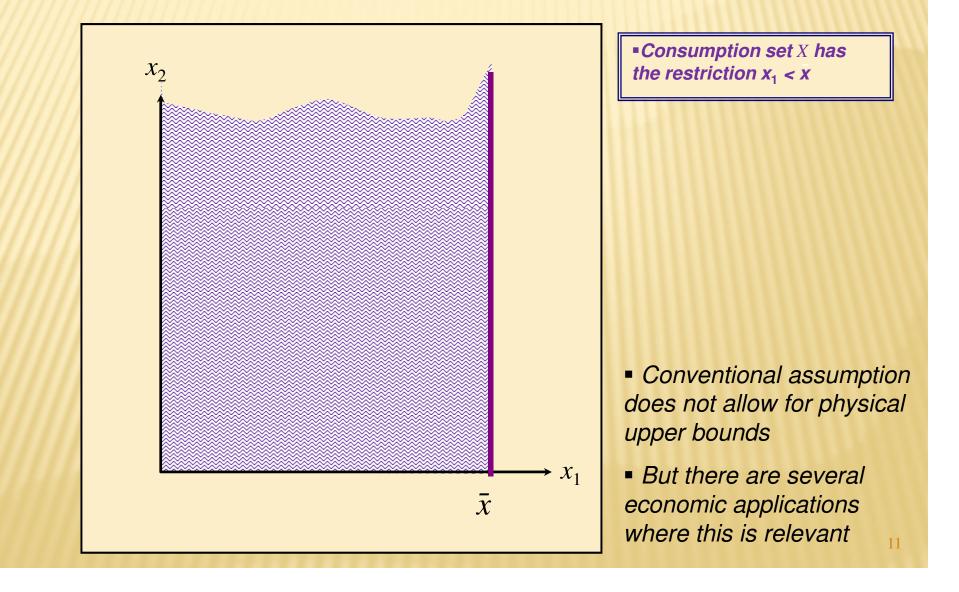
 Consumption set X consists of a countable number of points

- Conventional assumption does not allow for indivisible objects.
- But suitably modified assumptions may be appropriate

... AND THIS



... AND THIS

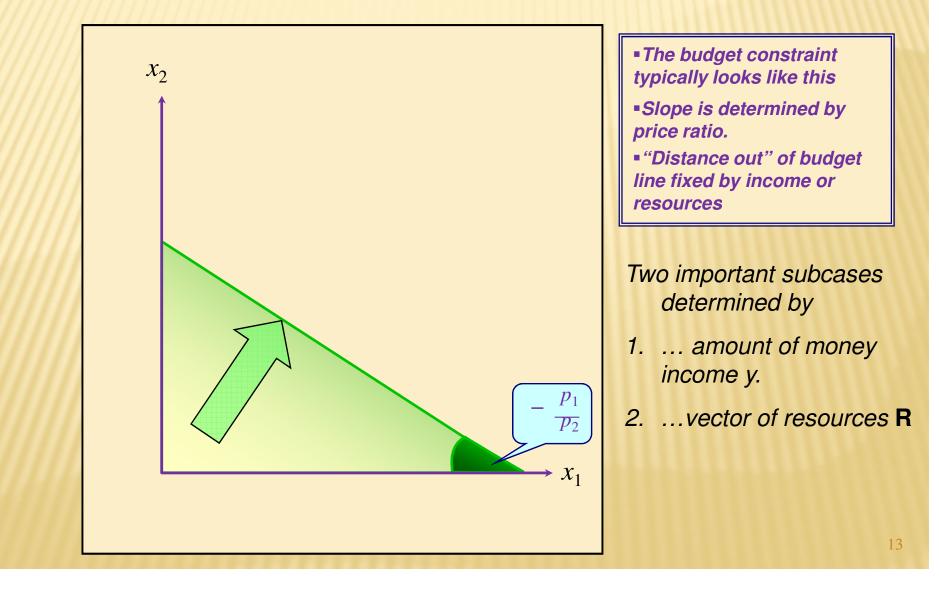


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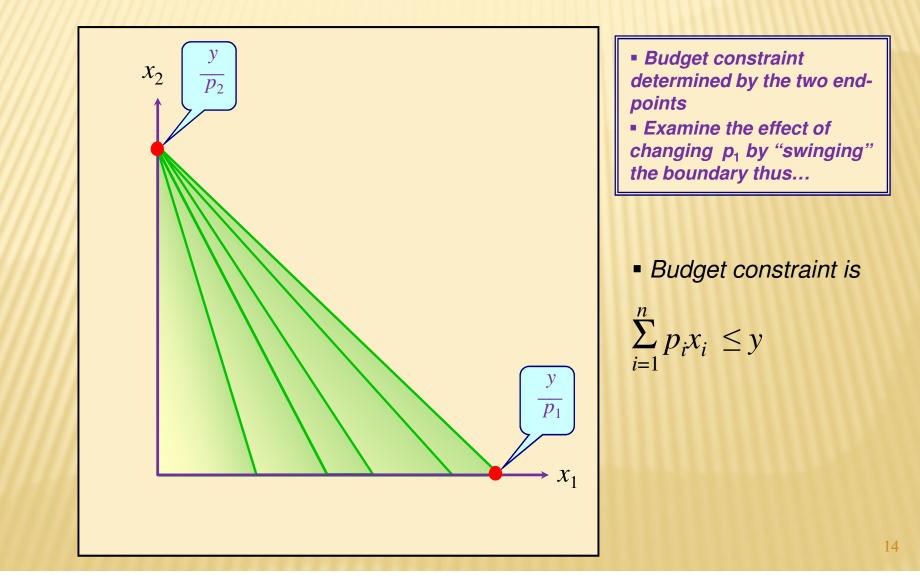
Budget constraints: prices, incomes and resources

Co	nsumption:
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	Approach

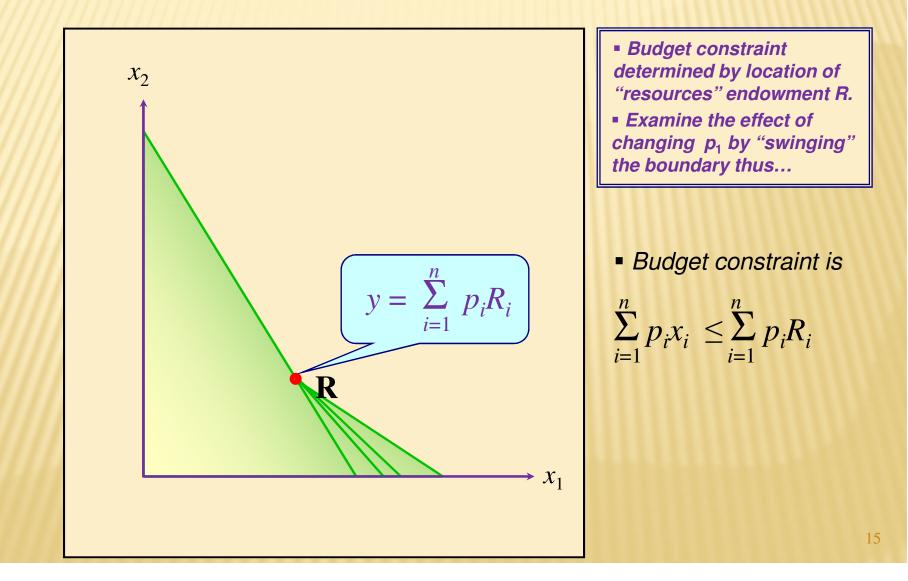
THE BUDGET CONSTRAINT



CASE 1: FIXED NOMINAL INCOME



CASE 2: FIXED RESOURCE ENDOWMENT



BUDGET CONSTRAINT: KEY POINTS

- Slope of the budget constraint given by price ratio.
- There is more than one way of specifying "income":
 - + Determined exogenously as an amount y.
 - + Determined endogenously from resources.
- The exact specification can affect behaviour when prices change.
 - + Take care when income is endogenous.
 - + Value of income is determined by prices.

OVERVIEW	Consumption: Basics	
Deducing preference from market	The setting Budget sets	
behaviour?	Revealed Preference Axiomatic Approach	

A BASIC PROBLEM

- In the case of the firm we have an observable constraint set (input requirement set)...
- ...and we can reasonably assume an obvious objective function (profits)
- **×** But, for the consumer it is more difficult.
- × We have an observable constraint set (budget set)...
- **×** But what objective function?

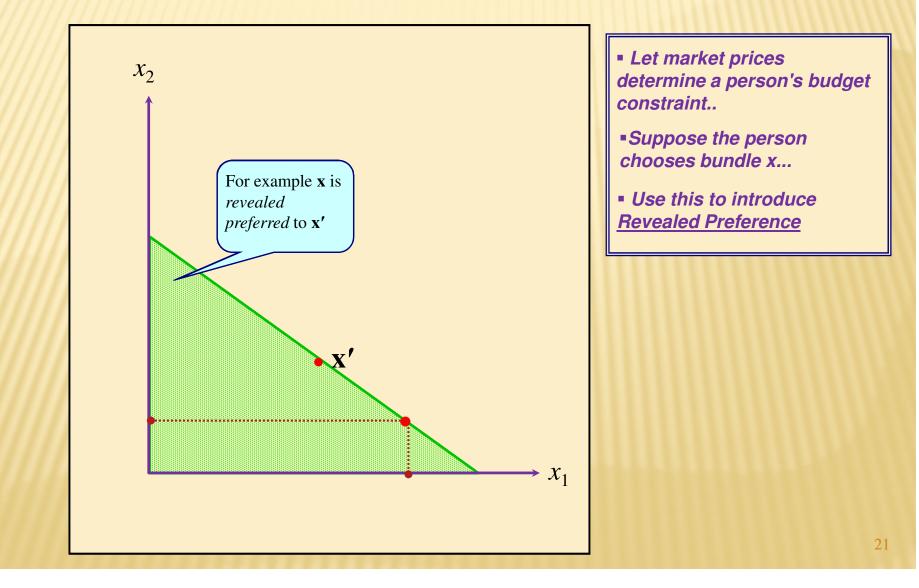
THE AXIOMATIC APPROACH

- **×** We could "invent" an objective function.
- **×** This is more reasonable than it may sound:
 - + It is the standard approach.
 - + See later in this presentation.
- But some argue that we should only use what we can observe:
 - + Test from market data?
 - + The "revealed preference" approach.
 - + Deal with this now.
- Could we develop a coherent theory on this basis alone?

USING OBSERVABLES ONLY

- **×** Model the opportunities faced by a consumer.
- **×** Observe the choices made.
- × Introduce some minimal "consistency" axioms.
- Substitution State St

"REVEALED PREFERENCE"



AXIOMS OF REVEALED PREFERENCE

Axiom of Rational Choice

the consumer always makes a choice, and selects the most preferred bundle that is available.

Essential if observations are to have meaning

Weak Axiom of Revealed Preference (WARP)
If x RP x' then x' not-RP x. If **x** was chosen when **x'** was available then **x'** can never be chosen whenever **x** is available

WARP is more powerful than might be thought

WARP IN THE MARKET

Suppose that x is chosen when prices are p.
If x' is also affordable at p then:

Now suppose x' is chosen at prices p'

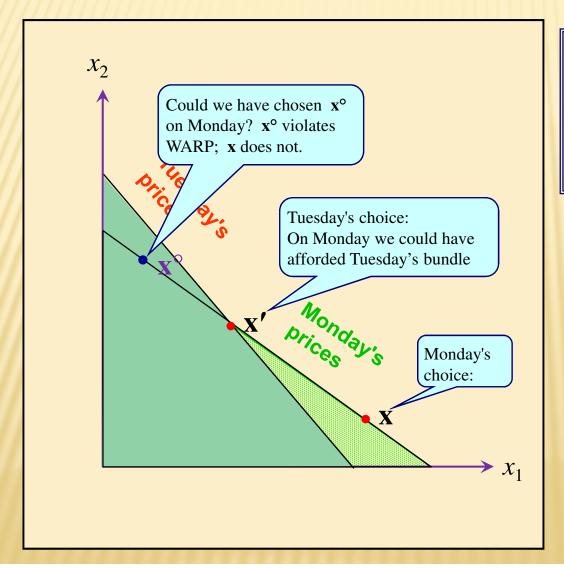
This must mean that **x** is not affordable at **p'**:

 $\sum_{i=1}^{n} p_i x_i \ge \sum_{i=1}^{n} p_i x_i'$

 $\sum_{i=1}^{n} p_i' x_i > \sum_{i=1}^{n} p_i' x_i'$

Otherwise it would violate WARP

WARP IN ACTION



• Take the original equilibrium

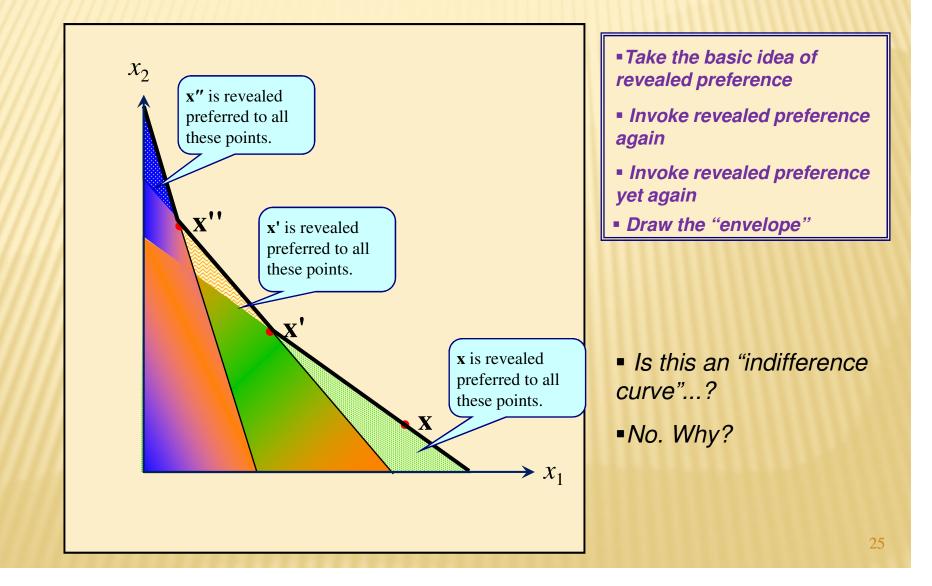
• Now let the prices change...

•WARP rules out some points as possible solutions

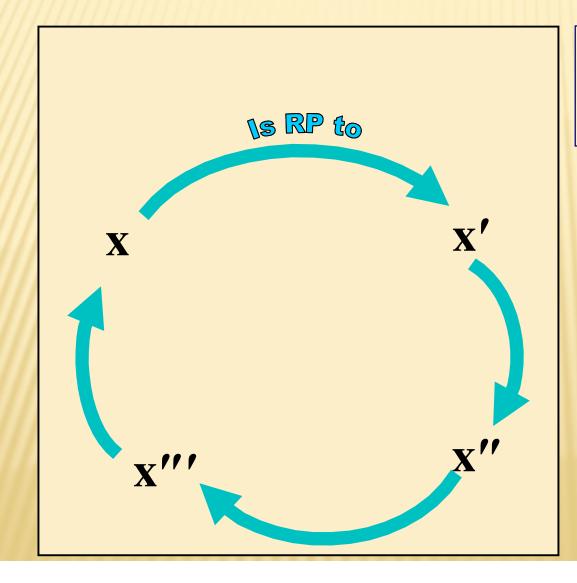
 Clearly WARP induces a kind of negative substitution effect

But could we extend this idea...?

TRYING TO EXTEND WARP



LIMITATIONS OF WARP



 WARP rules out this pattern

....but not this

 WARP does not rule out cycles of preference

• You need an extra axiom to progress further on this:

the strong axiom of revealed preference.

REVEALED PREFERENCE: IS IT USEFUL?

× You can get a lot from just a little: + You can even work out substitution effects. **×** WARP provides a simple consistency test: + Useful when considering consumers en masse. + WARP will be used in this way later on. **×** You do not need any special assumptions about consumer's motives: + But that's what we're going to try right now. + It's time to look at the mainstream modelling of preferences.

OVERVIEW.	
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Standard approach to modelling preferences

0	nsumption:
Bas	sics
	The setting
	Budget sets
	Revealed
	Preference
	Axiomatic
	Approach

THE AXIOMATIC APPROACH

- Setup Set
- **×** But, be careful...
- x ...axioms can't be "right" or "wrong,"...
- although they could be inappropriate or over-restrictive.
- **×** That depends on what you want to model.
- **×** Let's start with the basic relation...

THE (WEAK) PREFERENCE RELATION

• The basic weak-preference relation:

"Basket **x** is regarded as <u>at</u> least as good as basket x' ... "

X < X'

• From this we can derive the "x < x'" and "x' < x." indifference relation.

 $\mathbf{x} \vee \mathbf{x'}$

• ...and the strict preference relation...

xÂx'

"x < x'" and not "x' < x."

FUNDAMENTAL PREFERENCE AXIOMS

× Completeness

For every $\mathbf{x}, \mathbf{x}' \in X$ either $\mathbf{x} < \mathbf{x}'$ is true, or $\mathbf{x}' < \mathbf{x}$ is true, or both statements are true

- × Transitivity
- × Continuity
- × Greed
- × (Strict) Quasi-concavity
- × Smoothness

FUNDAMENTAL PREFERENCE AXIOMS

× Completeness

- × Transitivity
- × Continuity
- × Greed
- × (Strict) Quasi-concavity
- × Smoothness

For all $\mathbf{x}, \mathbf{x}', \mathbf{x}'' \in X$ if $\mathbf{x} < \mathbf{x}'$ and $\mathbf{x}' < \mathbf{x}''$ then $\mathbf{x} < \mathbf{x}''$.

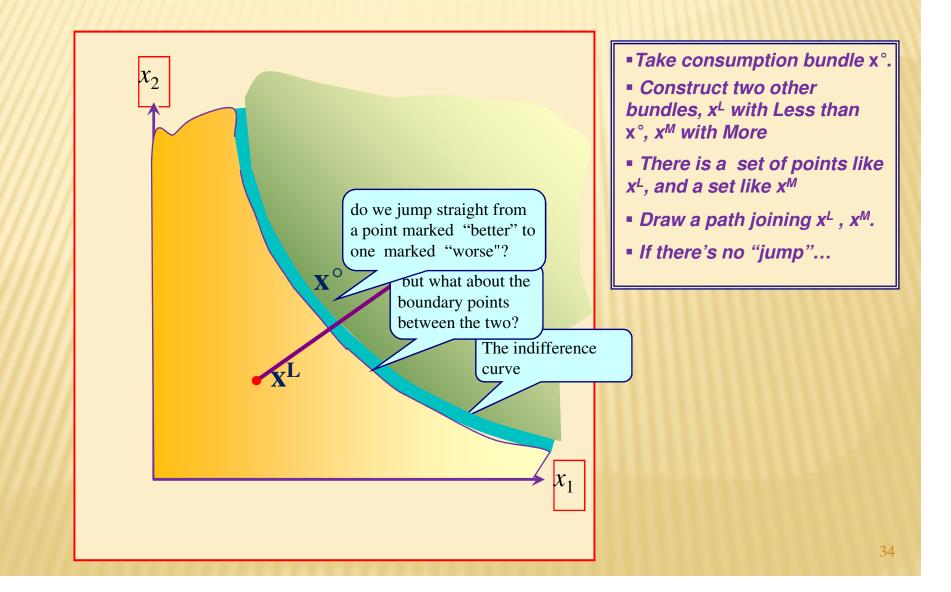
FUNDAMENTAL PREFERENCE AXIOMS

- × Completeness
- × Transitivity
- × Continuity

For all $\mathbf{x}' \in X$ the not-better-than- \mathbf{x}' set and the not-worse-than- \mathbf{x}' set are closed in X

- × Greed
- × (Strict) Quasi-concavity
- × Smoothness

CONTINUITY: AN EXAMPLE



AXIOMS 1 TO 3 ARE CRUCIAL ...

completenesstransitivity

•continuity

The utility function

A CONTINUOUS UTILITY FUNCTION THEN REPRESENTS PREFERENCES...

 $\mathbf{X} < \mathbf{X}'$



TRICKS WITH UTILITY FUNCTIONS

- **×** *U*-functions represent preference orderings.
- × So the utility scales don't matter.
- And you can transform the U-function in any (monotonic) way you want...

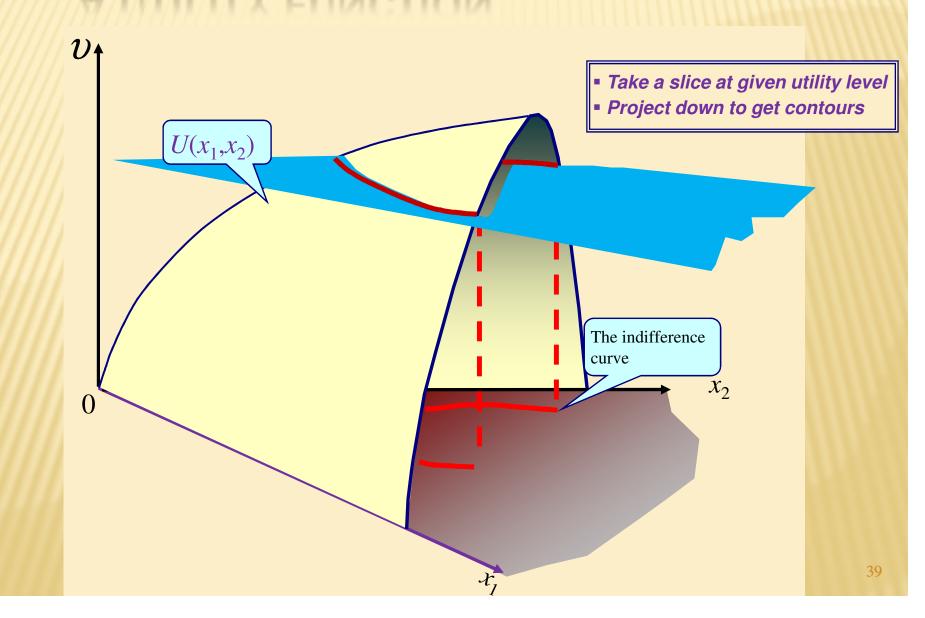
IRRELEVANCE OF CARDINALISATION

- $U(x_1, x_2, ..., x_n)$
- $\log(U(x_1, x_2, ..., x_n))$
- exp($U(x_1, x_2, ..., x_n)$)
- $\sqrt{(U(x_1, x_2, ..., x_n))}$
- $\varphi(U(x_1, x_2, ..., x_n))$

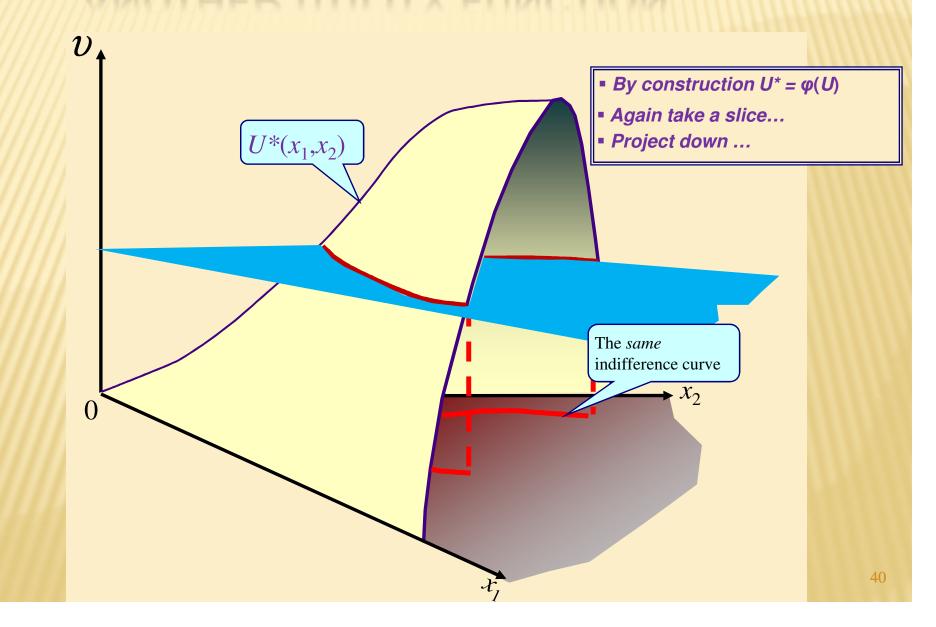
- So take any utility function.
- This transformation represents the same preferences...
- ...and so do both of these
- And, for any monotone increasing φ, this represents the same preferences.

- U is defined up to a monotonic transformation
- Each of these forms will generate the same contours.
- •Let's view this graphically.

A UTILITY FUNCTION



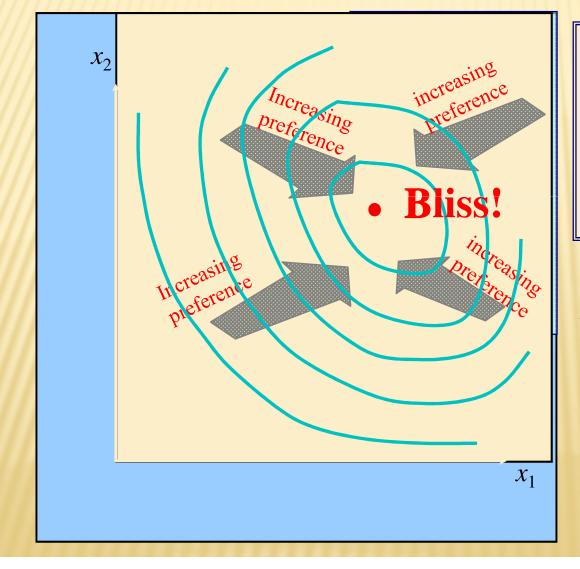
ANOTHER UTILITY FUNCTION



ASSUMPTIONS TO GIVE THE U-FUNCTION

- SHAPE
- × Completeness
- × Transitivity
- × Continuity
- × Greed
- × (Strict) Quasi-concavity
- Smoothness

THE GREED AXIOM



• Pick any consumption bundle in X.

- Greed implies that these bundles are preferred to x'.
- Gives a clear "North-East" direction of preference.

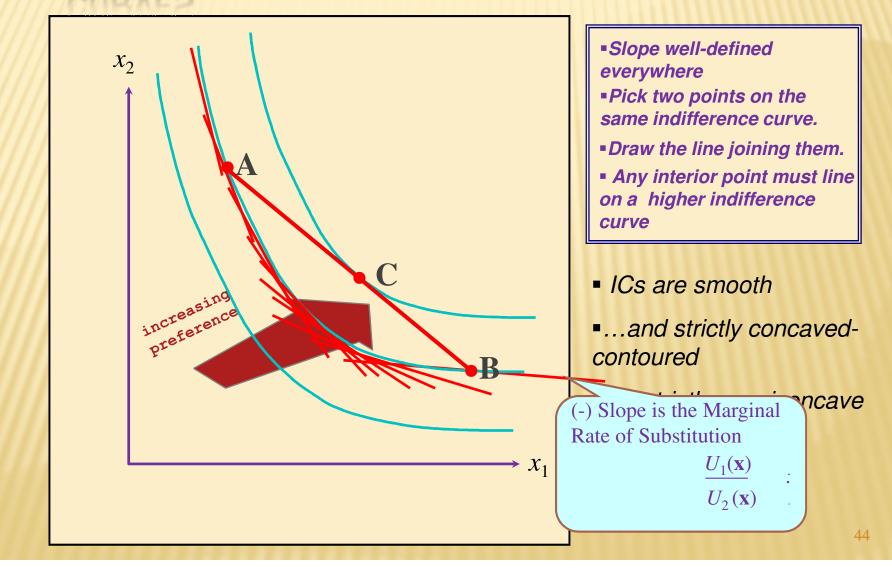
What can happen if consumers are not greedy

 Greed: utility function is monotonic

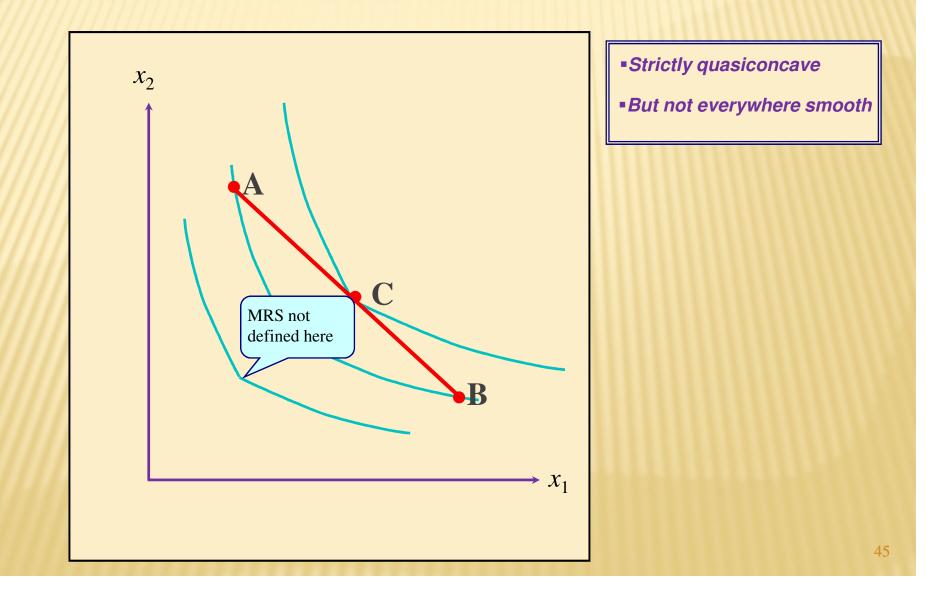
A KEY MATHEMATICAL CONCEPT

- **x** We've previously used the concept of concavity:
 - + Shape of the production function.
- **×** But here simple concavity is inappropriate:
 - + The U-function is defined only up to a monotonic transformation.
 - + *U* may be concave and *U*² non-concave even though they represent the same preferences.
- **×** So we use the concept of "quasi-concavity":
 - + "Quasi-concave" is equivalently known as "concave contoured".
 - + A concave-contoured function has the same contours as a concave function (the above example).
 - + Somewhat confusingly, when you draw the IC in (x_1, x_2) -space, common parlance describes these as "convex to the origin."
- **×** It's important to get your head round this:
 - + Some examples of ICs coming up...

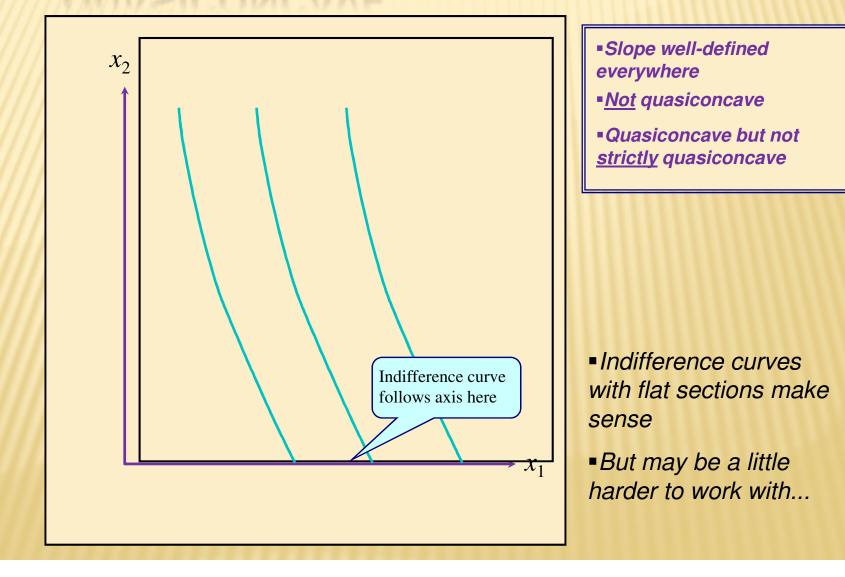
CONVENTIONALLY SHAPED INDIFFERENCE CURVES



OTHER TYPES OF IC: KINKS



OTHER TYPES OF IC: NOT STRICTLY QUASICONCAVE



SUMMARY: WHY PREFERENCES CAN BE A PROBLEM

- Substitution Number of States and States
- Unlike firms there is no observable objective function.
- And who is to say what constitutes a "good" assumption about preferences...?

REVIEW: BASIC CONCEPTS

Consumer's environment

- **×** How budget sets work
- **×** WARP and its meaning
- * Axioms that give you a utility function
- **x** Axioms that determine its shape

WHAT NEXT?

Setting up consumer's optimisation problem
Comparison with that of the firm
Solution concepts.