

Web Workload characterisation

- Workload: the set of all inputs a system receives over a time period.
- Workload identification → performance evaluation techniques (simulation, benchmarking, etc.)
- Web workload: HTTP message characteristics, Resource characteristics, User behaviour

Web Workload Parameters

- Protocol: request method, response code
- Resource: content type, resource size, response size, popularity, modification frequency, temporal locality, embedded resources
- user: session inter-arrival times, request inter-arrival times

HTTP Request methods

- Vast majority of requests: GET method to retrieve documents and execute scripts
- small fraction: use of POST method
- Future trends: WebDAV (Distributed authoring and versioning) may increase PUT/DELETE percentage, tracing/debugging web components may increase TRACE method.

HTTP response codes

- 200 OK status code: 75% to 90% of responses.
- Next most common response code: 304 Not modified - typically 10% to 30%
- Other popular status codes: redirection (3xx) and client error (4xx).
- Future trends: sophistication level of HTTP clients e.g., 206 partial content

Web resource characteristics

- Resource size: average resource size for HTML files: 4KB - 8 KB.
Image Average Resource Size: 14 KB.

- Wide variability in the HTML file sizes.
- The high variability is captured by the Pareto distribution.

$$F(x) = (k / x)^{\alpha}, x \geq k$$

- Shape parameter α , and scale parameter k .
- Mean = $(k\alpha) / (\alpha - 1)$
- Pareto distribution is heavy tailed for values of α between 0 and 2.
- Random variables whose distributions are heavy tailed exhibit very high variability: infinite variance, and if $\alpha \leq 1$, infinite mean.

Web Resource sizes

- Pareto shape parameter, α , for Web resources is between 1.0 and 1.5.
- Pareto is not a good approximation for resources of limited size. Only for large resources.
- Body of distribution is better modeled through the lognormal distribution.

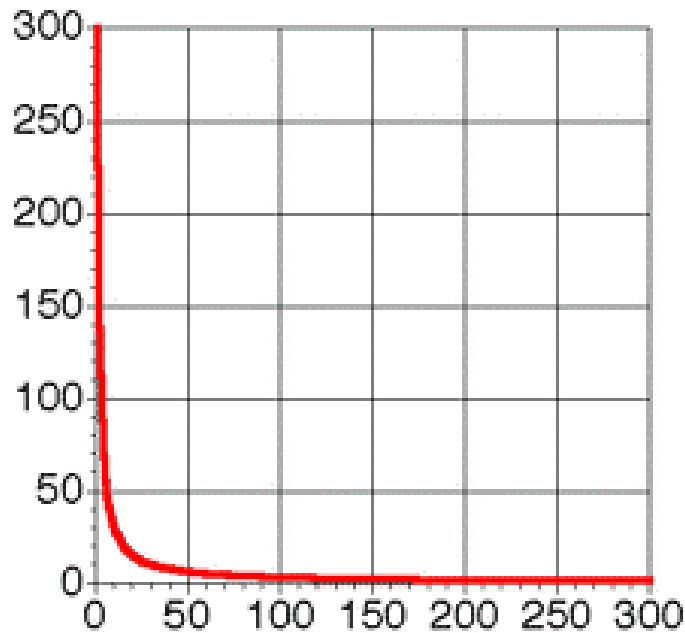
Zipf Law

Zipf's law usually refers to the 'size' y of an occurrence of an event relative to its rank r . George Kingsley Zipf, a Harvard linguistics professor, sought to determine the 'size' (or frequency of use in English text) of the 3rd or 8th or 100th most common word. **Zipf's law states that the size of the r 'th largest occurrence of the event is inversely proportional to its rank:**

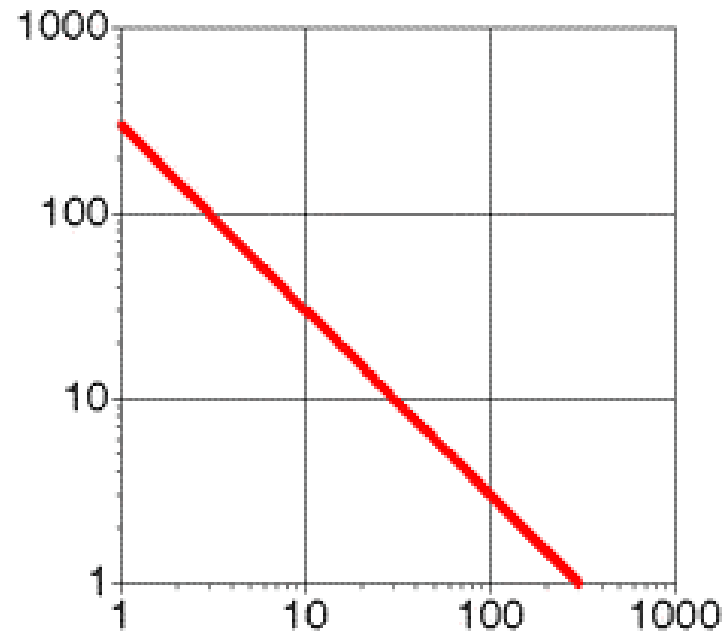
$$y \sim r^{-b}, \text{ with } b \text{ close to unity.}$$

GK Zipf, *Human Behavior and the Principle of Least Effort* (Addison-Wesley, 1949).

Zipf Distribution



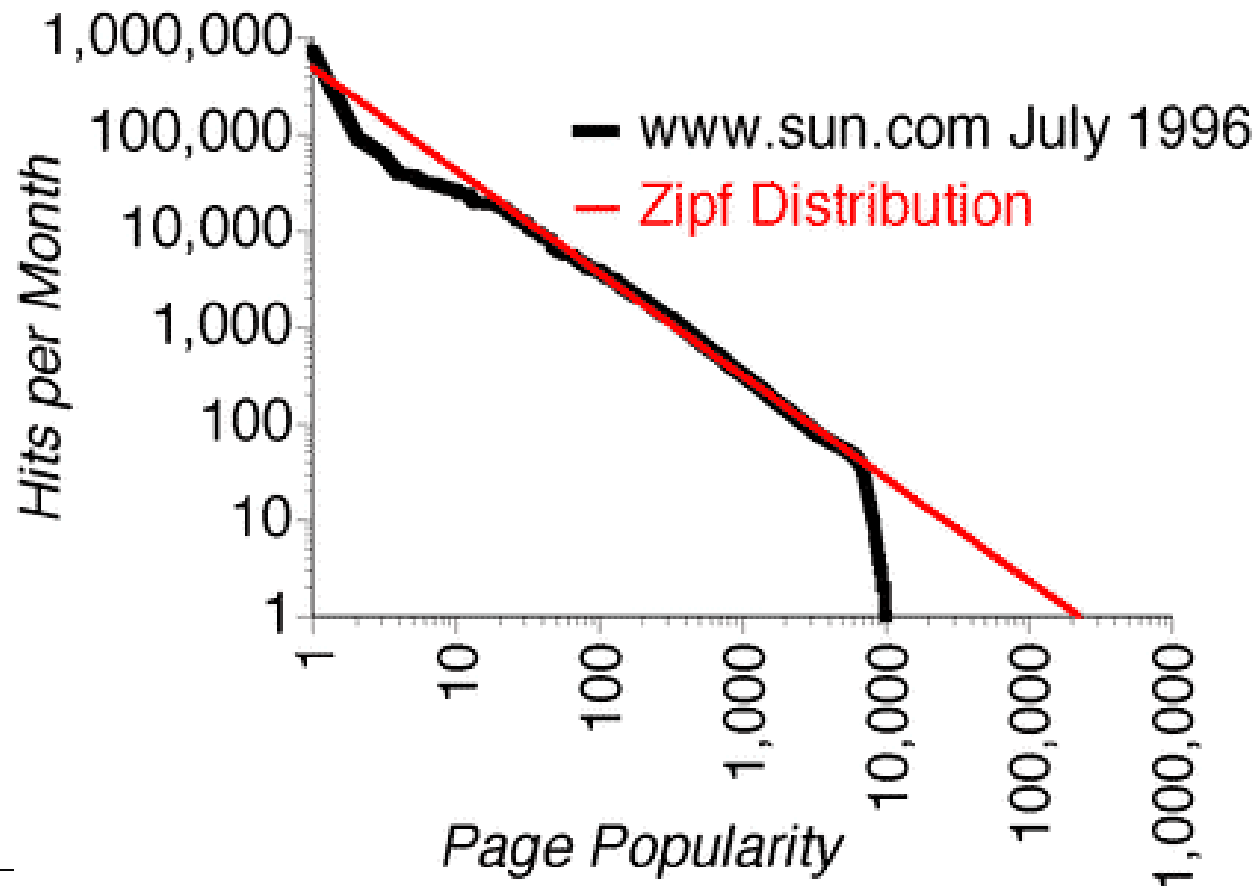
Linear scales on both axes



Logarithmic scales on both axes

The same data plotted on linear and logarithmic scales. Both plots show a Zipf distribution with 300 datapoints.

Zipf Distribution



Pareto Law

Pareto was interested in the distribution of income. Instead of asking what the r th largest income is, he asked how many people have an income greater than x . **Pareto's law** is given in terms of the cumulative distribution function (CDF), i.e. the number of events larger than x is an inverse power of x :

$$P[X > x] \sim x^{-k}.$$

It states that there are a few multi-billionaires, but most people make only a modest income.

Pareto Distribution

The Pareto distribution gives the probability that a person's income is greater than or equal to x :

$$\Pr[X \geq x] = (m/x)^k, \quad m > 0, k > 0, x \geq m,$$

where m represents a minimum income. As a consequence, the CDF

$$\Pr[X < x] = 1 - (m/x)^k$$

and the PDF is

$$p_X(x) = k m^k x^{-(k+1)}, \quad m > 0, k > 0, x \geq m$$

Temporal locality

- The time between successive requests for the same resource.
- Temporal locality captures the likelihood that a requested resource will be requested again in the near future.
- Measurement: stack distance.
- (a,b,a,b,a,b,a) vs (a,a,a,a,b,b,b): first stream exhibits lower temporal locality than the second.
- Small stack distances: higher temporal locality.
- Distribution of temporal locality: lognormal distribution.

Embedded References

- Web pages have a median of 8 to 20 embedded references.
- The respective distribution has high variability, following the pareto distribution.

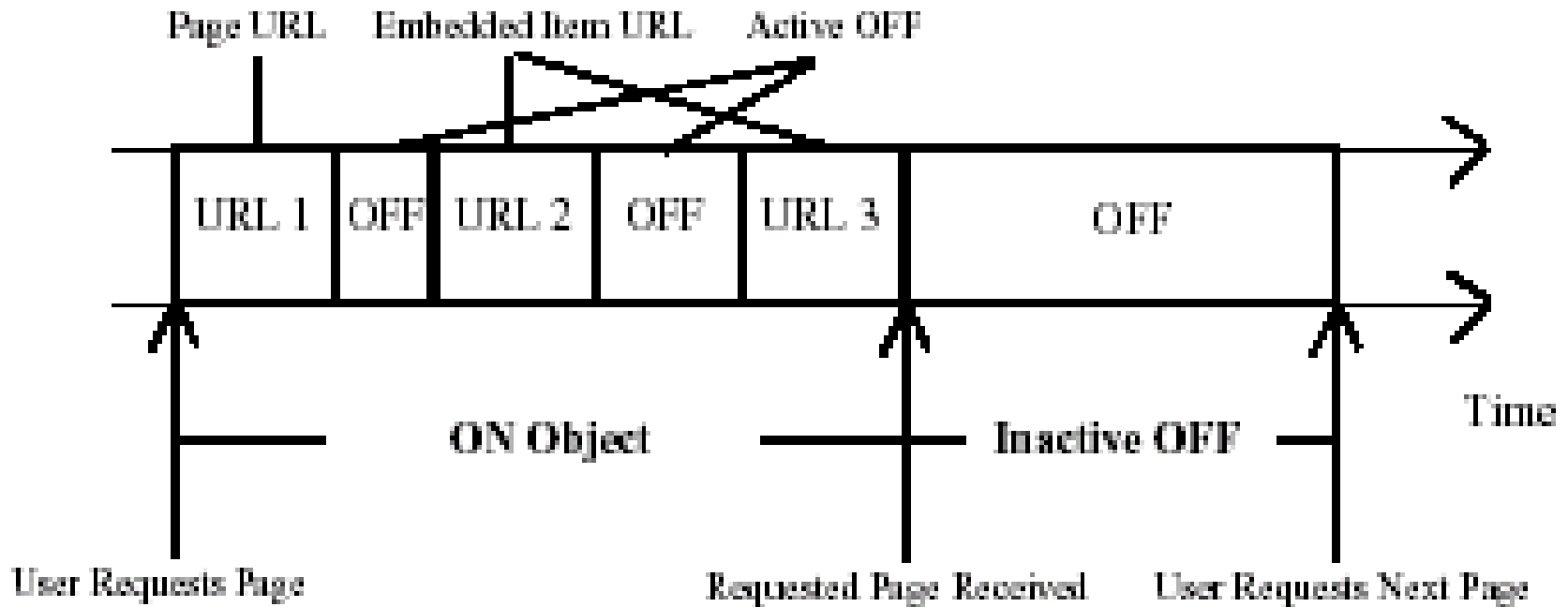
Session inter-arrival times.

- Session inter-arrival times follow the exponential distribution.
- Exponential model is not adequate for interarrival times of TCP connections and HTTP requests.

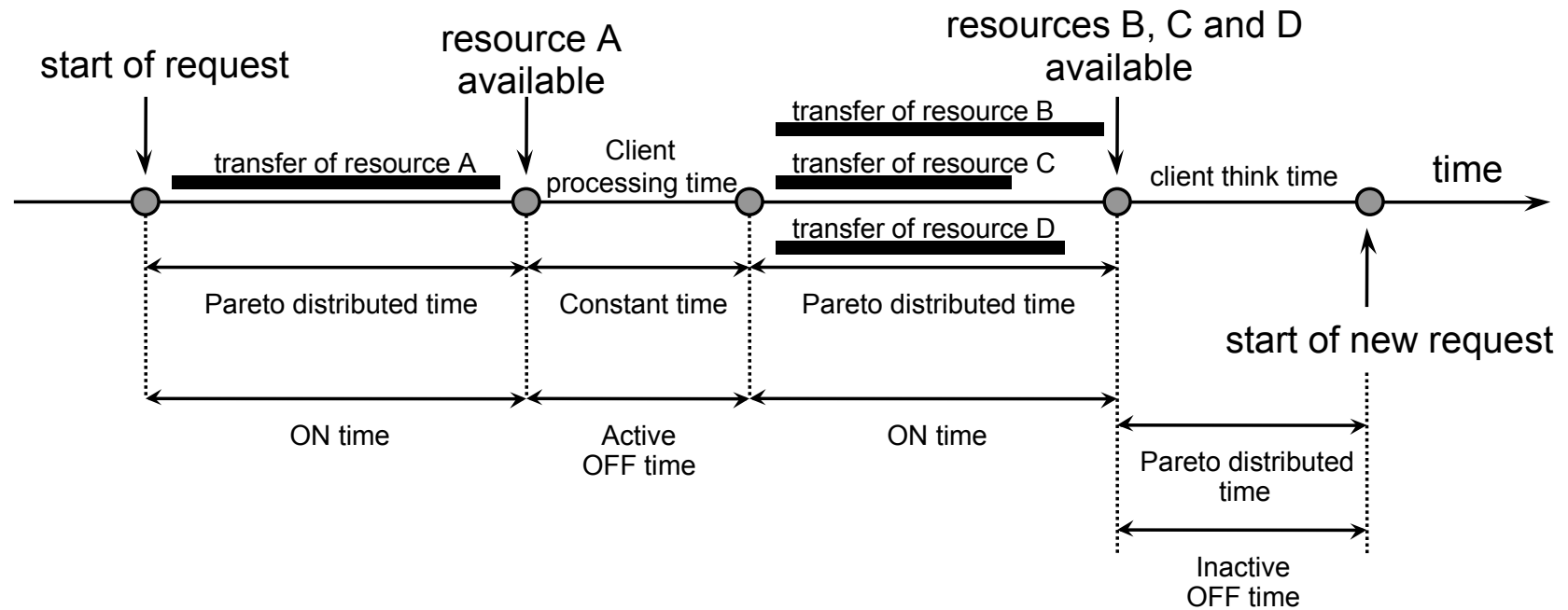
Web traffic models

- WWW traffic exhibits characteristics consistent with self-similar traffic models.
- Self-similarity is attributed to the multiplexing of a large number of ON/OFF sources where both the ON and the OFF period lengths are heavy tailed processes.
- ON times correspond to WWW resource transmissions while the OFF times correspond to intervals of client/browser inactivity.
- OFF times are classified either as Active (attributed to client processing delays: parsing, rendering) or as Inactive (user think time).

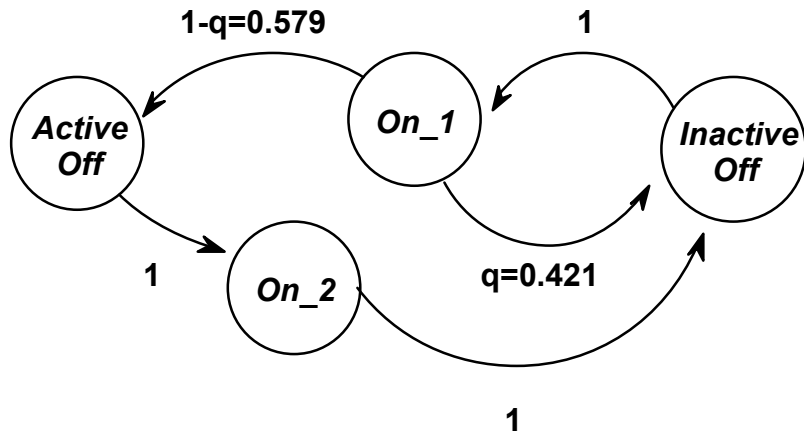
Web traffic model



Web traffic model



Web traffic chain



- On_1: HTML page retrieval
- On_2: retrieval of embedded references
- Inactive Off ~ Pareto
- On_1 ~ Pareto
- On_2 ~ Pareto
- Active Off ~ Weibull

Web model statistics

Component	Model	Probability Density Function	Parameters
File Sizes – Body	Lognormal	$p(x) = \frac{1}{x\sigma\sqrt{2\pi}} e^{-(\ln x - \mu)^2 / 2\sigma^2}$	$\mu = 9.357; \sigma = 1.318$
File Sizes – Tail	Pareto	$p(x) = \alpha k^\alpha x^{-(\alpha+1)}$	$k = 133K; \alpha = 1.1$
Popularity	Zipf		
Temporal Locality	Lognormal	$p(x) = \frac{1}{x\sigma\sqrt{2\pi}} e^{-(\ln x - \mu)^2 / 2\sigma^2}$	$\mu = 1.5; \sigma = 0.80$
Request Sizes	Pareto	$p(x) = \alpha k^\alpha x^{-(\alpha+1)}$	$k = 1000; \alpha = 1.0$
Active OFF Times	Weibull	$p(x) = \frac{bx^{b-1}}{a^b} e^{-(x/a)^b}$	$a = 1.46; b = 0.382$
Inactive OFF Times	Pareto	$p(x) = \alpha k^\alpha x^{-(\alpha+1)}$	$k = 1; \alpha = 1.5$
Embedded References	Pareto	$p(x) = \alpha k^\alpha x^{-(\alpha+1)}$	$k = 1; \alpha = 2.43$

Self-Similar processes

Traffic processes are said to be self-similar if they look qualitatively the same irrespective of the time scale from which we look at them.

